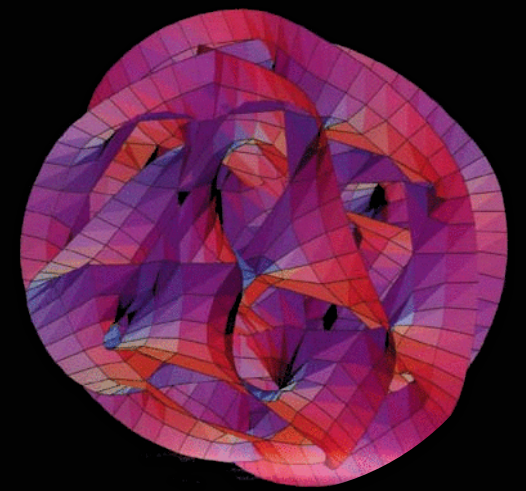
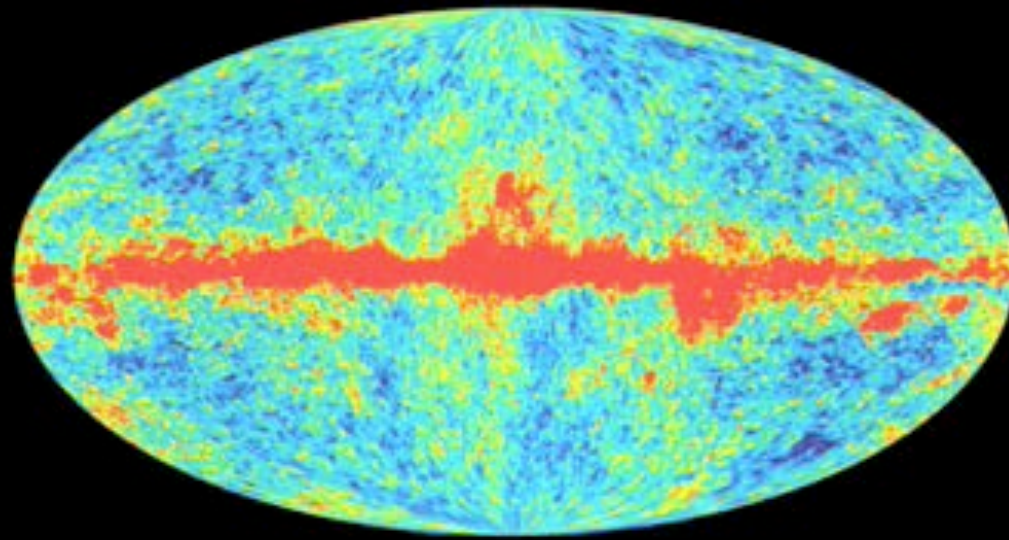
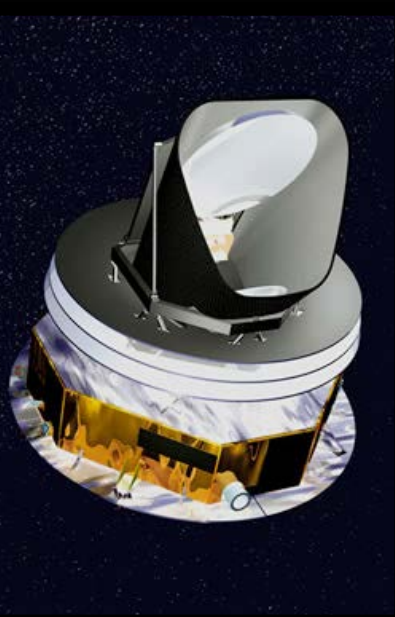


ULTRA-LIGHT AXIONS AND THE COSMIC MICROWAVE BACKGROUND

DANIEL GRIN
HAVERFORD COLLEGE

PICO WORKSHOP
5/1/2018



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OUTLINE

- ✦ Ultra-light Axion (ULA) fundamentals
- ✦ Testing **axion** dark matter and dark energy using the CMB
- ✦ Future work

Collabs: R.Hložek, D.J. E. Marsh, P.Ferreira, J. Dunkley, E. Calabrese, R.Allison



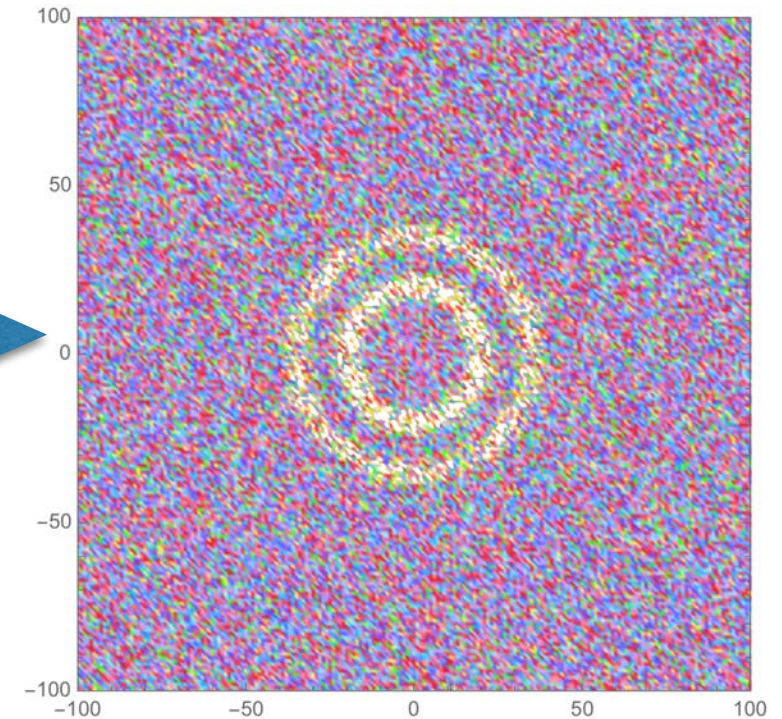
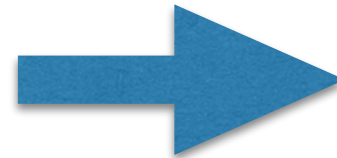
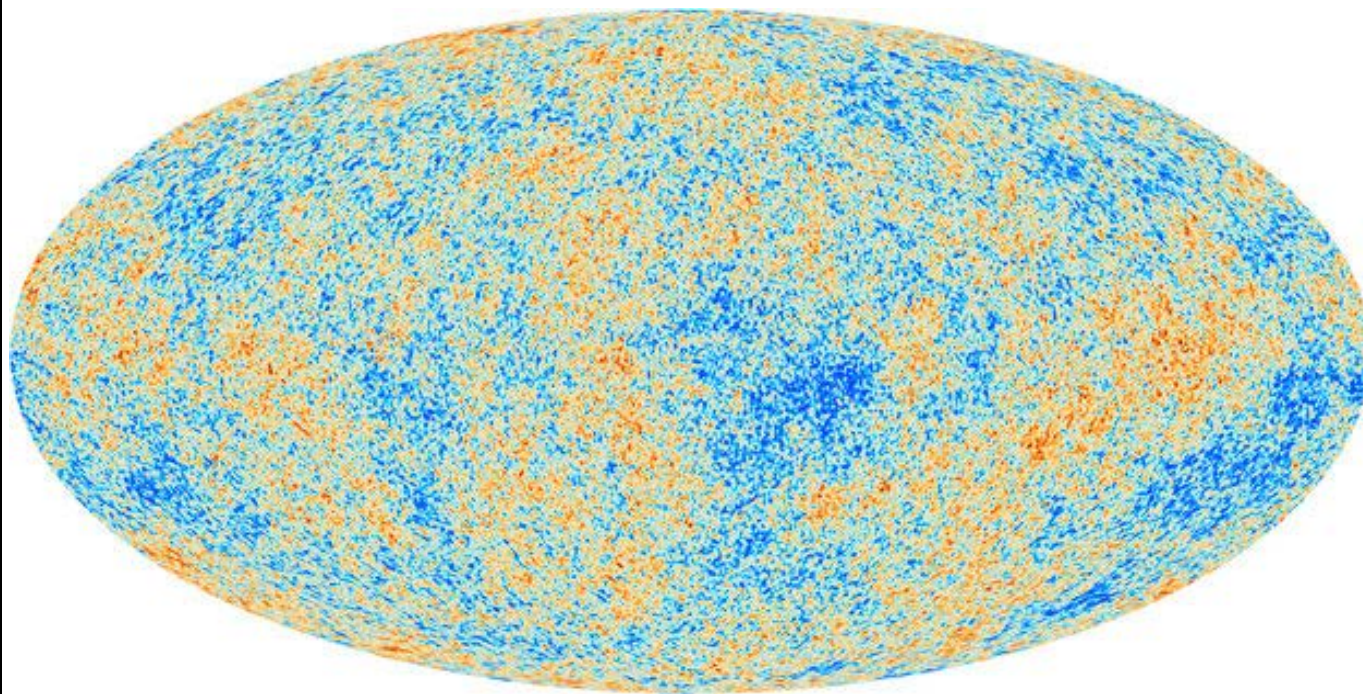
G. Given, E. Trott, D. Zegeye, S. Ditkovsky, J. Cookmeyer, M. Shea



FOURIER ANALYSIS OF PRIMORDIAL SOUND

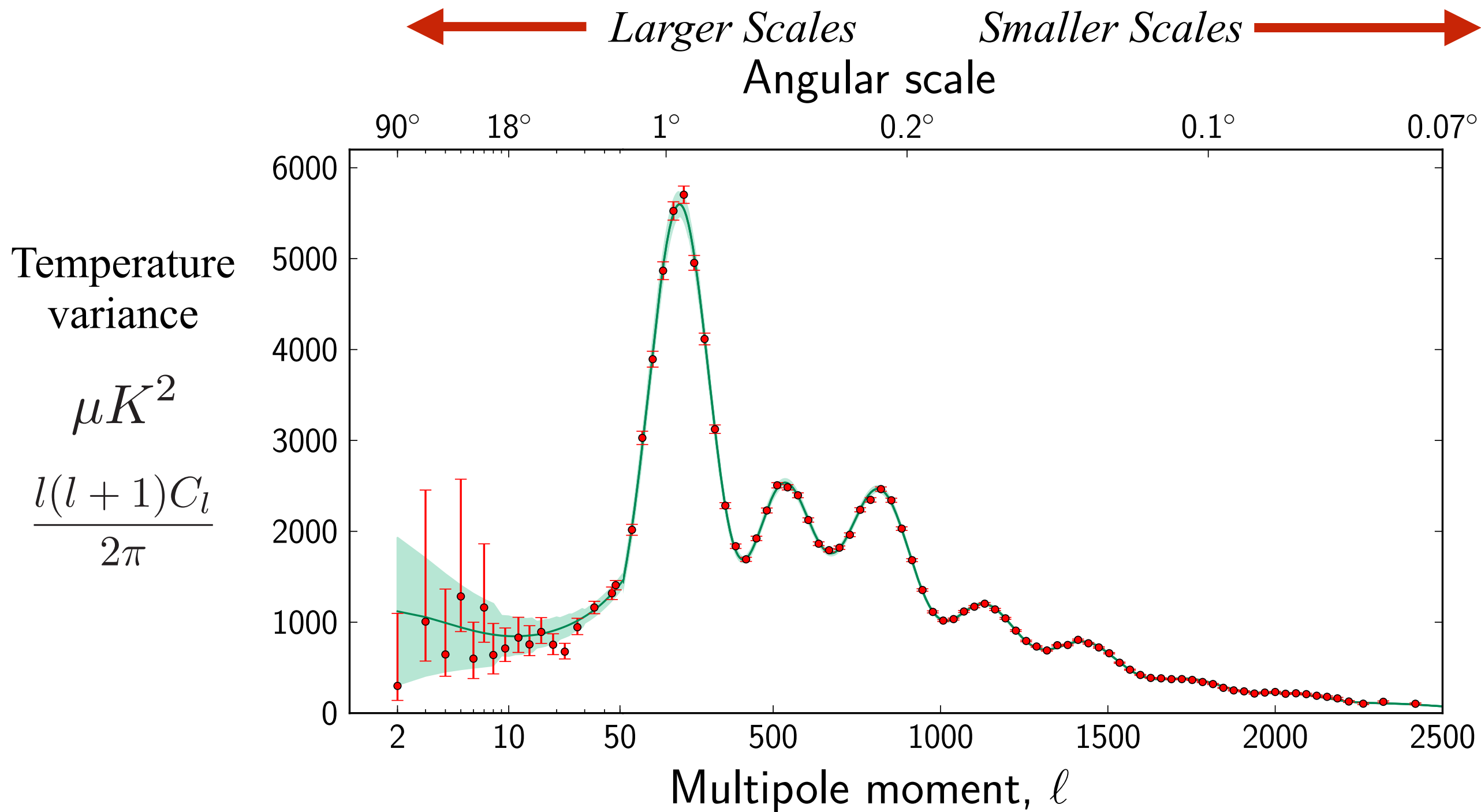
$$T(\vec{\theta})$$

$$a(\vec{k}) = \int T(\vec{\theta}) e^{i\vec{\theta} \cdot \vec{k}} d^2\theta$$



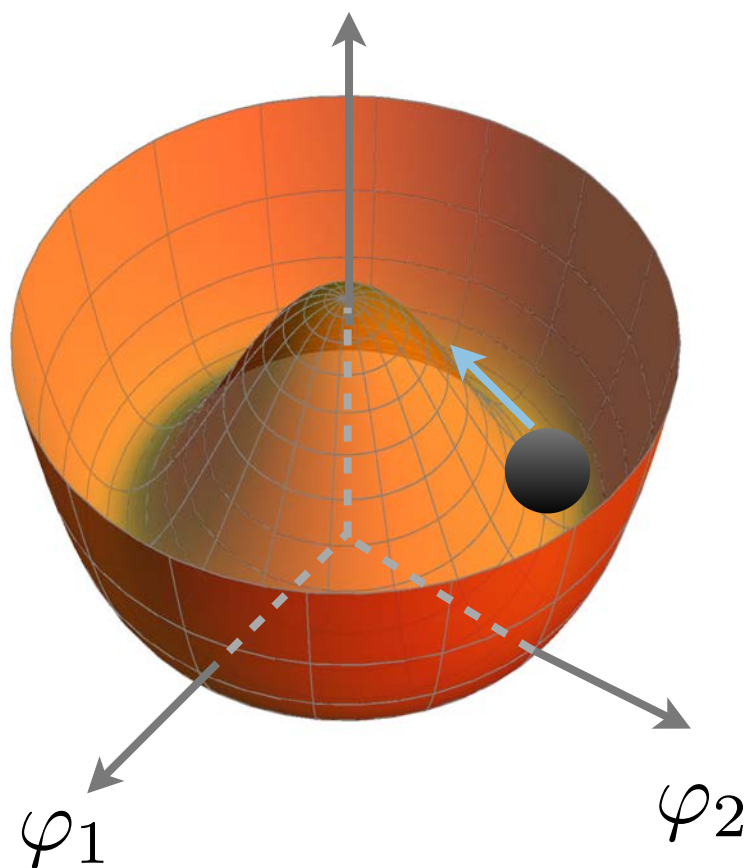
What can the CMB tell us about dark-matter and dark-energy particle physics?

FOURIER ANALYSIS OF PRIMORDIAL SOUND



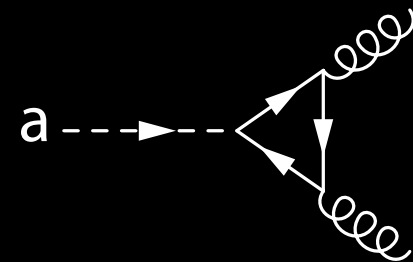
What can the CMB tell us about dark-matter and dark-energy particle physics?

WHAT ARE AXIONS?



New scalar field with global U(1) symmetry!

$$\mathcal{L}_{\text{CPV}} = \frac{\theta g^2}{32\pi^2} G\tilde{G} - \frac{a}{f_a} g^2 G\tilde{G}$$



✱ Couples to SM gauge fields (via fermions)

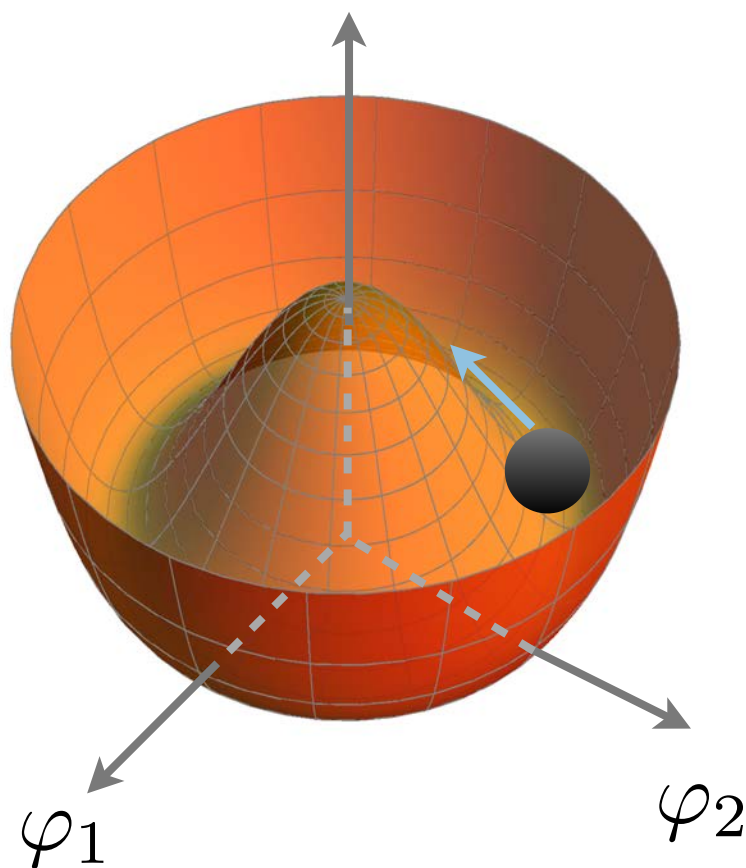
✱ Dynamically erases QCD CP-violation

✱ Axion gets mass through non-perturbative QCD effects

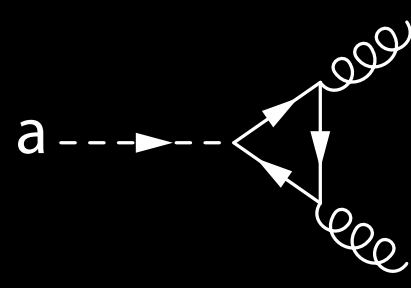
$$m_a \sim \frac{\Lambda_{\text{QCD}}^2}{f_a}$$

Peccei + Quinn (1977), Weinberg + Wilczek (1978), Kim (1979), Shifman et. al (1980), Zhitnitsky (1980), Dine et al. (1981), D.B. Kaplan (1985), A.E Nelson (1985,1990)

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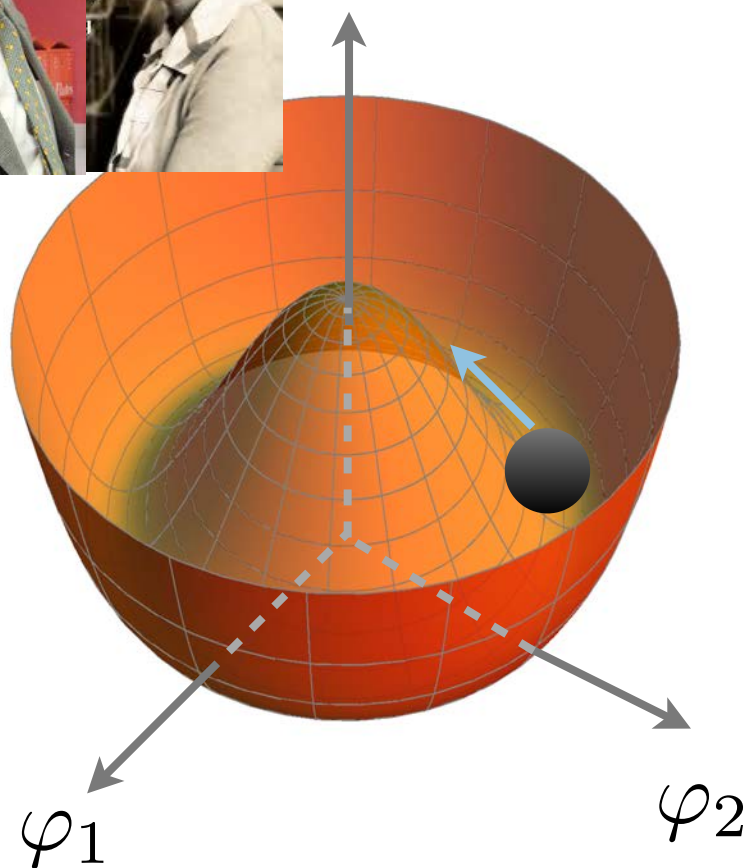
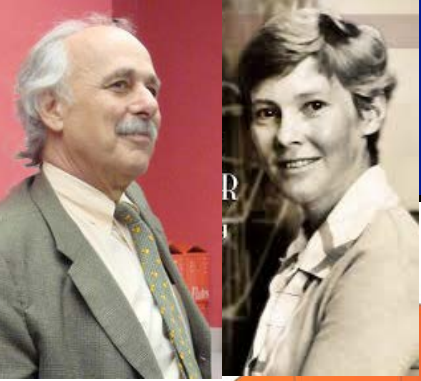
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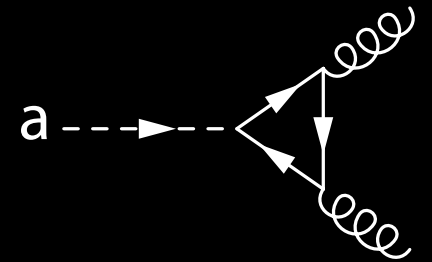
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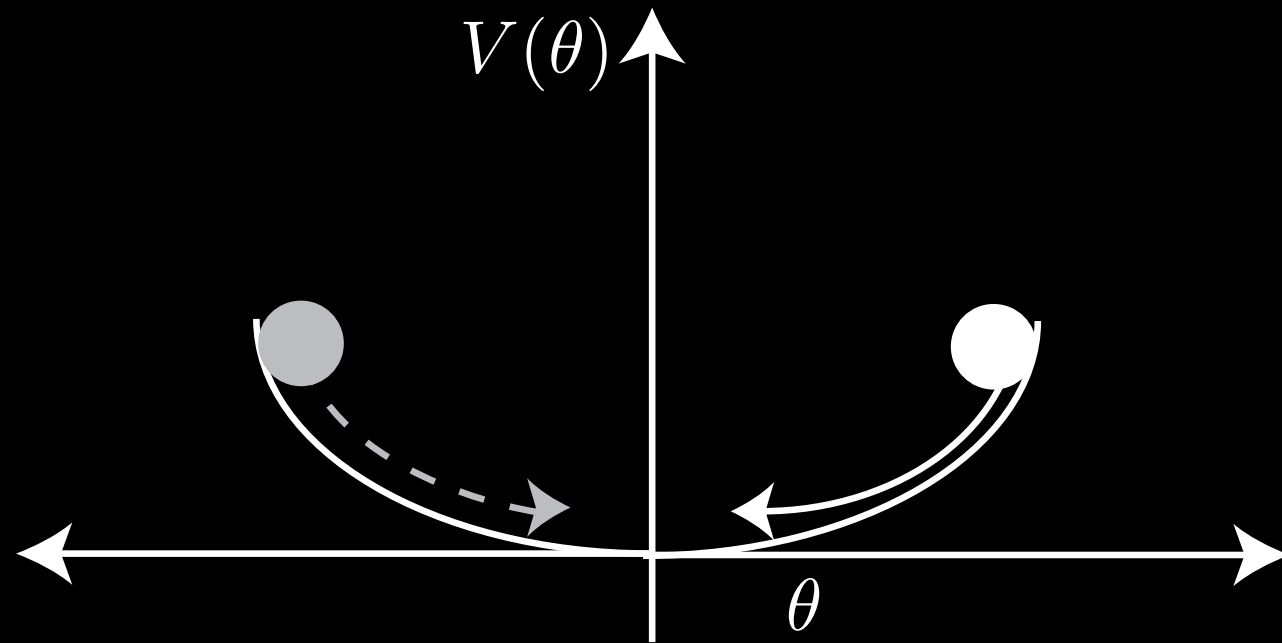
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2 axion populations: Cold axions

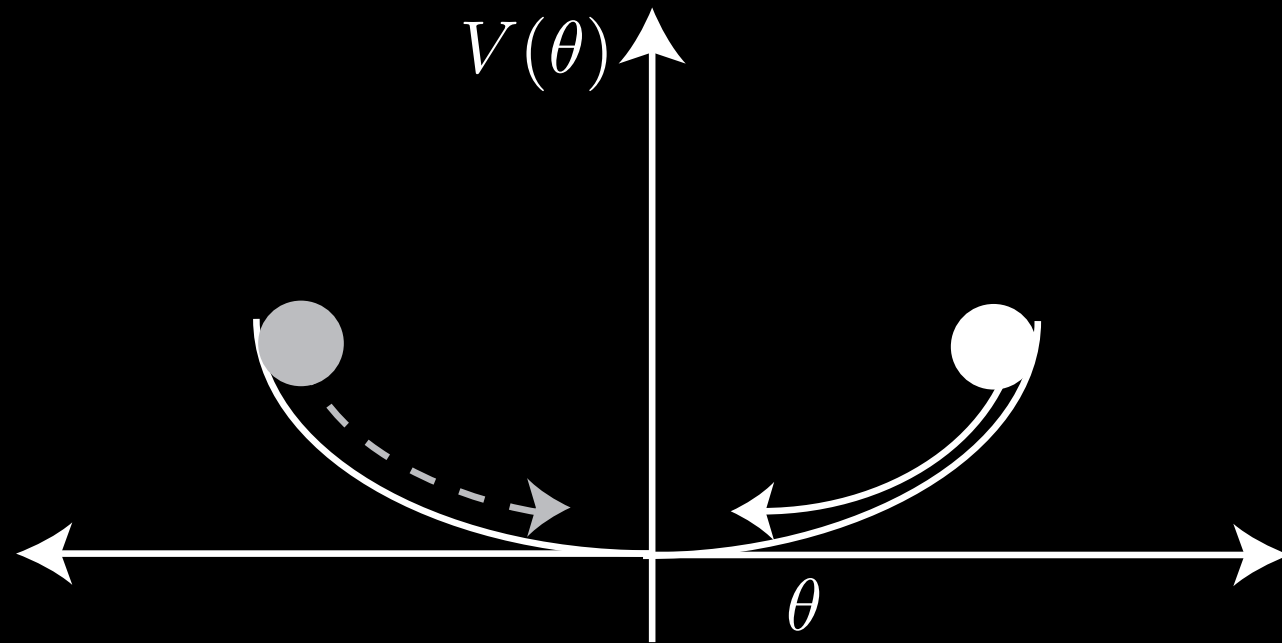
$$m_a < 10^{-2} \text{ eV}$$



- * Before PQ symmetry breaking, θ is generically displaced from vacuum value
- * EOM: $\ddot{\bar{\theta}} + 3H\dot{\bar{\theta}} + m_a^2(T)\bar{\theta} = 0$ $m_a(T) \simeq 0.1m_a(T=0)(\Lambda_{\text{QCD}}/T)^{3.7}$
- * After $m_a(T) \gtrsim 3H(T)$, coherent oscillations begin, leading to $n_a \propto a^{-3}$
- * Axions are cold $p \ll m_a c$

2 axion populations: Cold axions

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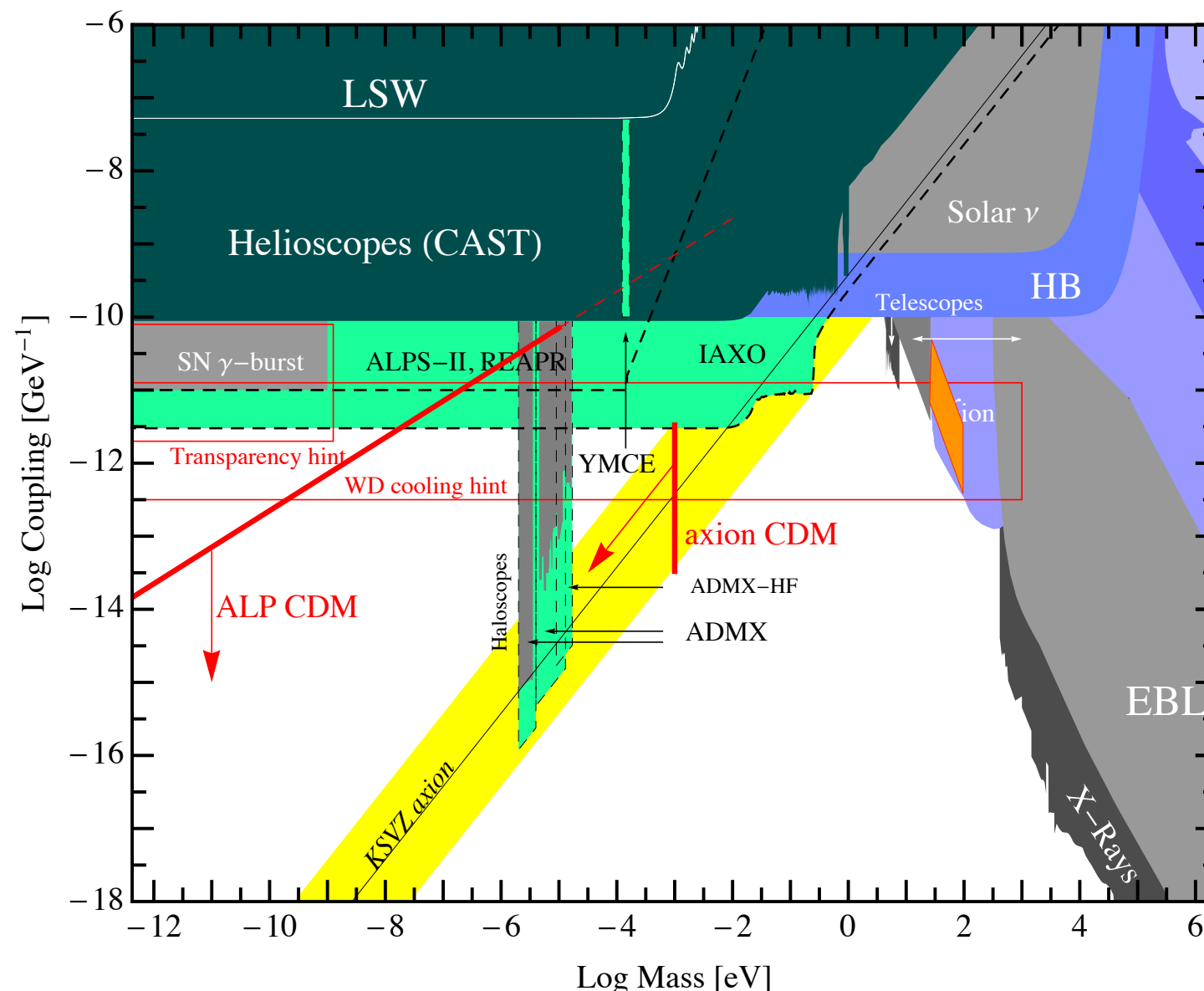
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* After $m_a(T) \gtrsim 3H(T)$, coherent oscillations begin, leading to $n_a \propto a^{-3}$

*
$$\Omega_{\text{mis}} h^2 = 0.236 \langle \theta_i^2 f(\theta_i) \rangle \left(\frac{m_a}{6.2 \mu\text{eV}} \right)^{-7/6}$$

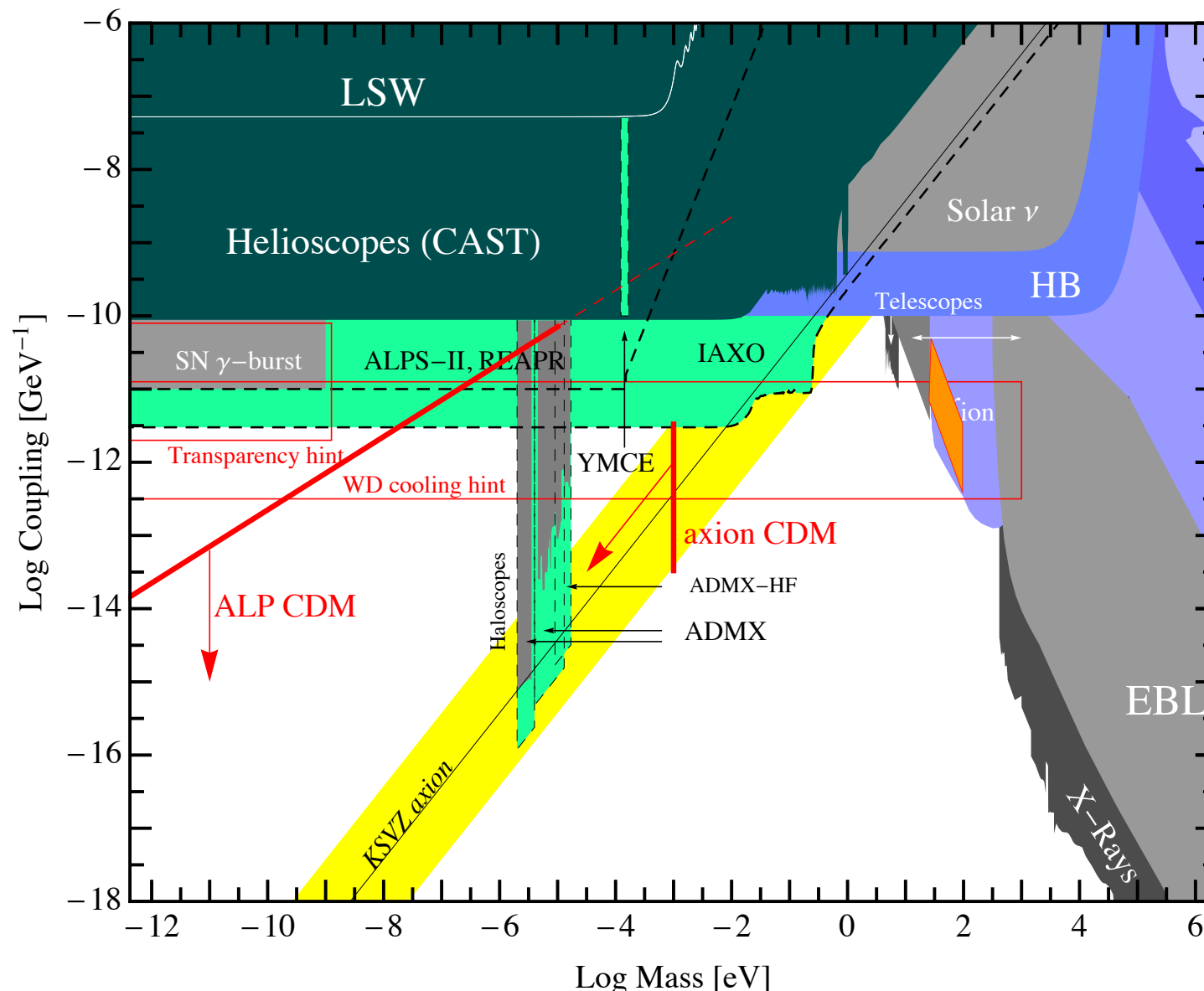
Experimental constraints ULA and axion-like particles (ALPs)



$$\mathcal{L} \propto g_{a\gamma\gamma} \vec{E} \cdot \vec{B}$$

Experimental constraints ULA and axion-like particles (ALPs)

Experimental desert: Gravitational constraints essential

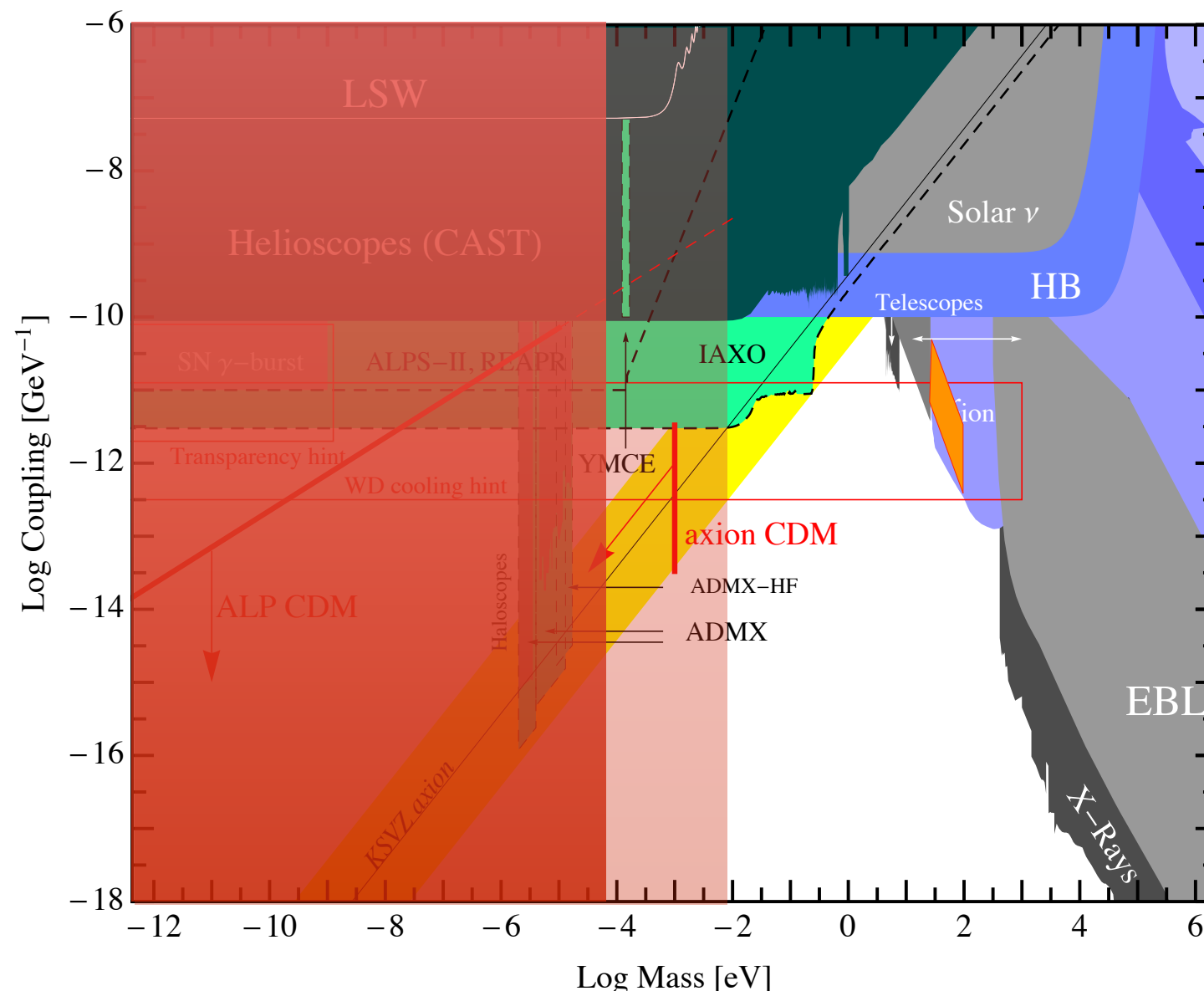


$$\mathcal{L} \propto g_{a\gamma\gamma} \vec{E} \cdot \vec{B}$$

From arXiv: 1205.2671

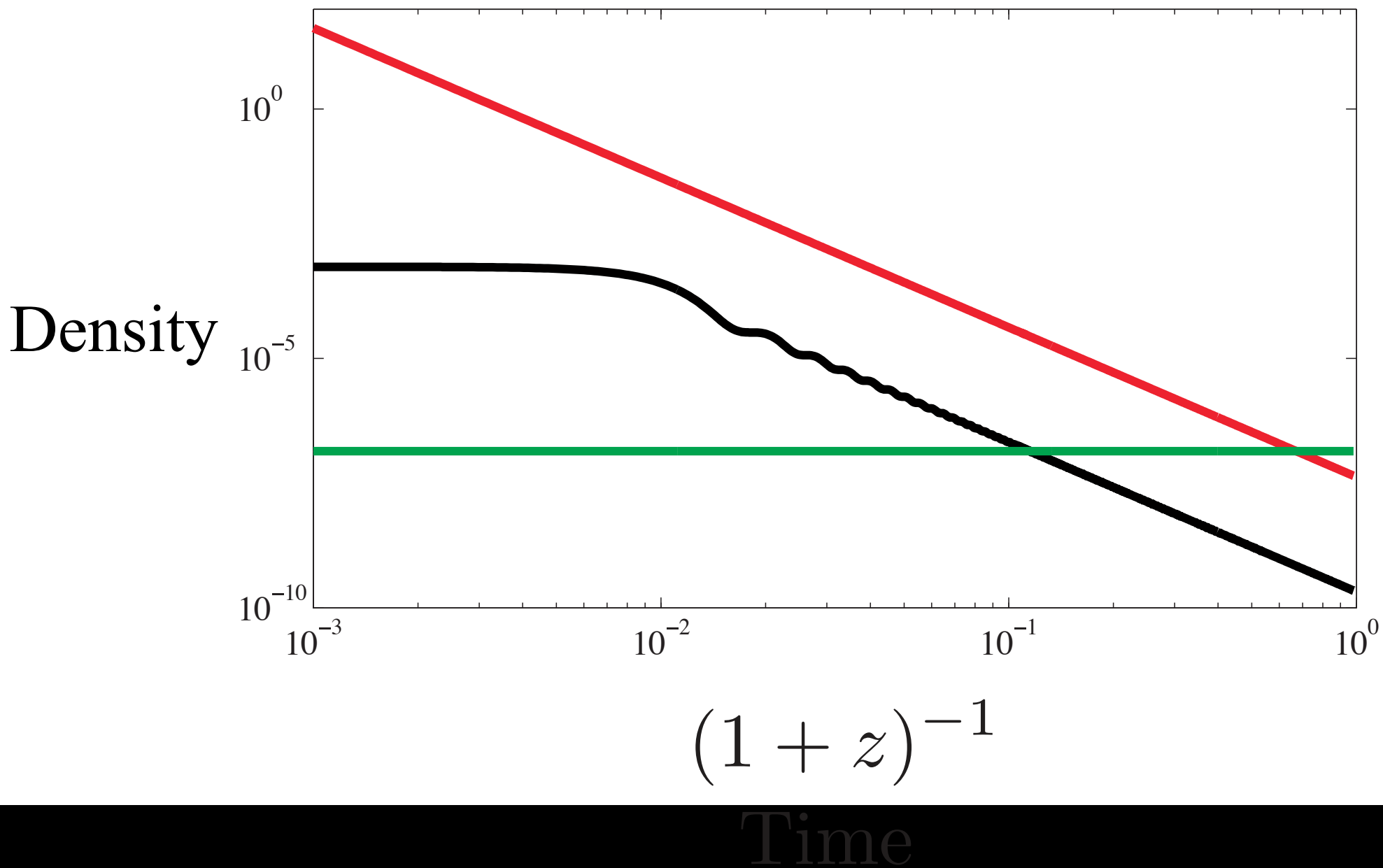
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Cosmological abundance limits

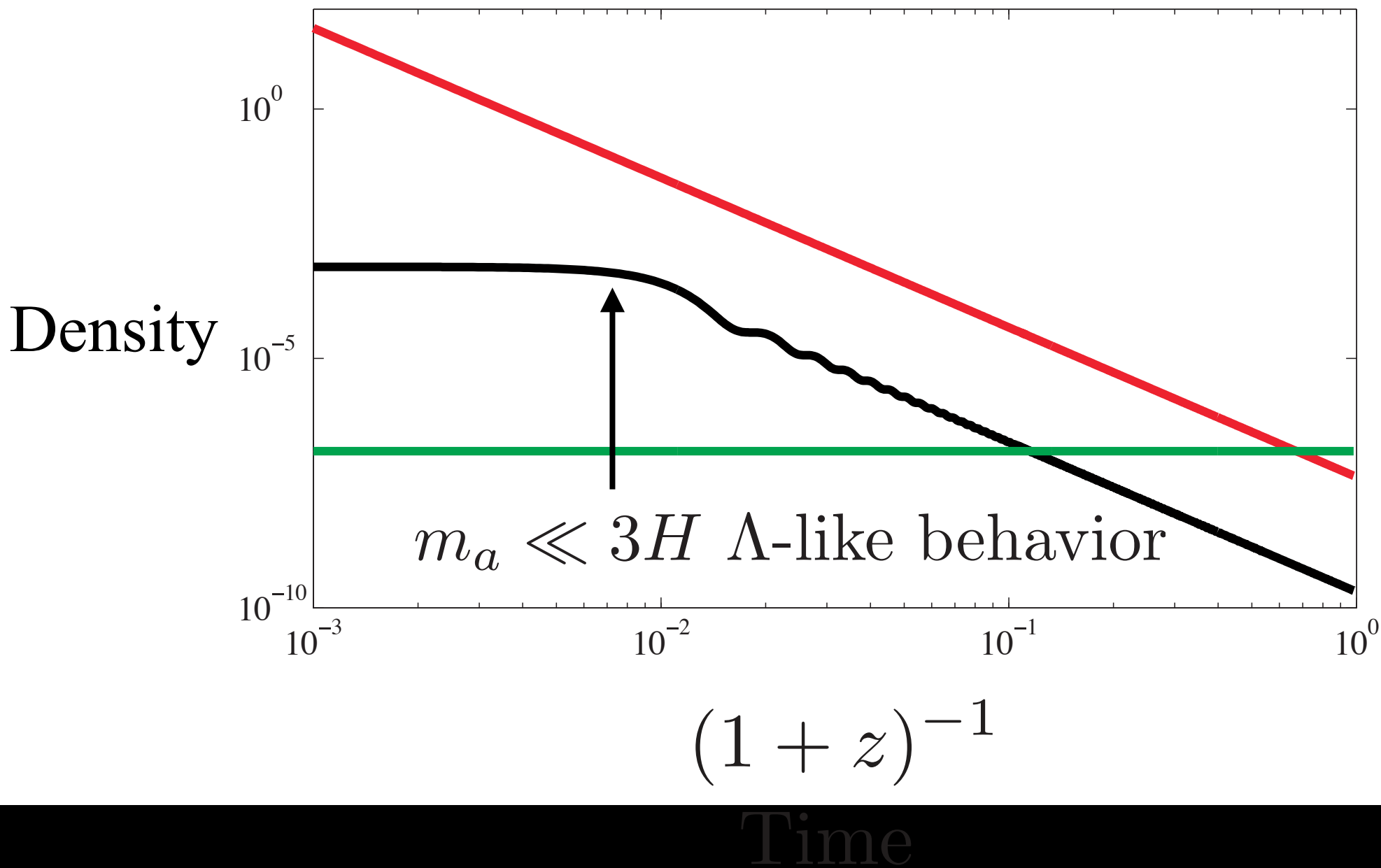


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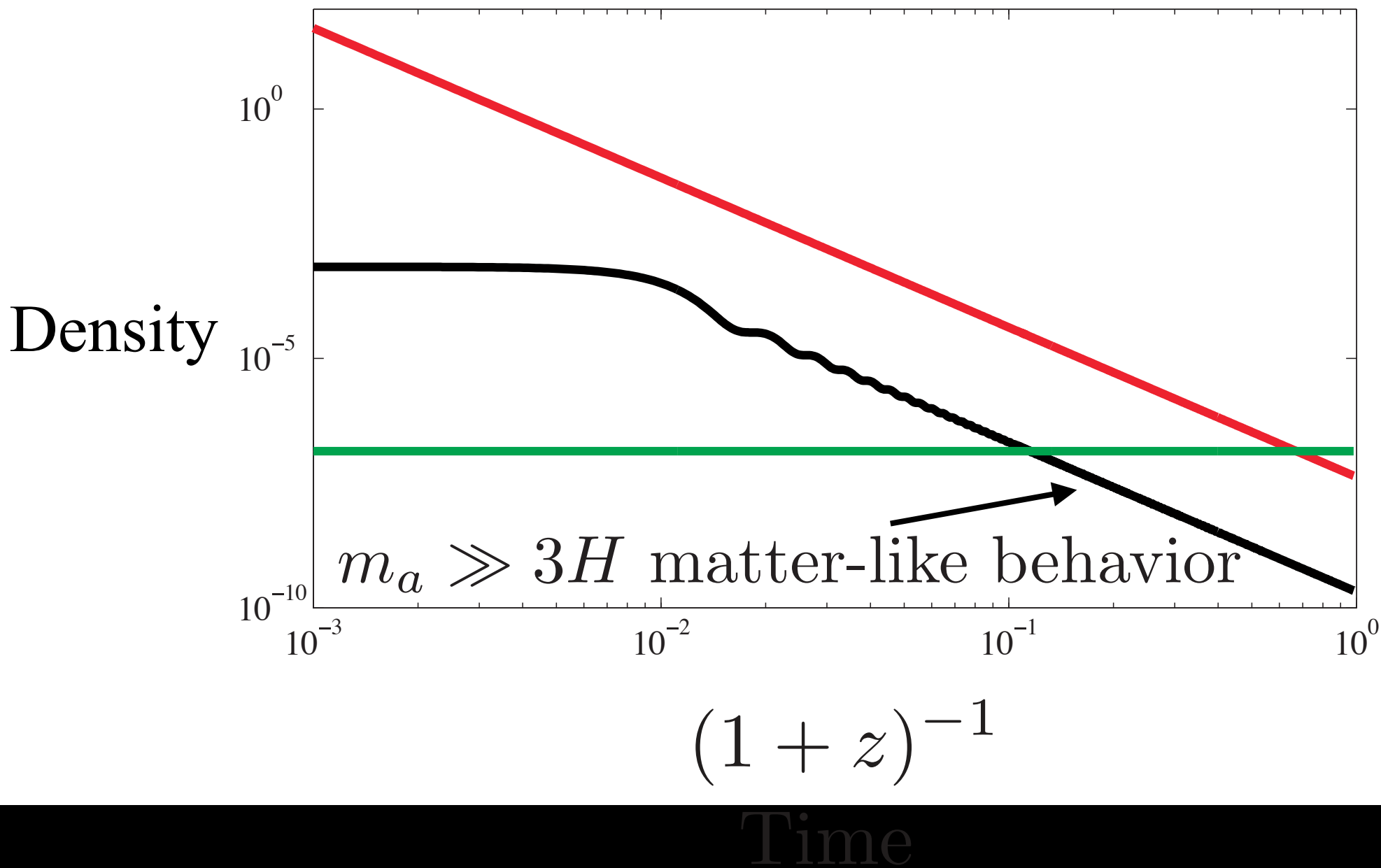
COSMOLOGY OF ULTRA-LIGHT AXIONS: DARK MATTER AND DARK ENERGY CANDIDATES



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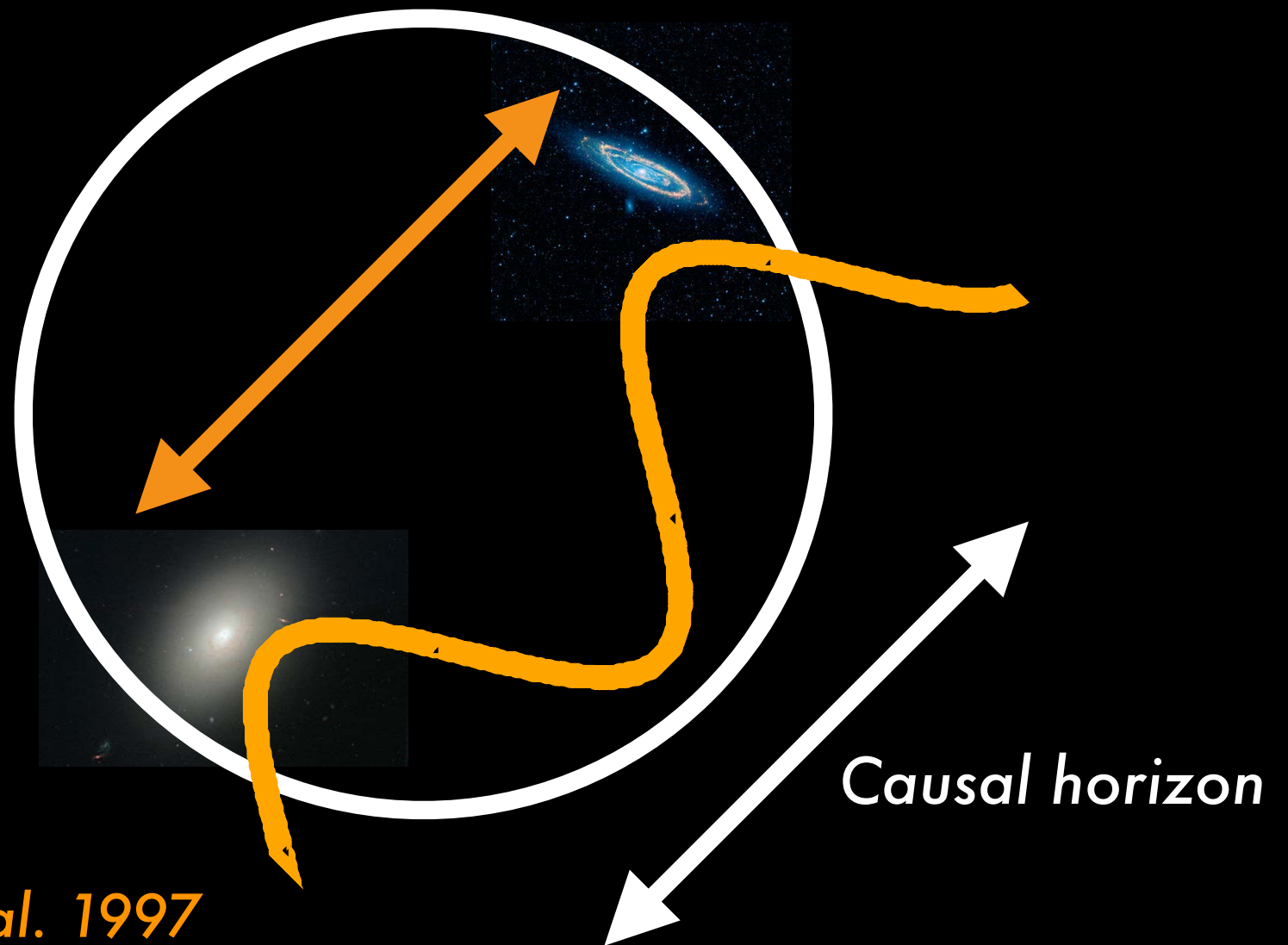
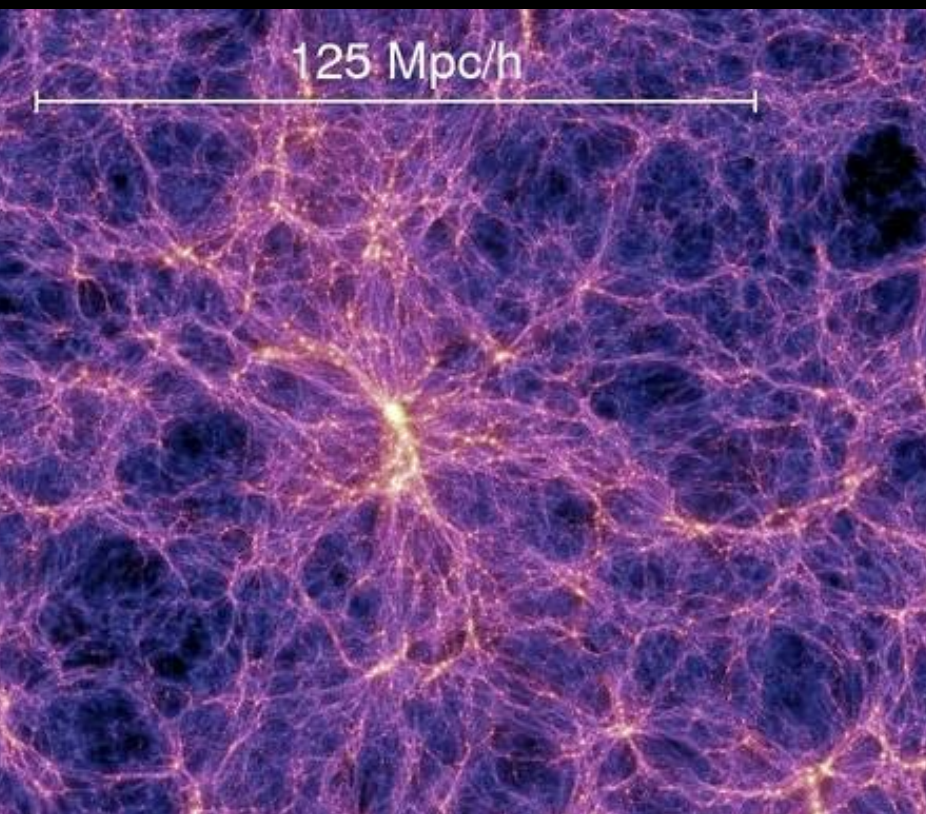


COSMOLOGY OF ULTRA-LIGHT AXIONS: DARK MATTER AND DARK ENERGY CANDIDATES



COSMOLOGY OF ULTRA-LIGHT AXIONS: DARK MATTER AND DARK ENERGY CANDIDATES

*Scale corresponding to
typical galaxy separation today*



Frieman et al 1995, Coble et al. 1997

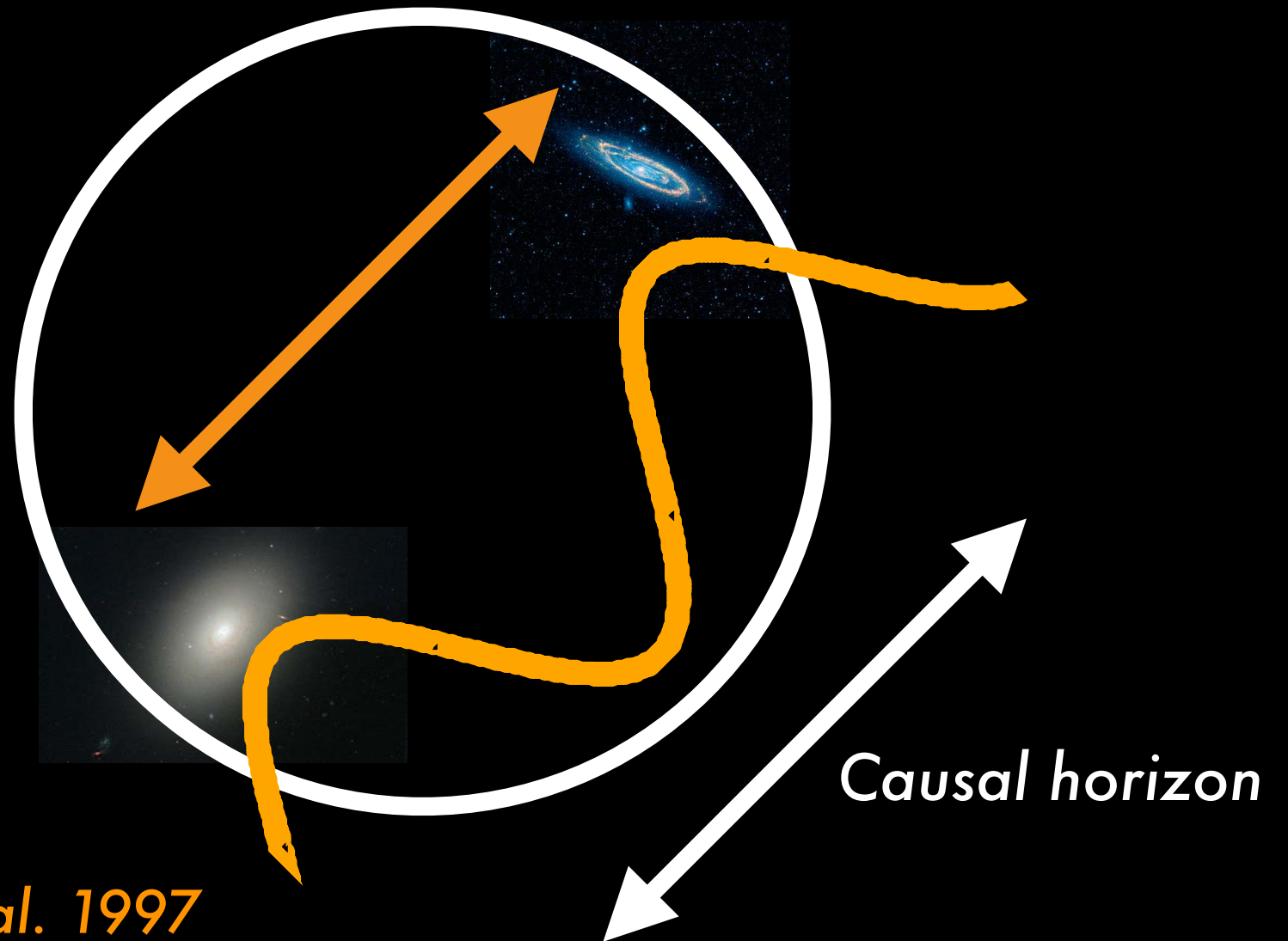
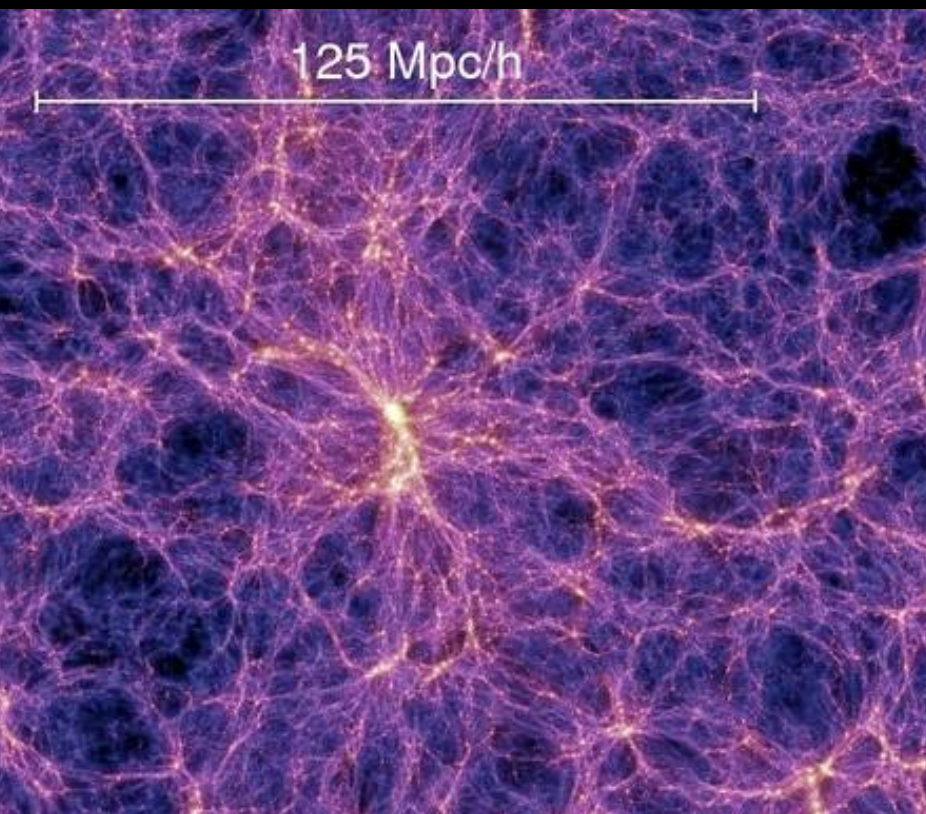
ULA as dark energy with specific $w(z)$

$$m_a \lesssim 10^{-27} \text{ eV}$$

ULA matter behavior starts too late for struct. formation

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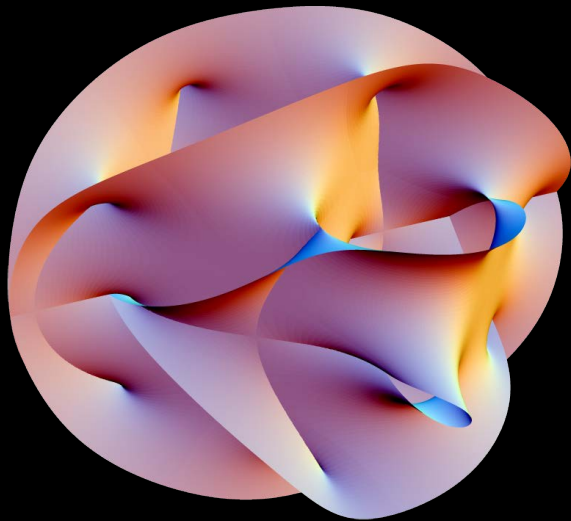
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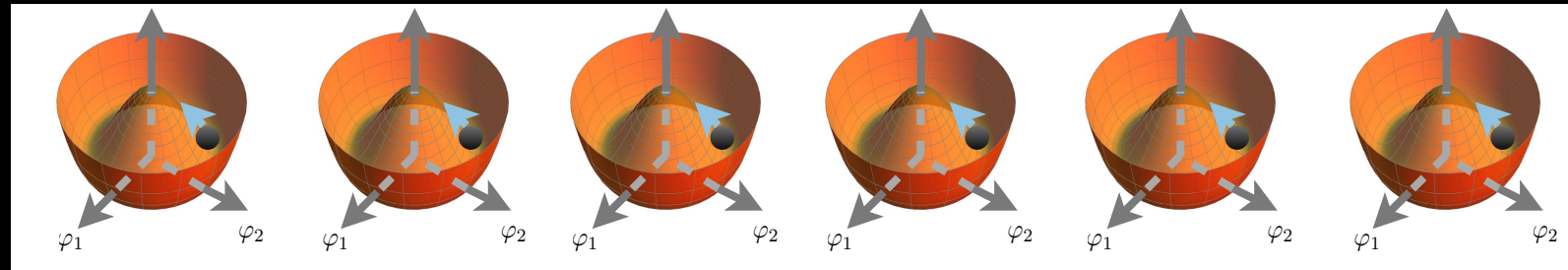
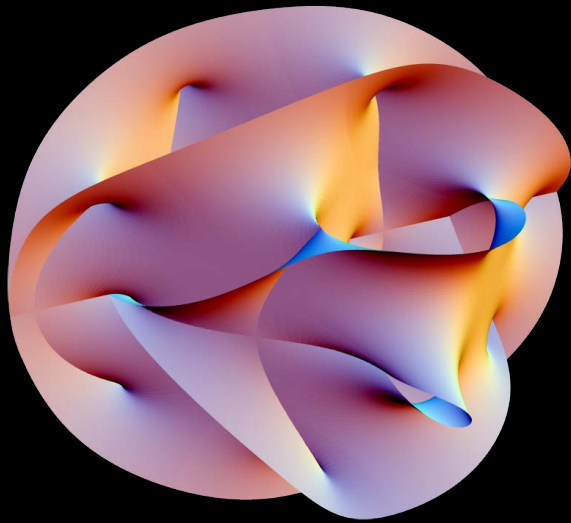
ULTRA-LIGHT AXIONS (ULAS) IN STRING THEORY

✧ In string theory, extra dimensions compactified: Calabi-Yau manifolds



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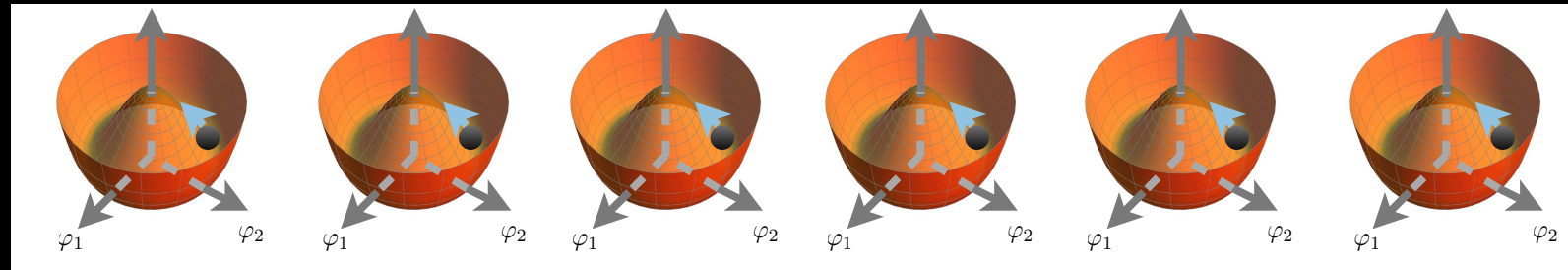
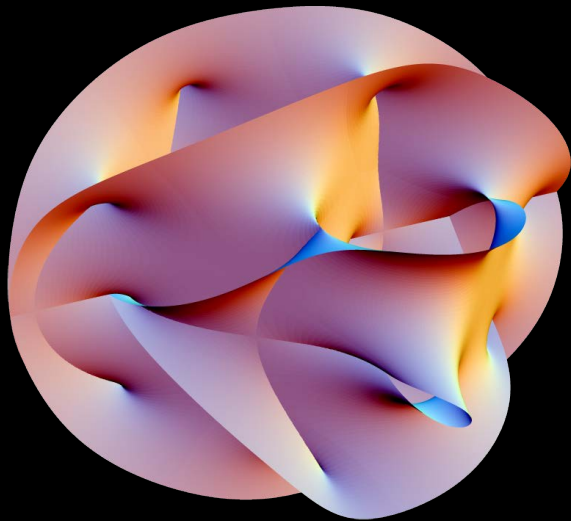


+....

*Hundreds of scalars
with approx shift symmetry*

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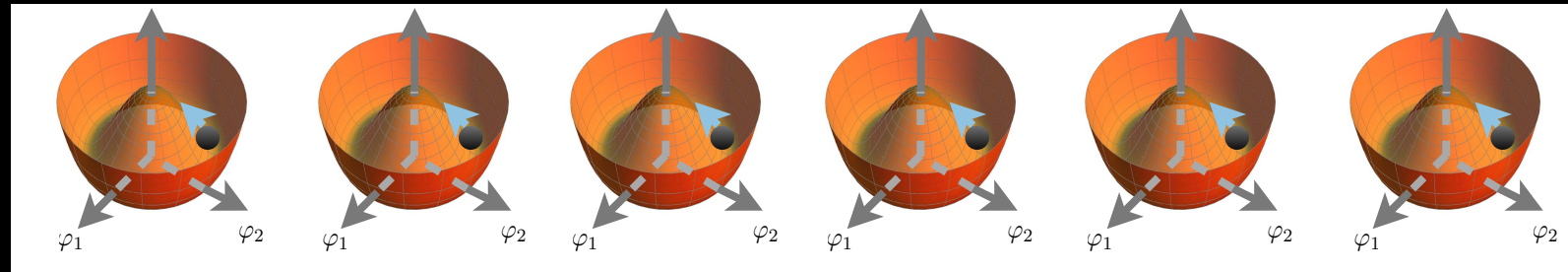
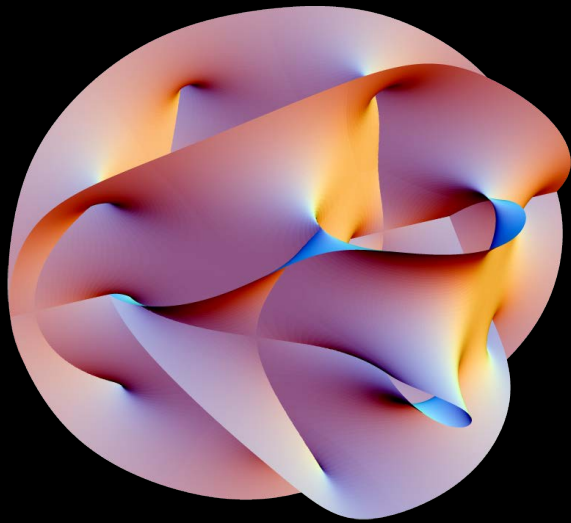
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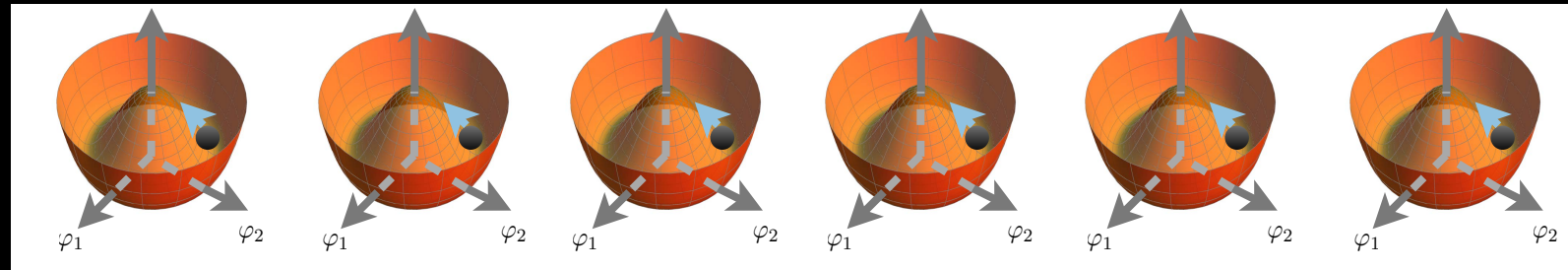
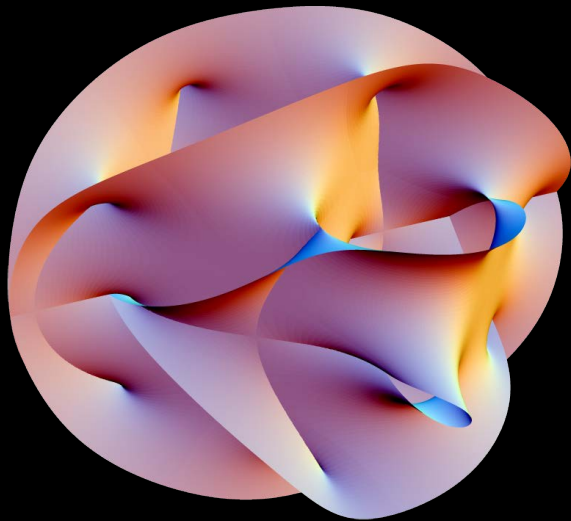
Many axions

- * Mass acquired non-perturbatively (instantons, D-Branes)

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

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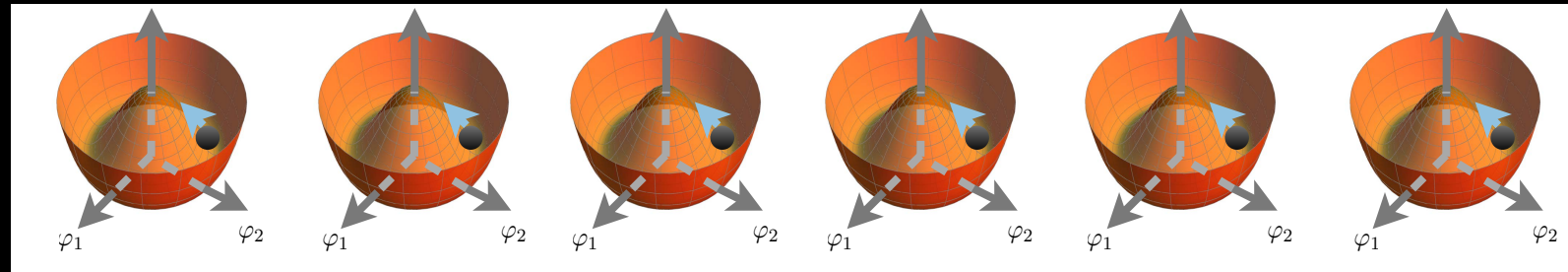
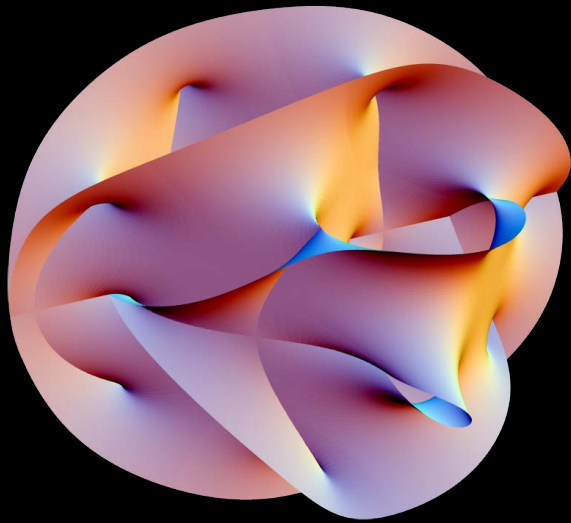
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**Scale of new
ultra-violet physics**

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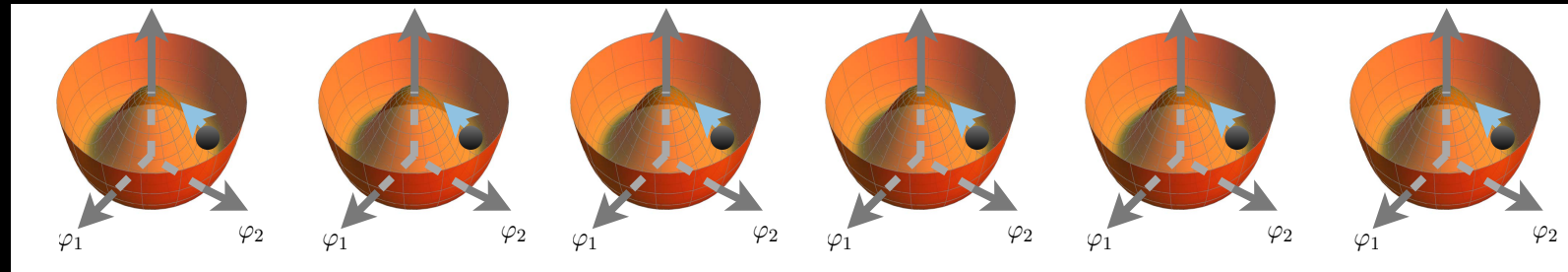
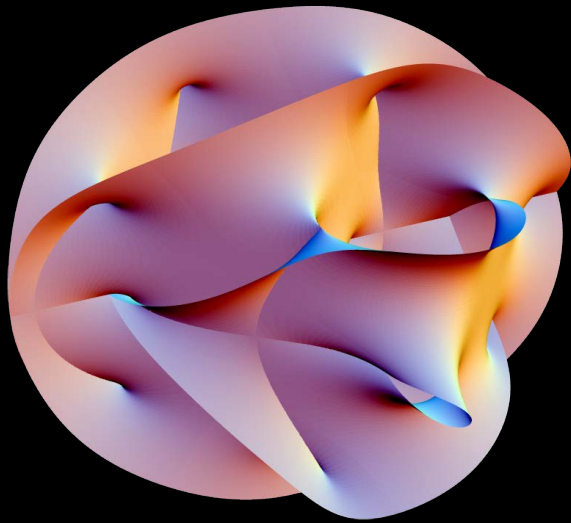
**Scale of extra dimensions
in Planck units**

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$



ULTRA-LIGHT AXIONS (ULAS) IN STRING THEORY

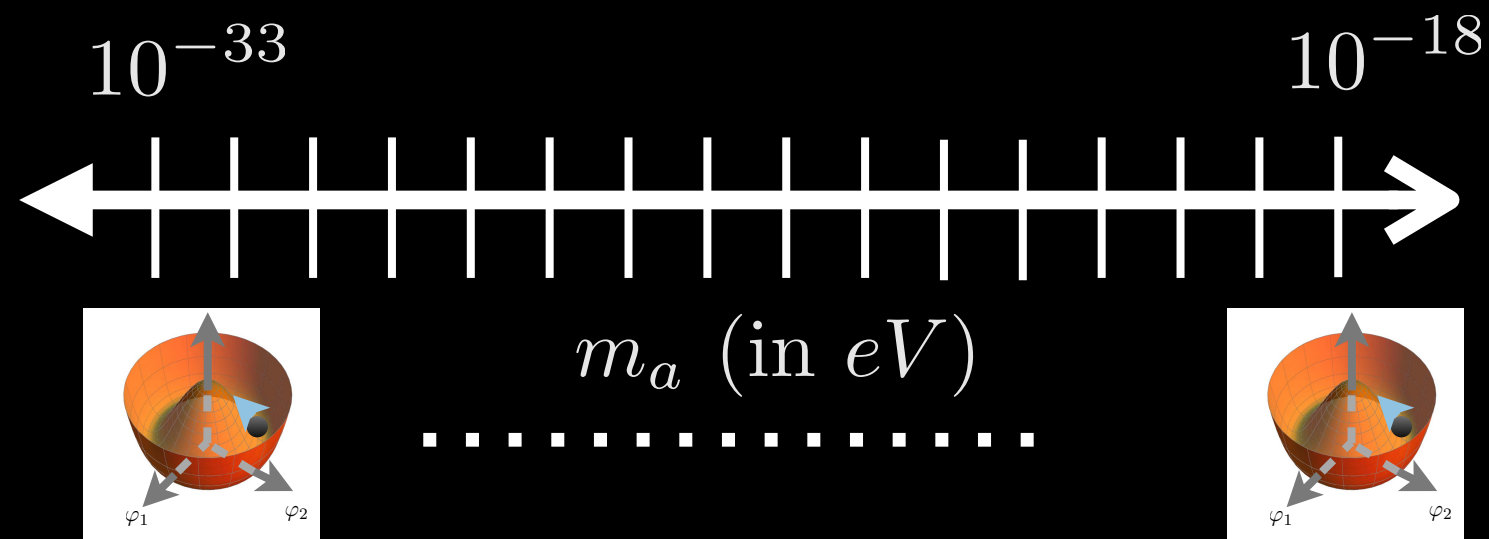
✧ In string theory, extra dimensions compactified: Calabi-Yau manifolds



+

Axiverse! Arvanitaki+ 2009

Witten and Svrcek (2006), Acharya et al. (2010), Cicoli (2012)



GROWTH OF ULA PERTURBATIONS

✱ Perturbed Klein-Gordon + Gravity

$$\ddot{\delta\phi} + 2\mathcal{H}\dot{\delta\phi} + (k^2 + m_a^2 a^2)\delta\phi = 4\dot{\Psi}\dot{\phi}_0 - \Psi a^2 m_a^2 \phi_0$$

✱ Axionic Jeans Scale is macroscopic [in contrast to QCD axion]:

$$\lambda_J = 2.4h^{-1/2} \left(\frac{m}{10^{-25} \text{ eV}} \right)^{-1/2} \text{ Mpc}$$

✱ Computing observables is expensive for $m \gg 3\mathcal{H}$:

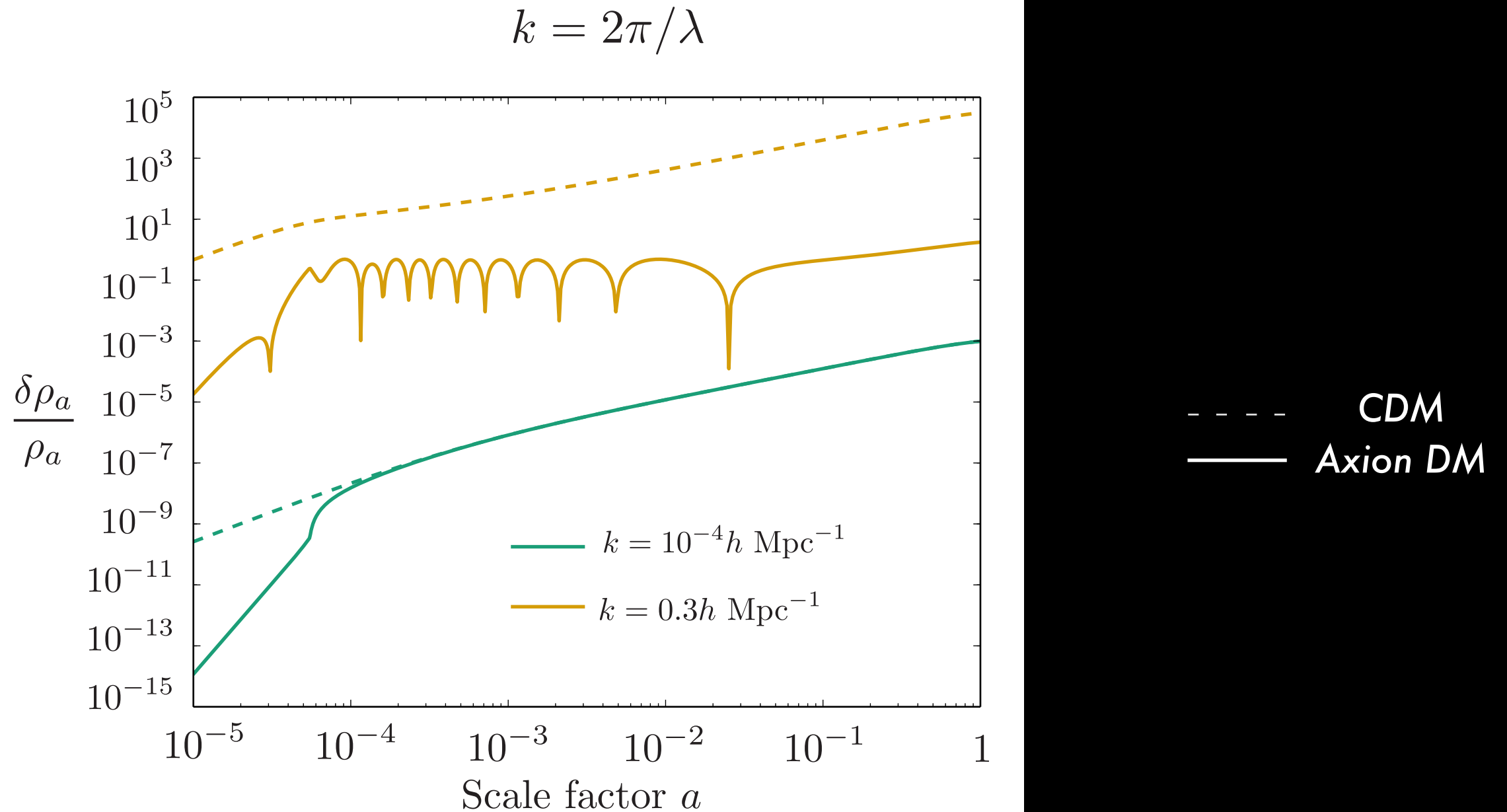
✱ Coherent oscillation time scale $\Delta\eta \sim (ma)^{-1} \ll \Delta\eta_{\text{CAMB}}$

✱ WKB approximation

$$\delta\phi = A_c \Delta_c(k, \eta) \cos(m\eta) + A_s \Delta(k, \eta) \sin(m\eta)$$

$$c_a^2 = \frac{\delta P}{\delta \rho} = \frac{k^2 / (4m^2 a^2)}{1 + k^2 / (4m^2 a^2)}$$

GROWTH OF **ULA** PERTURBATIONS

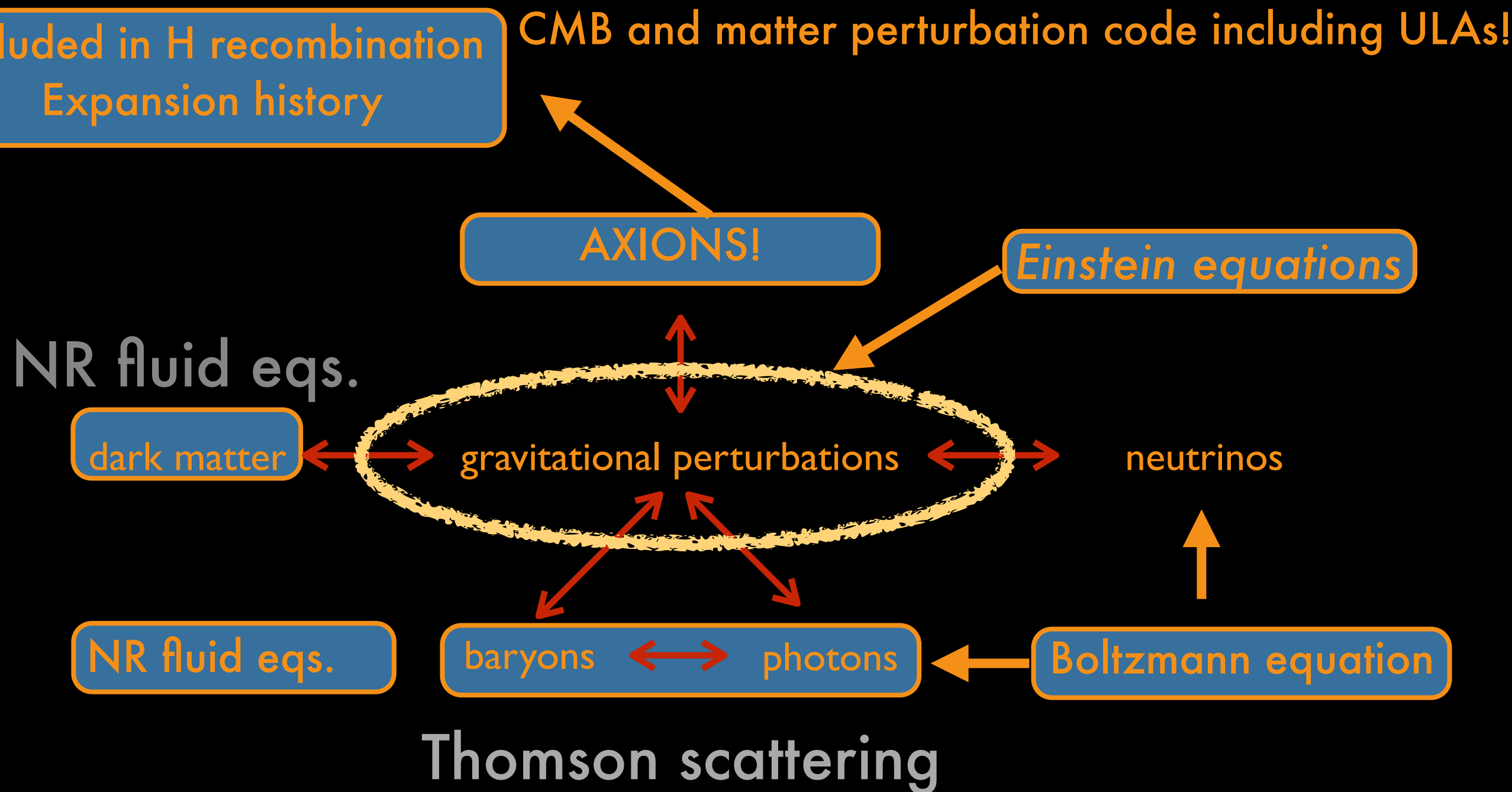


* Modes with $k \gg k_J \sim \sqrt{m\mathcal{H}}$ oscillate instead of growing

AXIONCAMB

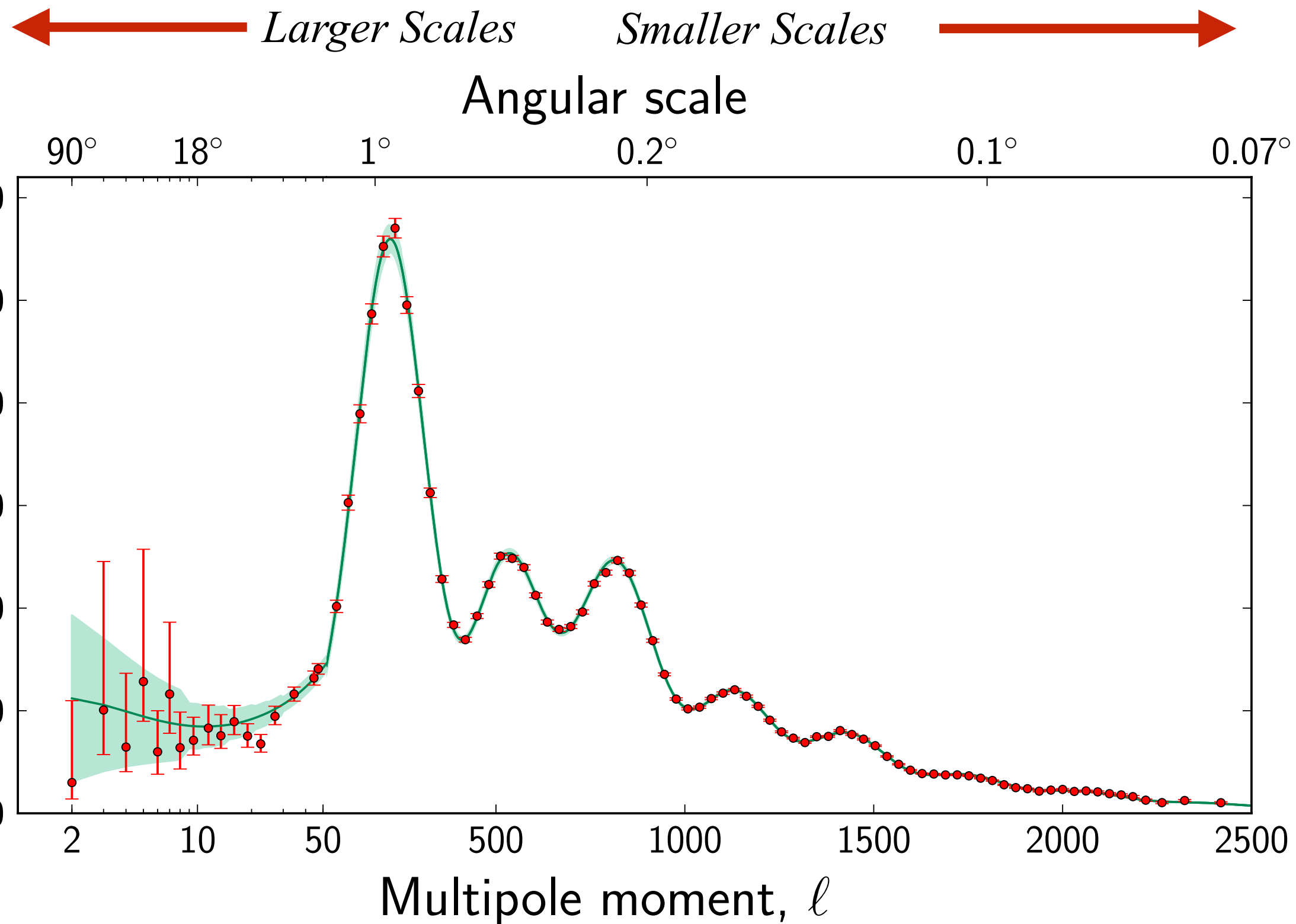
Code by Grin et al. 2013, based on CAMB (A. Lewis)

<http://github.com/dgrin1/axionCAMB>

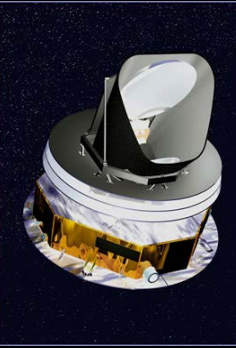
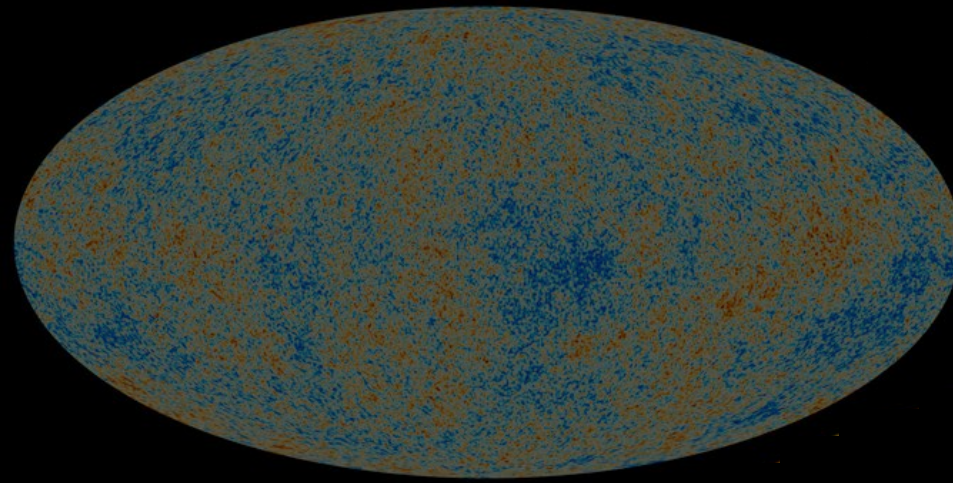


ULA of any mass is self-consistently followed from DE to DM regime

AXIONCAMB



DATA + ANALYSIS



- * Planck 2013 temperature anisotropy power spectra (+SPT+ACT)

 - * Cosmic variance limited to $\ell \sim 1500$

- * WiggleZ galaxy survey (linear scales only $k \lesssim 0.2h \text{ Mpc}^{-1}$)

 - * 240,000 emission line galaxies at $z < 1$

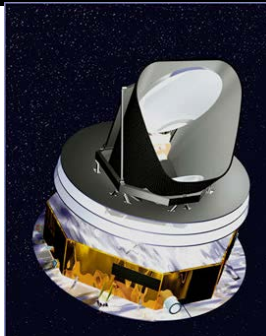
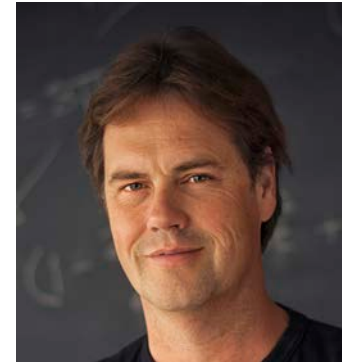
 - * 3.9 m Anglo-Australian Telescope (AAT)

- * Nested sampling, MCMC, vary $m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$



CONSTRAINTS

Comparison with data



R.Hlozek, DG, D.J. E. Marsh, P.Ferreira

arXiv: 1708.05681, submitted to Phys. Rev. D

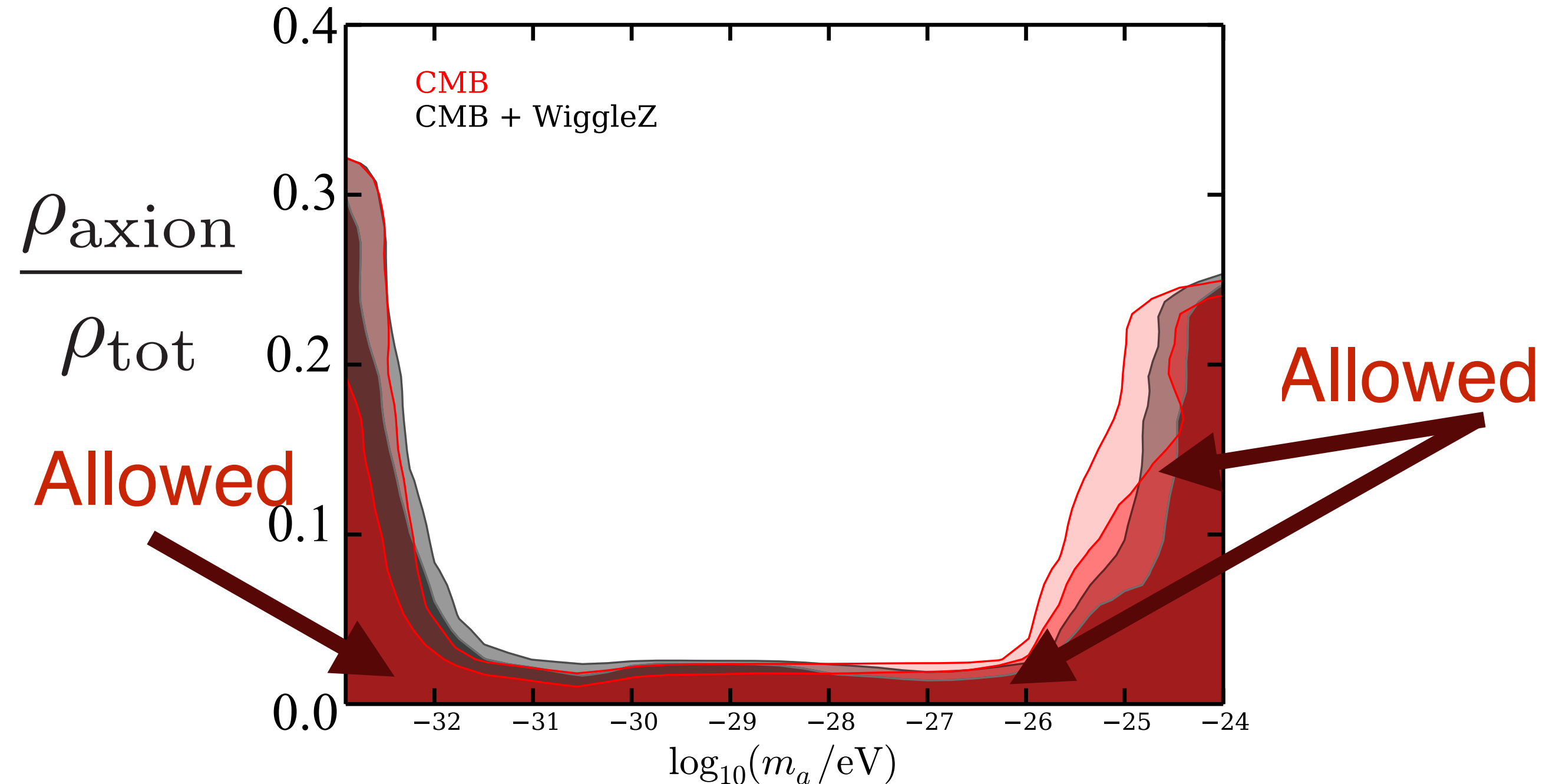
arXiv: 1607.08208, Phys. Rev. D 95, 123511 (2017).

arXiv:1410.2896, Phys. Rev. D 91, 103512 (2015)

arXiv:1403.4216, Phys. Rev. Lett. 113, 011801 (2014)

arXiv:1303.3008, Phys. Rev. D 87, 121701(R) (2013)

CONSTRAINTS

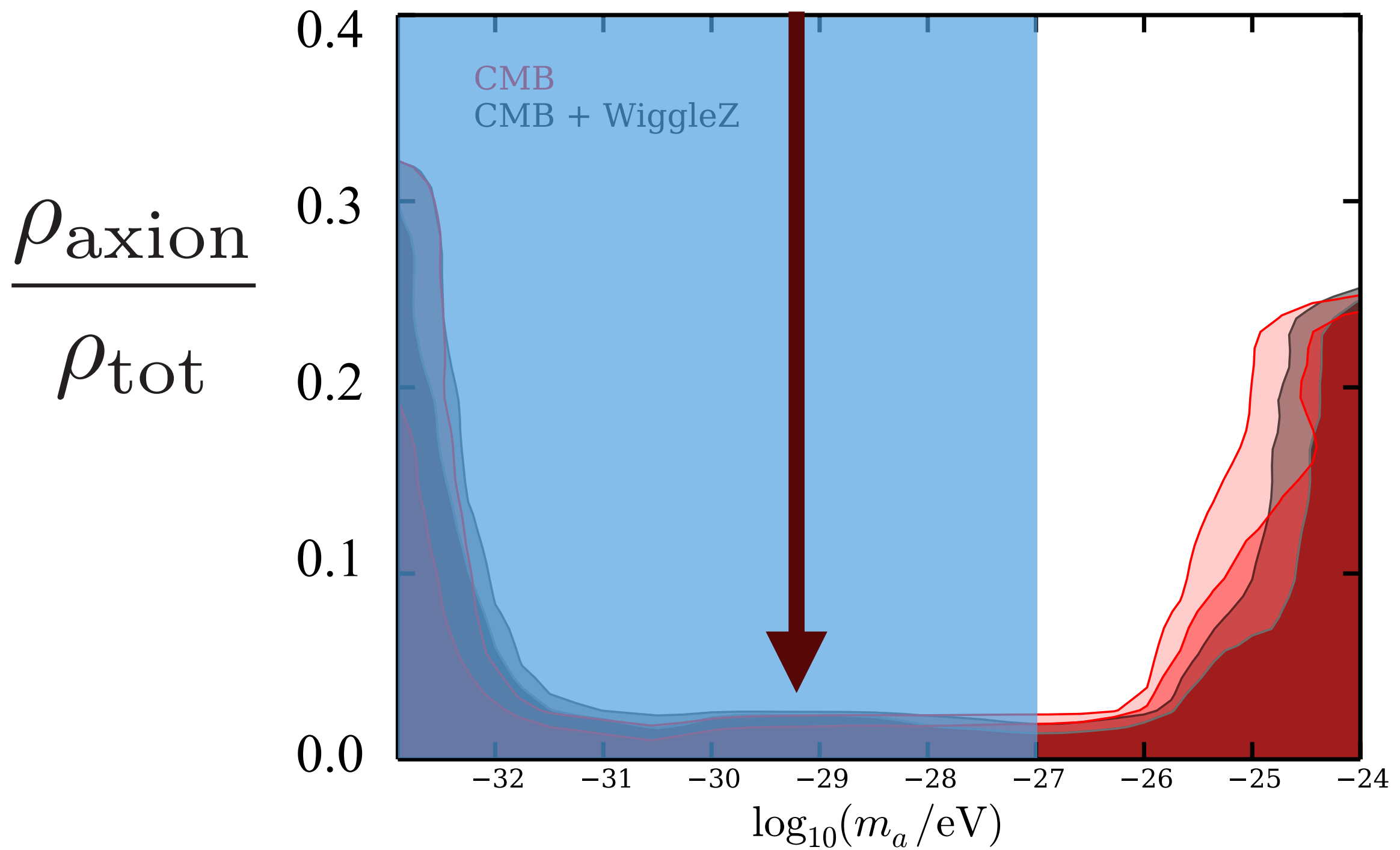


Thanks to AXIONCAMB and Planck

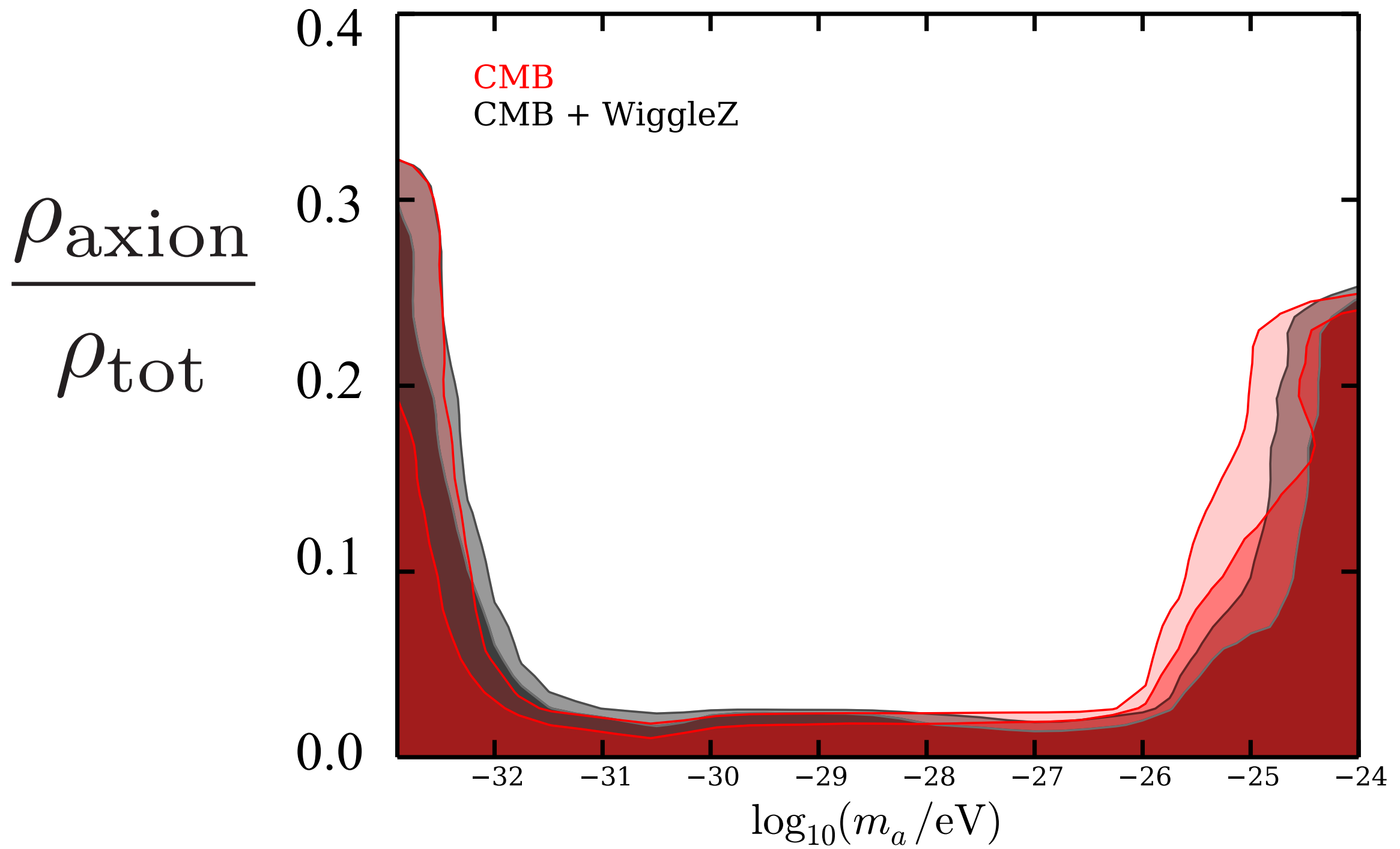
✳ ULAs are viable DM/DE candidates in linear theory outside ``belly''

CONSTRAINTS

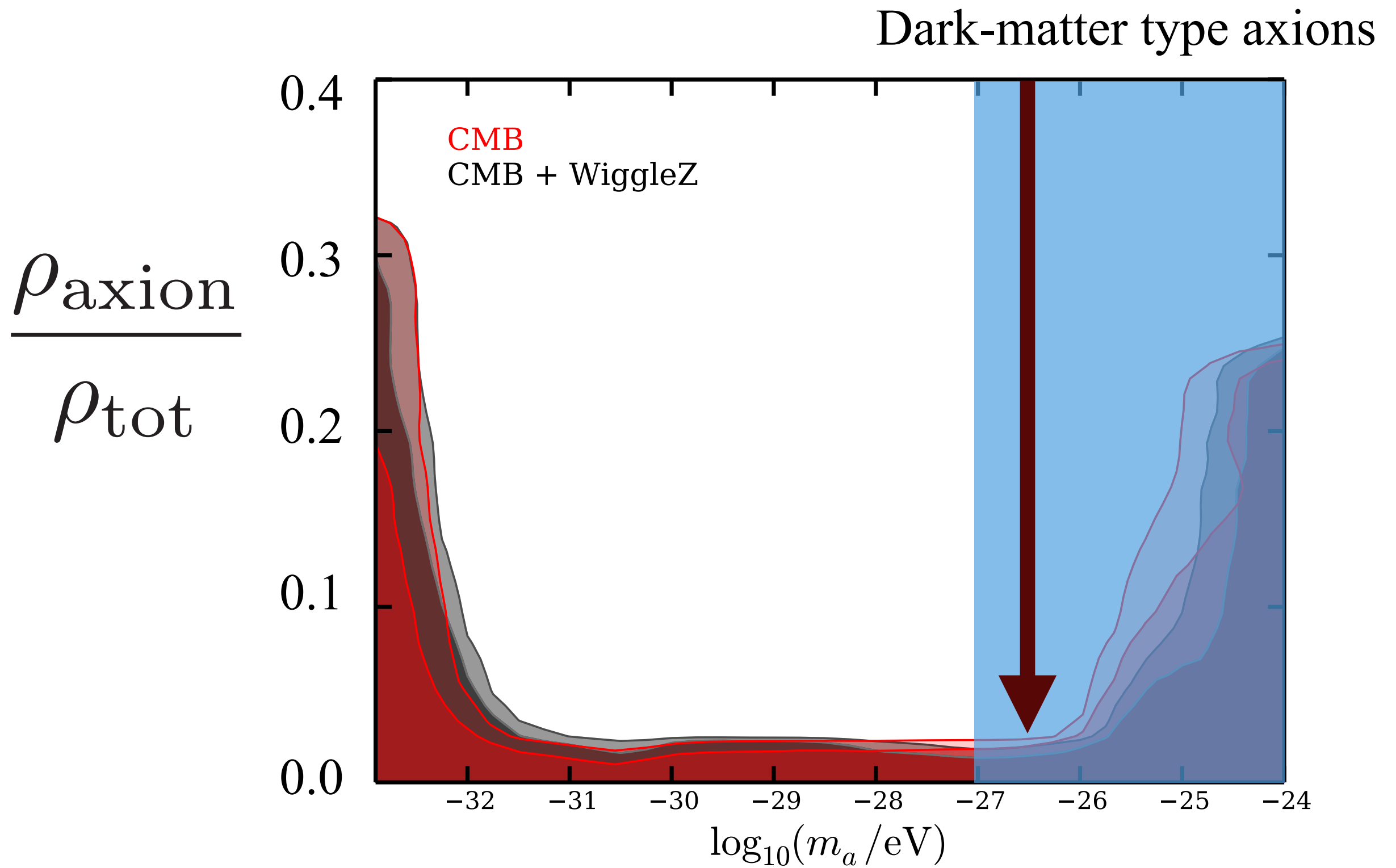
Dark-energy type axions



CONSTRAINTS



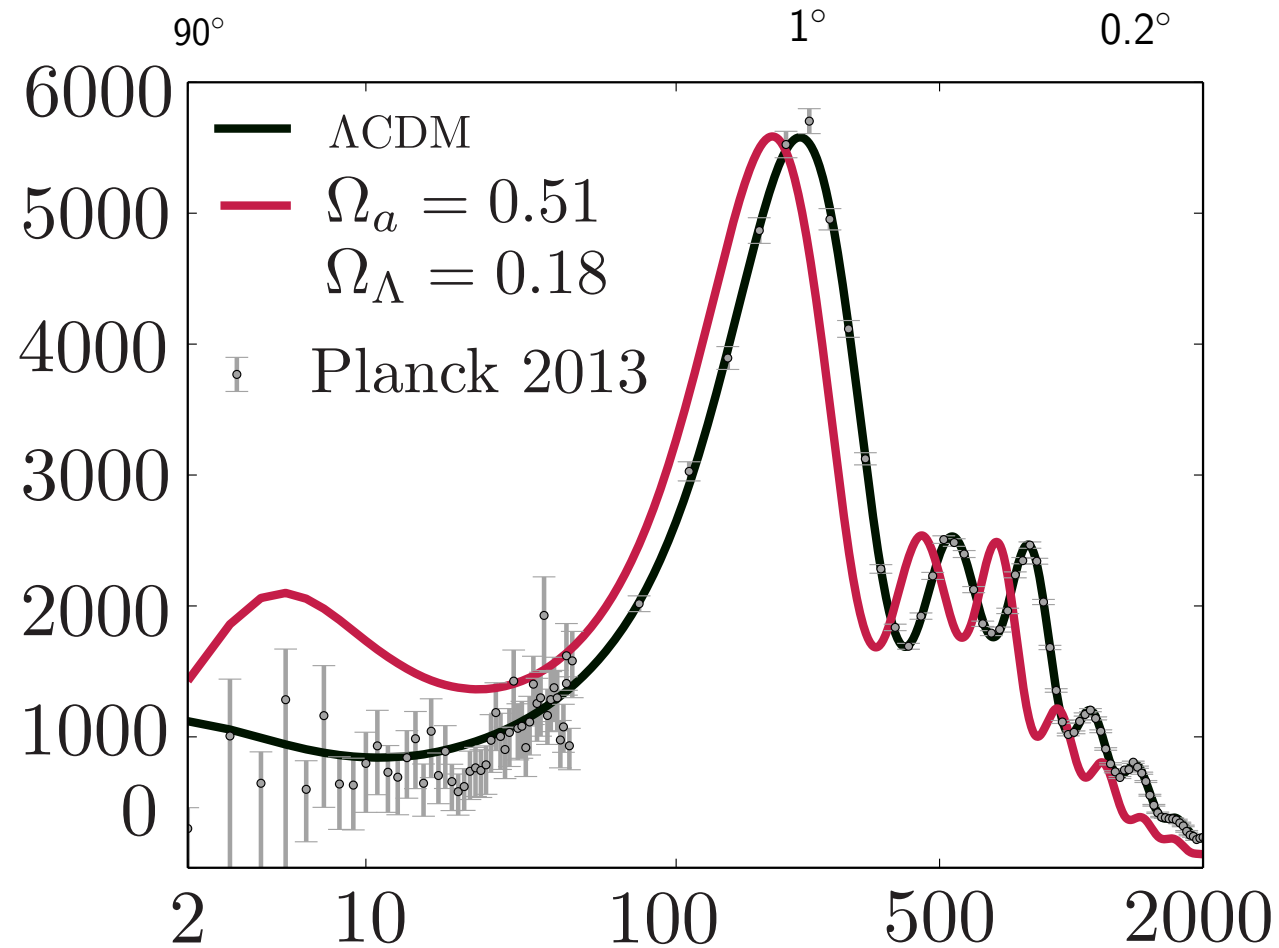
CONSTRAINTS



CONSTRAINTS

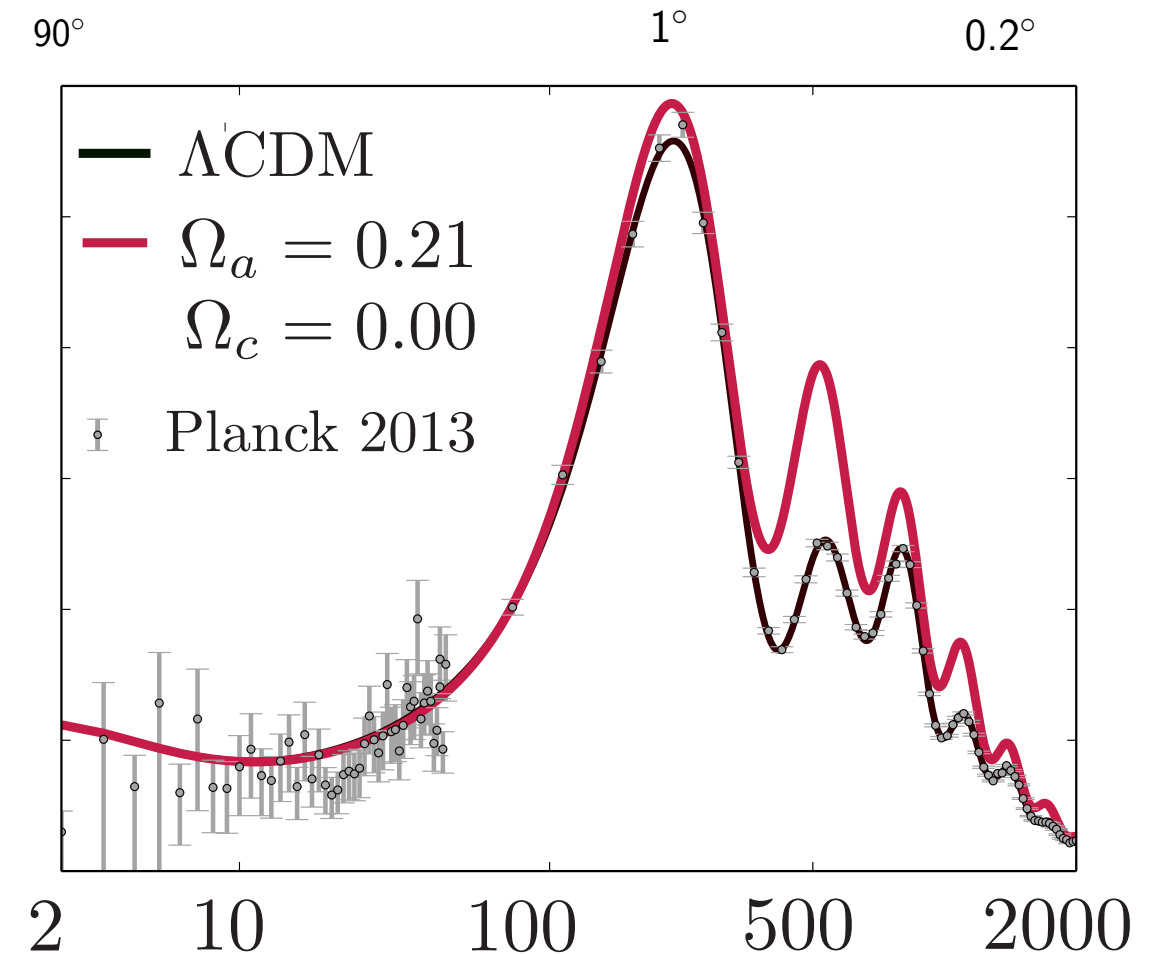
$$m_a = 10^{-32} \text{ eV}$$

Angular scale



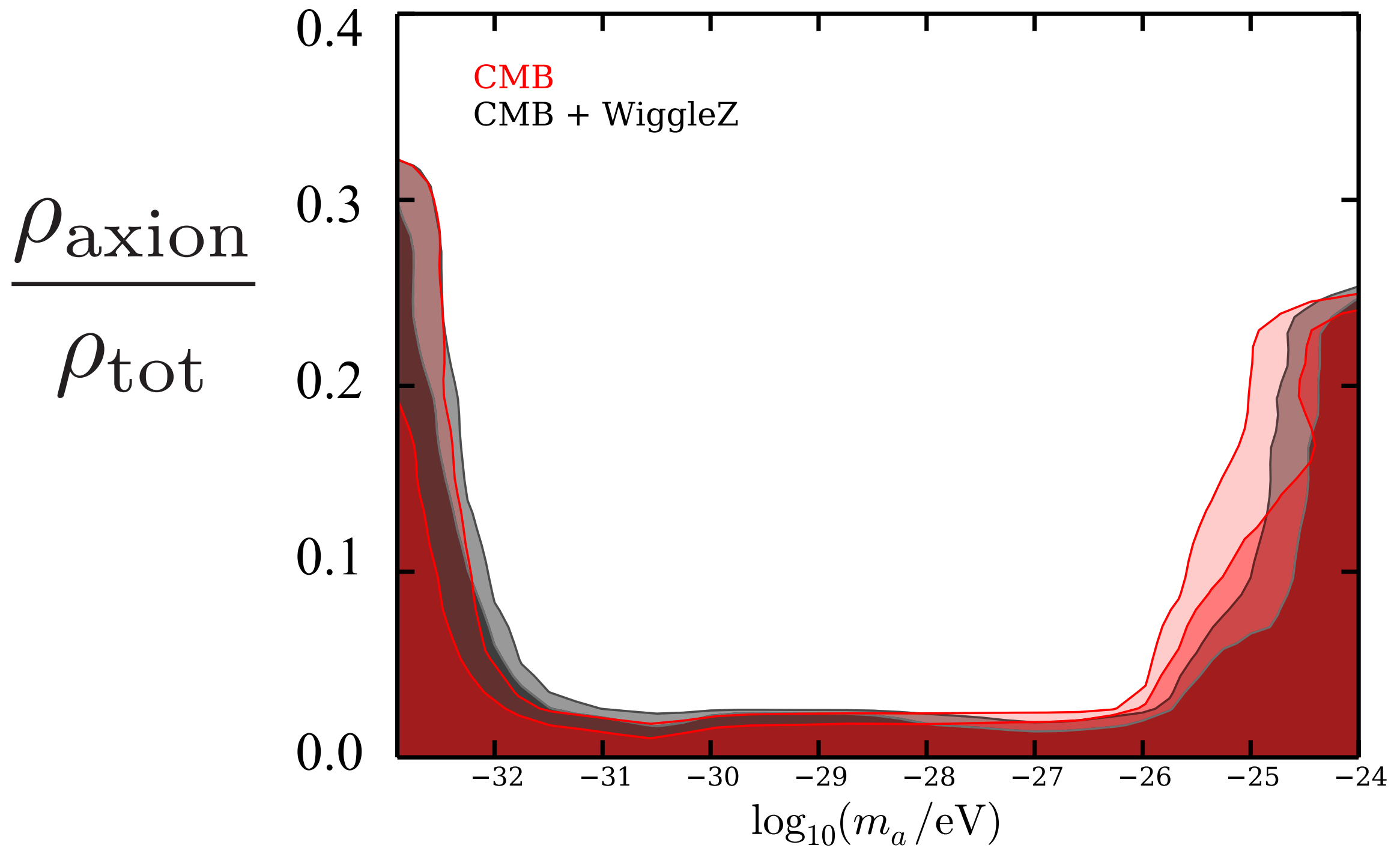
$$m_a = 10^{-27} \text{ eV}$$

Angular scale

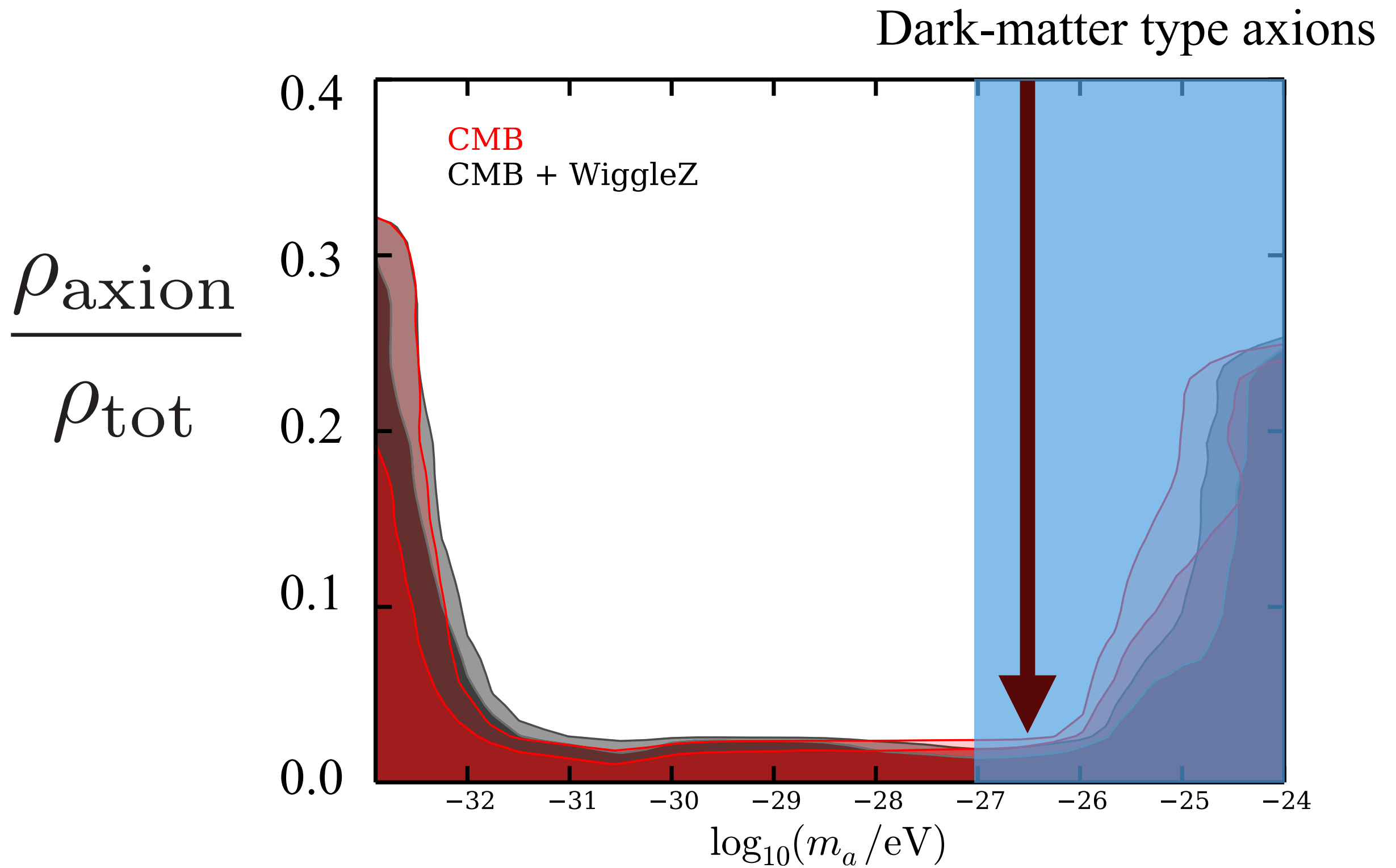


Dramatic changes to observables can result

CONSTRAINTS



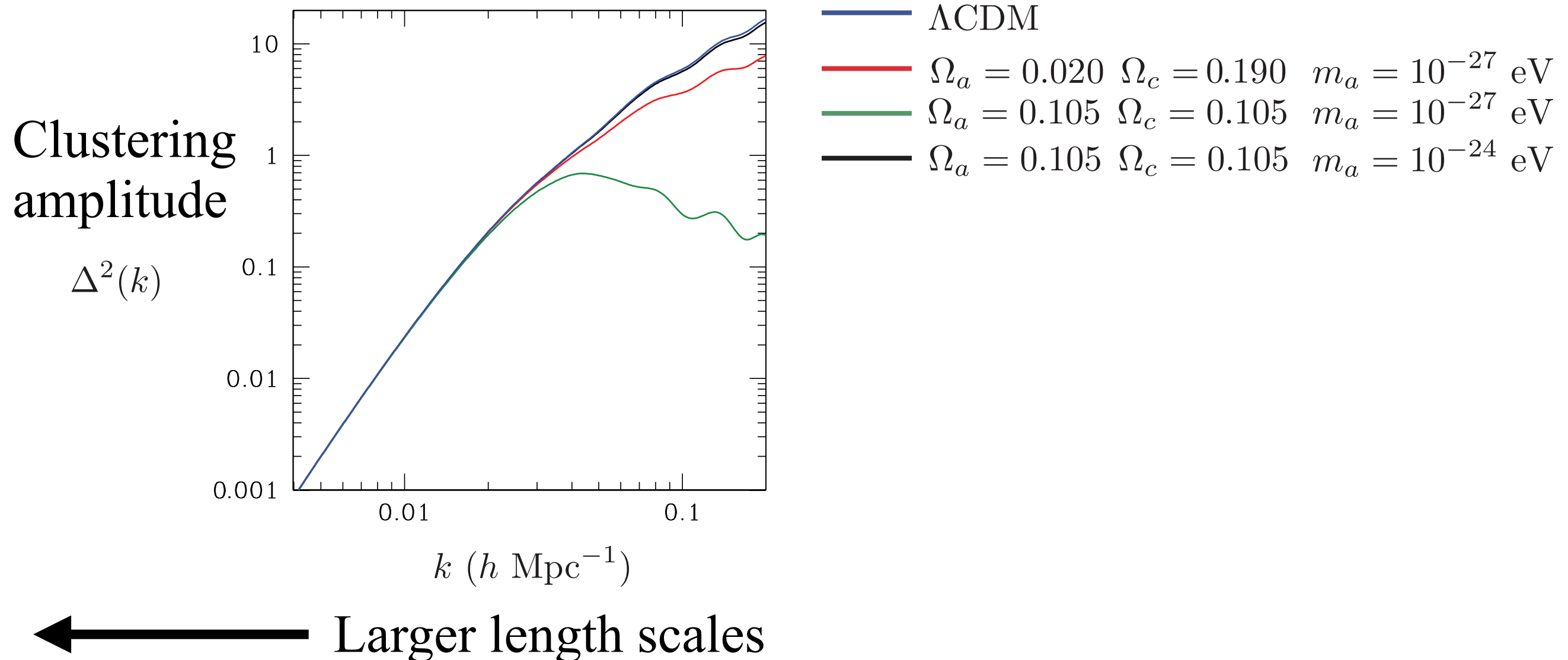
CONSTRAINTS



Matter clustering for ULA (in dark matter regime)

✧ Galaxies trace the matter in the universe

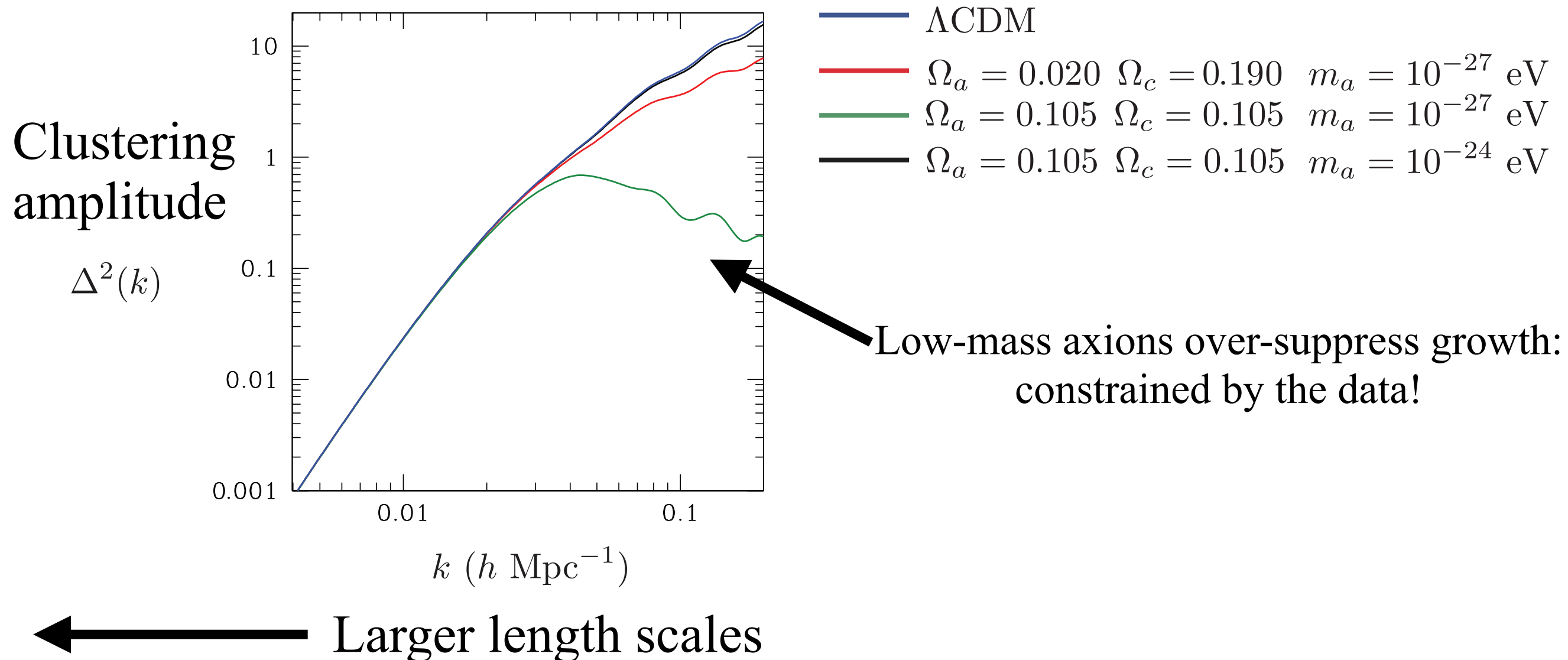
Matter clustering for ULA (in dark matter regime)



✳ DM structure growth severely suppressed on scales $k > k_J \simeq \sqrt{m\mathcal{H}}$

✳ Suppression grows $\propto -\frac{\Omega_a}{\Omega_a + \Omega_c}$

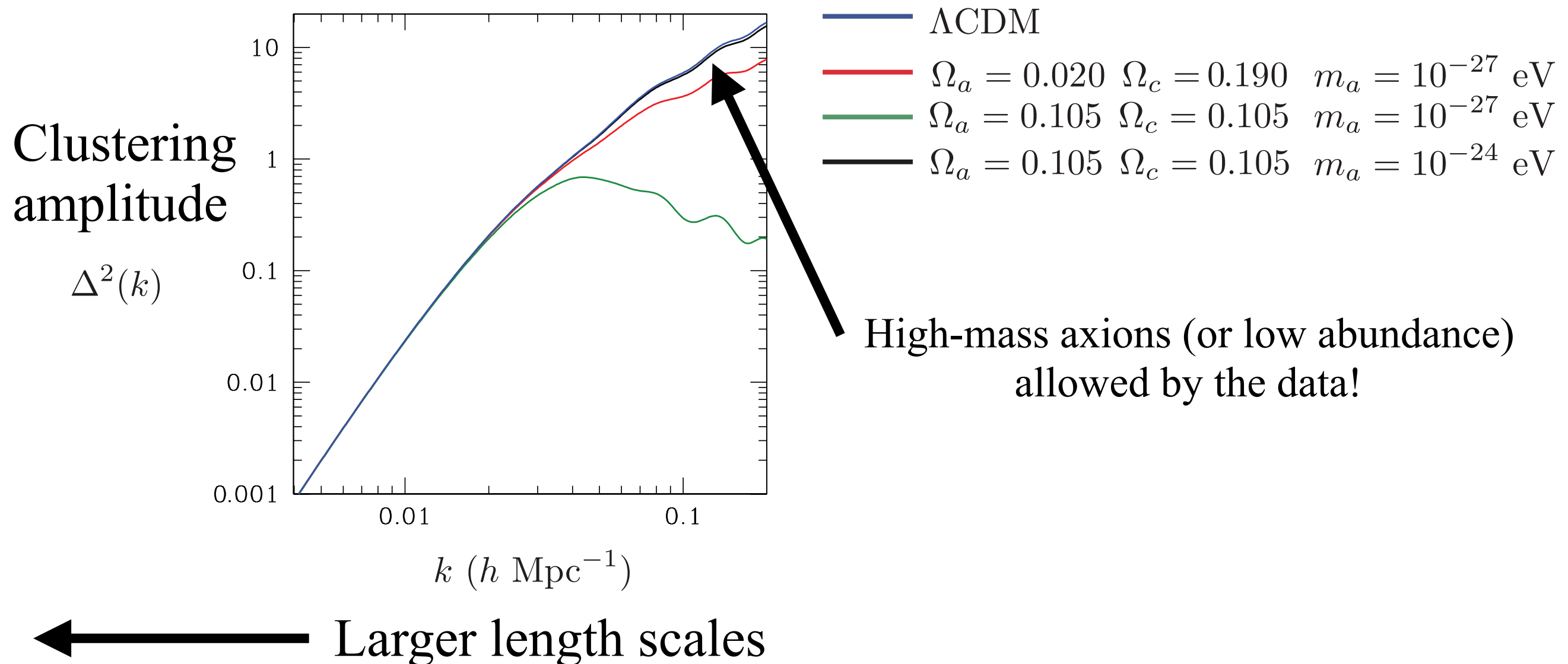
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*Suppression grows $\propto -\frac{\Omega_a}{\Omega_a + \Omega_c}$

Matter clustering for ULA (in dark matter regime)

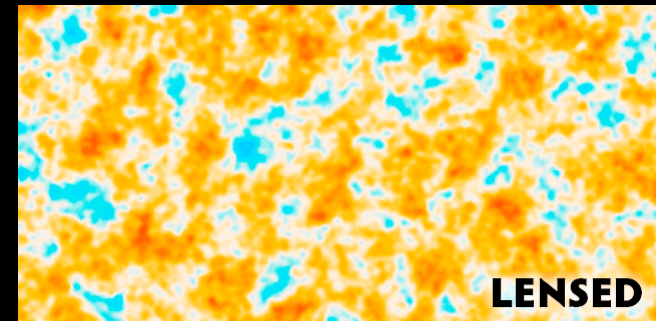
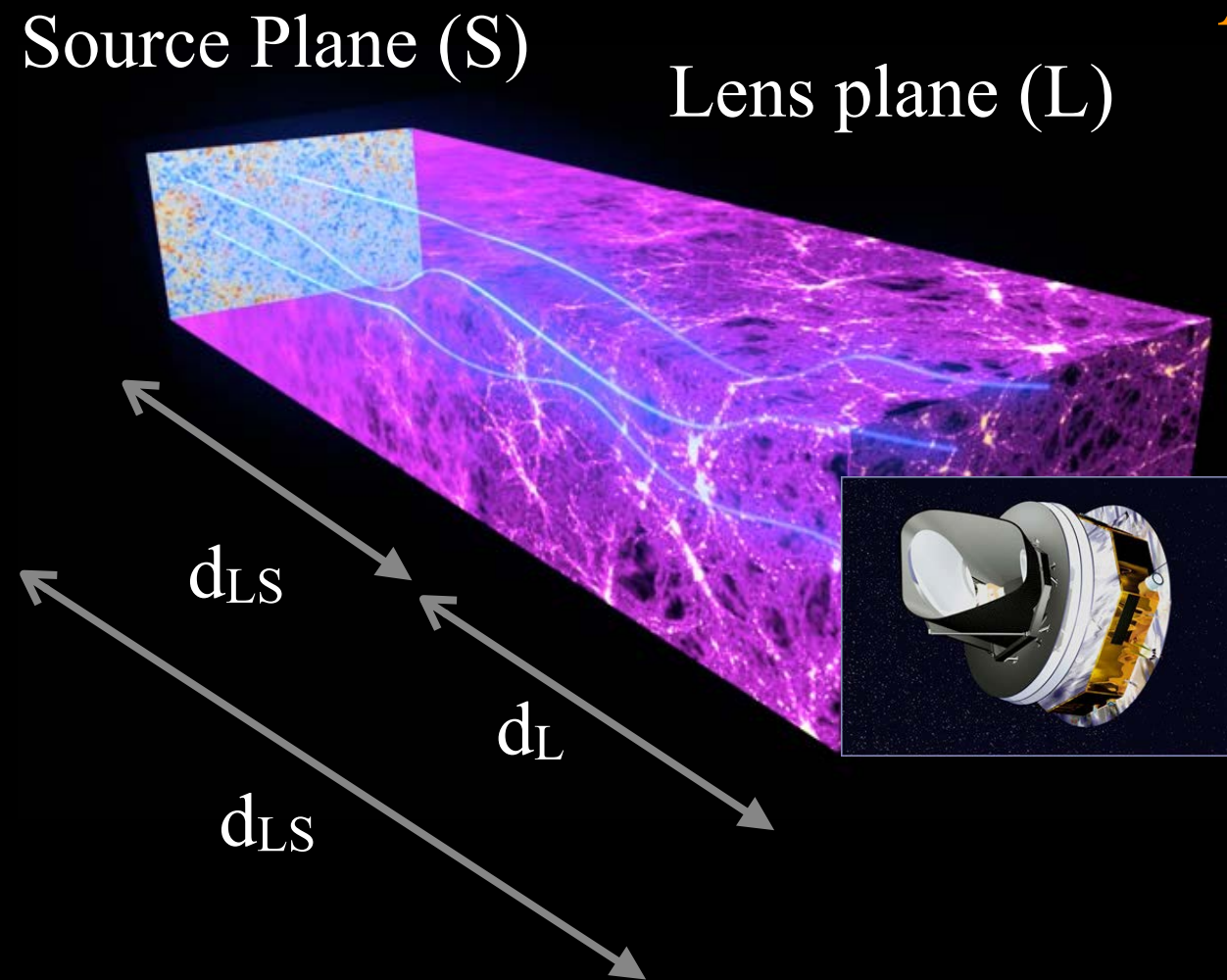


*DM structure growth severely suppressed on scales $k > k_J \simeq \sqrt{m\mathcal{H}}$

*Suppression grows $\propto -\frac{\Omega_a}{\Omega_a + \Omega_c}$

CMB LENSING

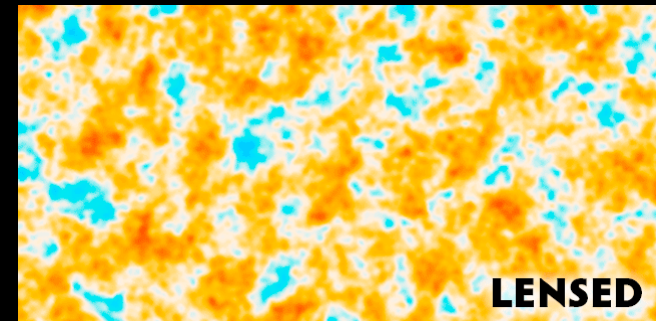
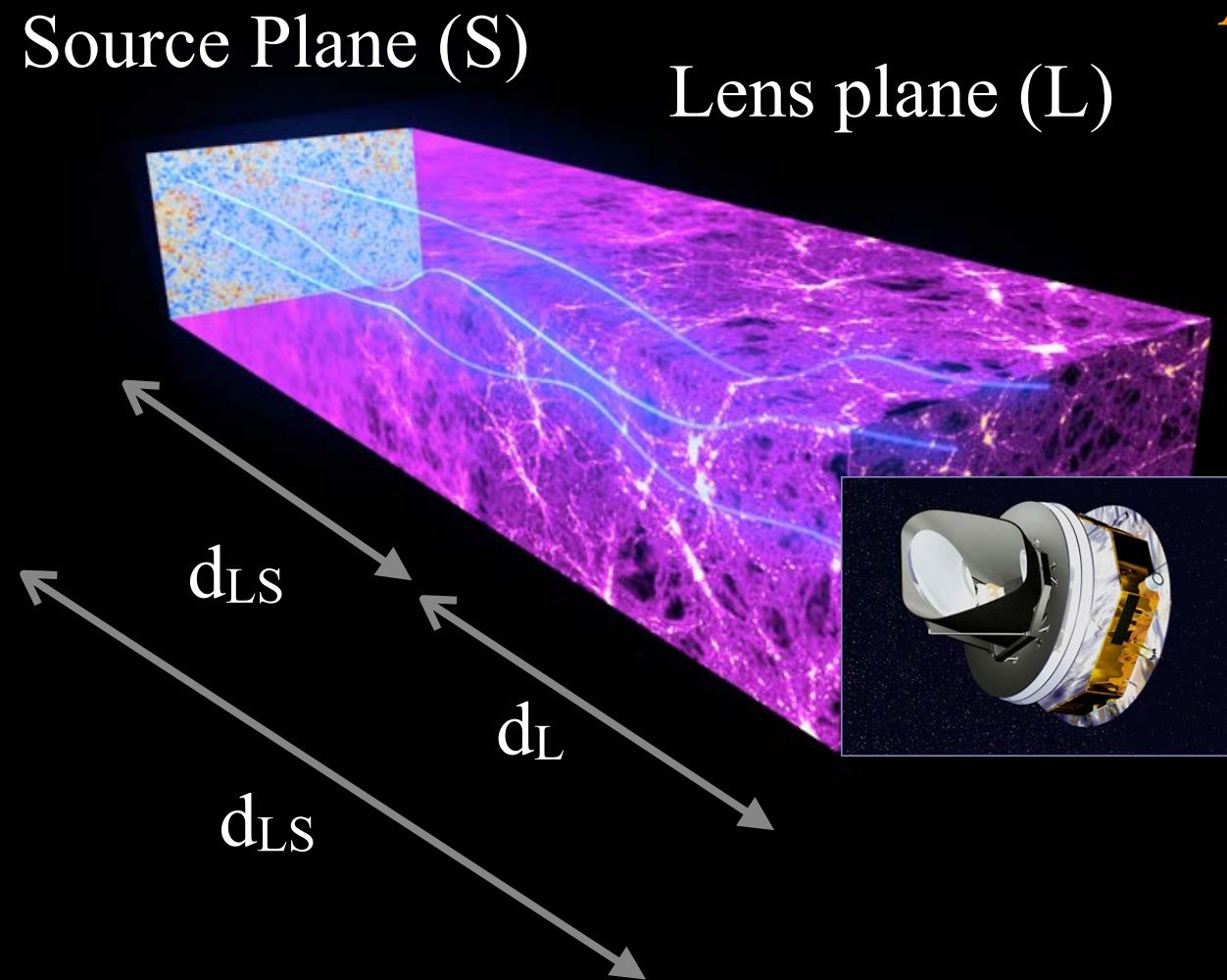
A slice of (dark matter) life at $z \sim 1$



$$\vec{\alpha} = \nabla_{\vec{\theta}} \left\{ \int \left(\frac{d_{LS}}{d_L d_S} \right) \Phi \left[d(\eta) \vec{\theta}, \eta \right] d\eta \right\}$$

CMB LENSING

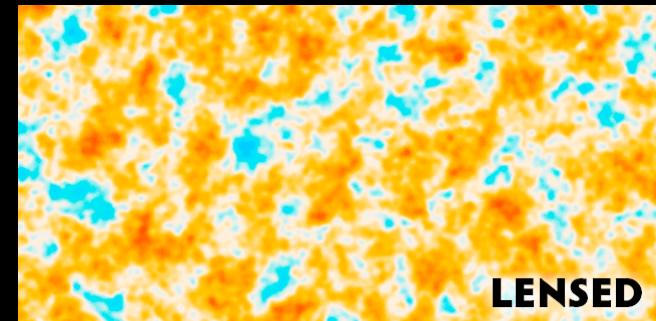
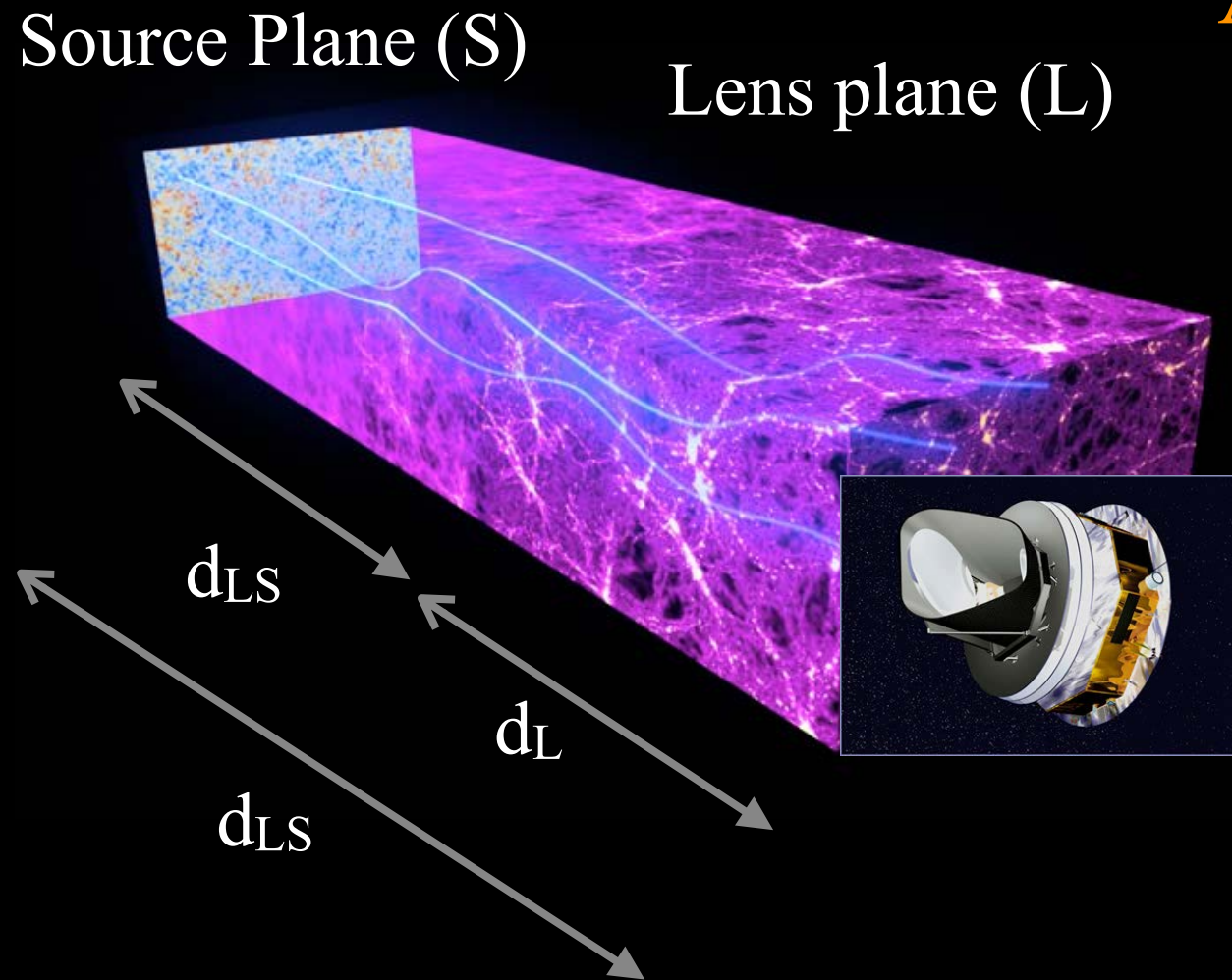
A slice of (dark matter) life at $z \sim 1$



$$\vec{\alpha} = \nabla_{\vec{\theta}} \left\{ \int \left(\frac{d_{LS}}{d_L d_S} \right) \Phi \left[d(\eta) \vec{\theta}, \eta \right] d\eta \right\}$$

CMB LENSING

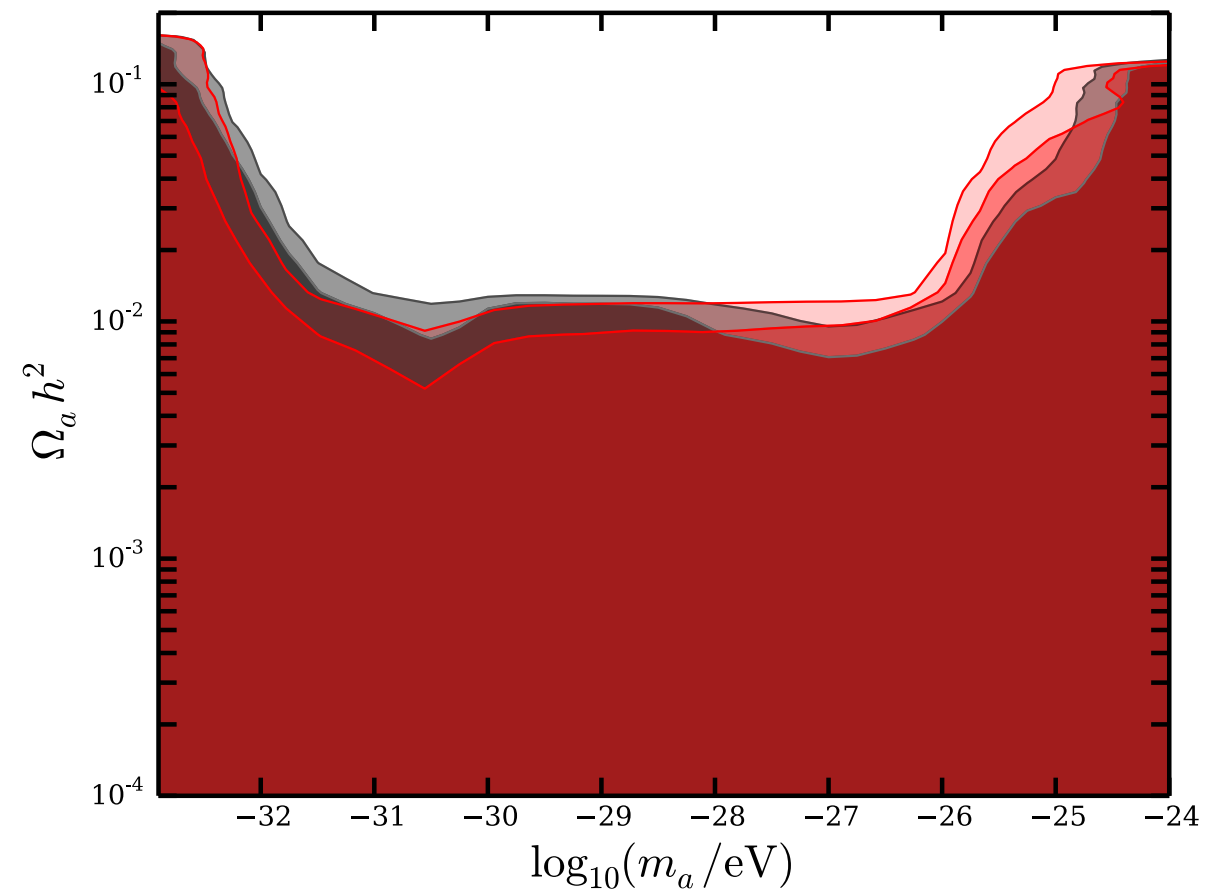
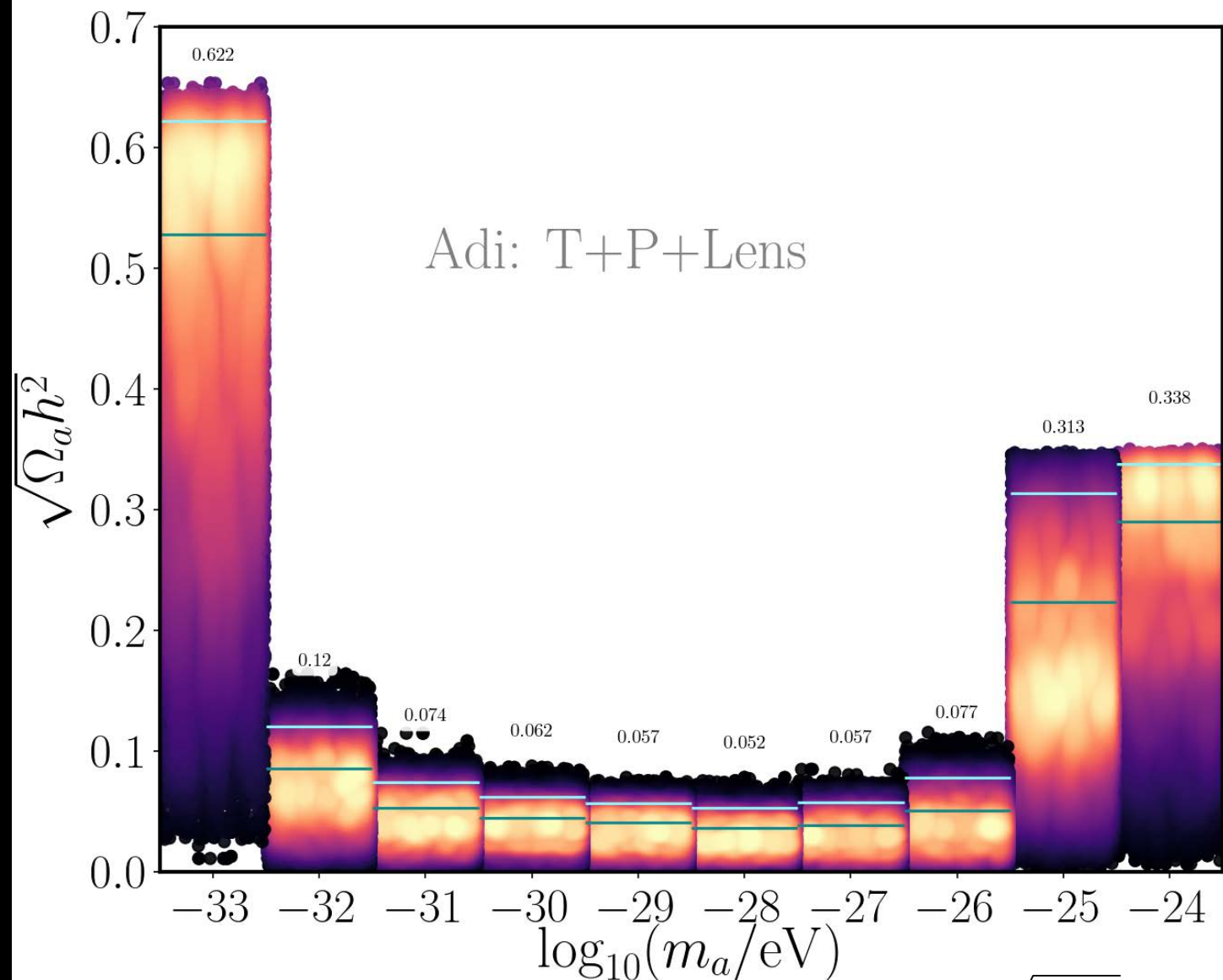
A slice of (dark matter) life at $z \sim 1$



$$\vec{\alpha} = \nabla_{\vec{\theta}} \left\{ \int \left(\frac{d_{LS}}{d_L d_S} \right) \Phi \left[d(\eta) \vec{\theta}, \eta \right] d\eta \right\}$$

ULAs change

CMB LENSING



<https://arxiv.org/abs/1708.05681>

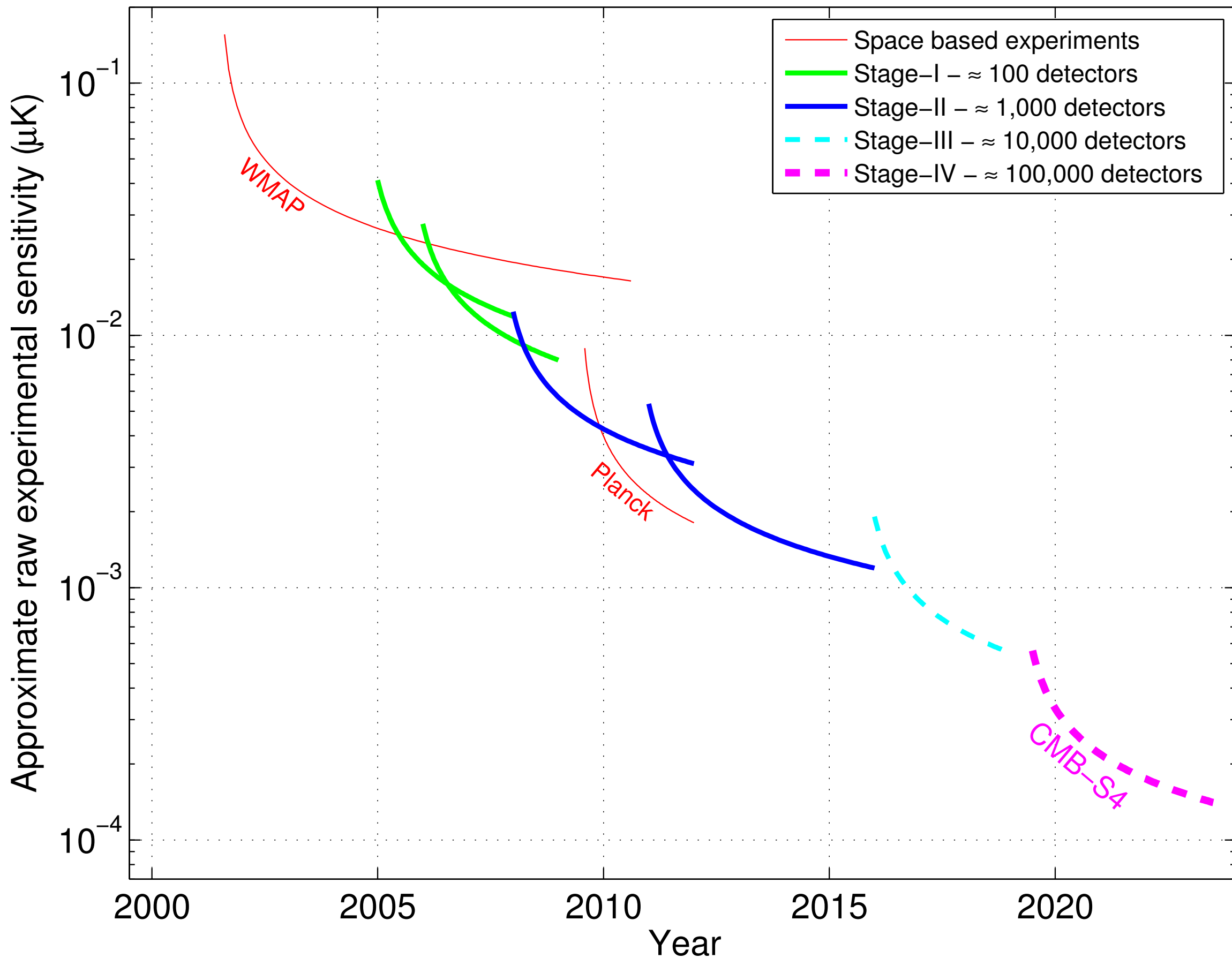
Monthly Notices of the Royal Astronomical Society, Volume 476,
Issue 3, 21 May 2018, Pages 3063–3085



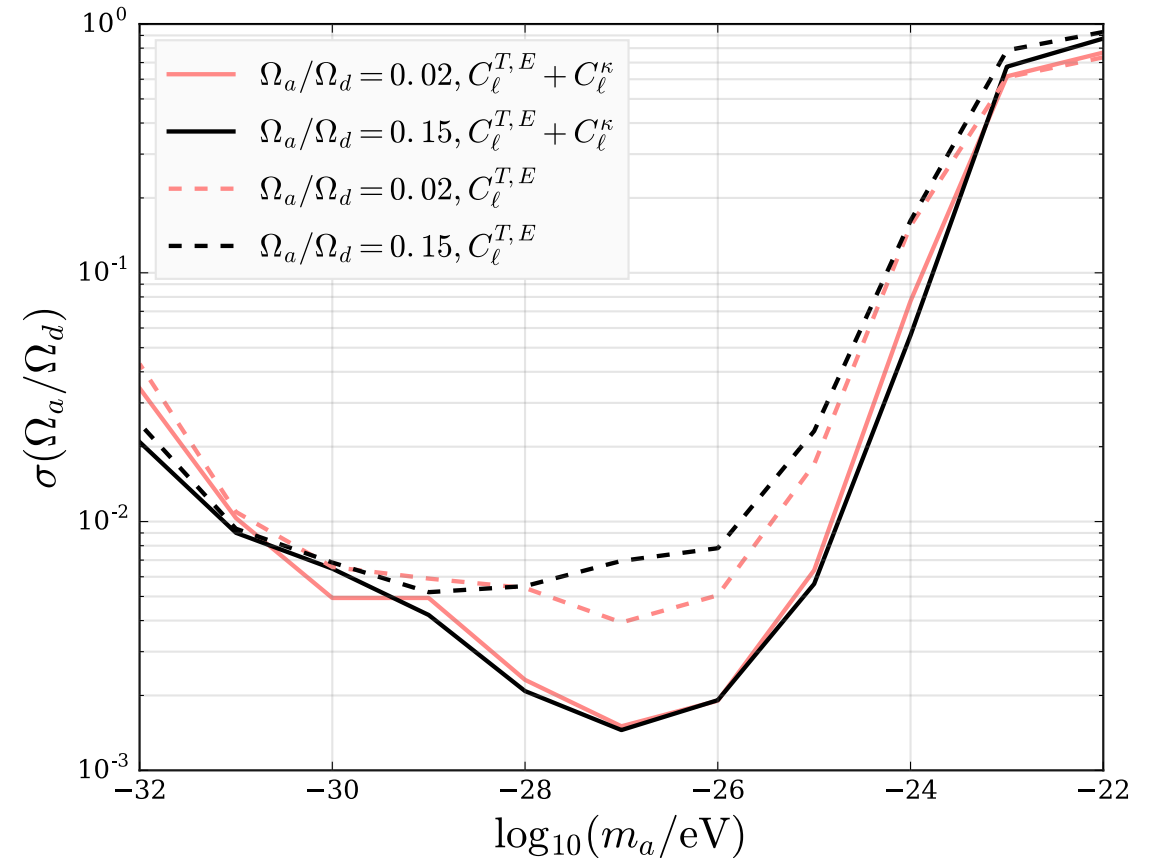
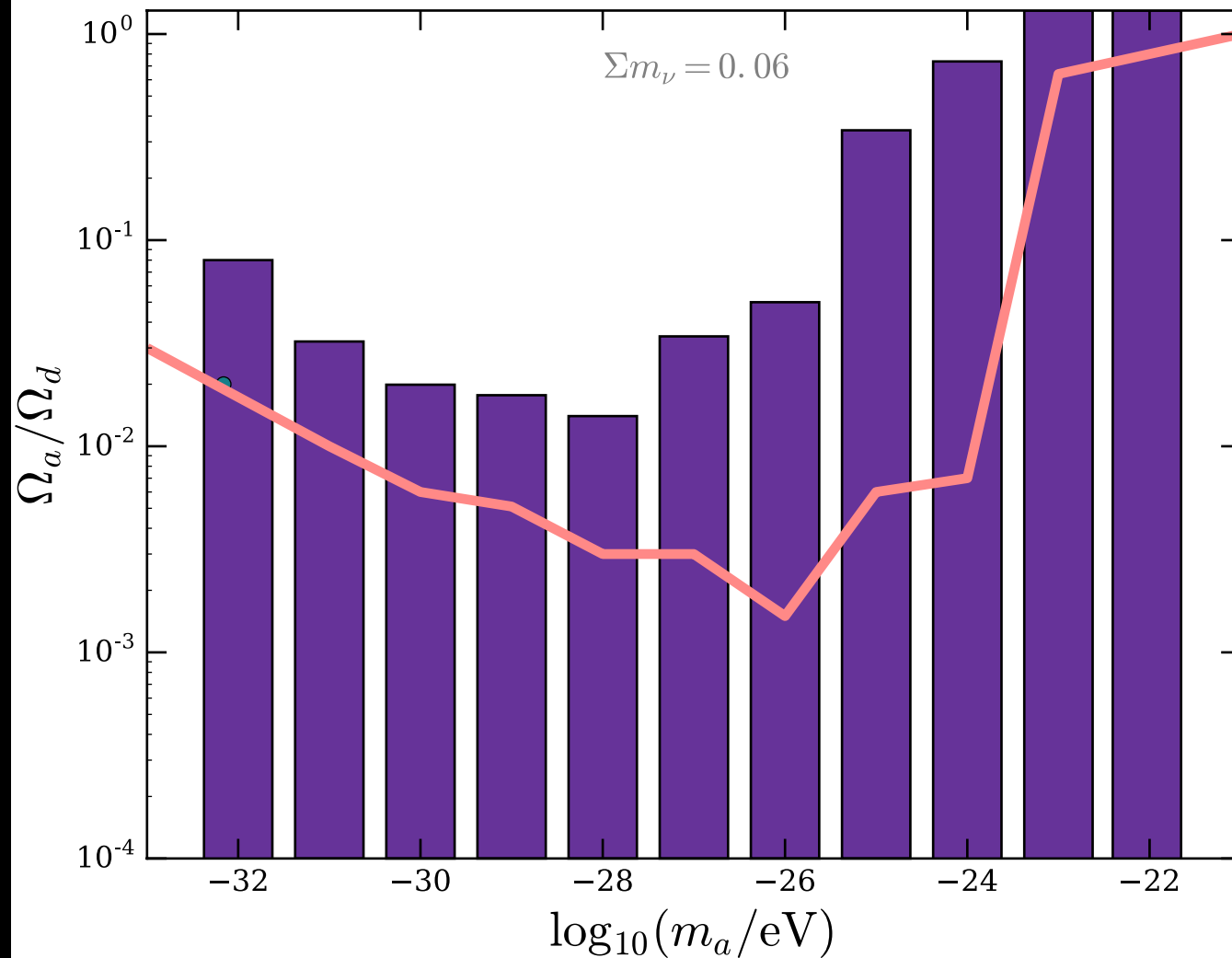
- * Next gen. CMB ground-based expt. concept
 - * ~ 1 arcmin beam
 - * $1 \mu\text{K}$ arcmin noise level
 - * $\sim 500,000$ detectors
 - * Location, sky coverage TBD

From CMB-S4 Science book... [arXiv: 1610.02743](https://arxiv.org/abs/1610.02743)

CMB-S4



S4-CAST FOR LENSING AND ULAS



Fisher forecast using OXFISH code—OOM
improvement driven by lensing

R.Hlozek, D.J.E. Marsh, D.G., J. Dunkley, R. Allison, E. Calabrese

arXiv: 1607.08208, Phys. Rev. D 95, 123511 (2017).

NON-LINEAR MATTERS

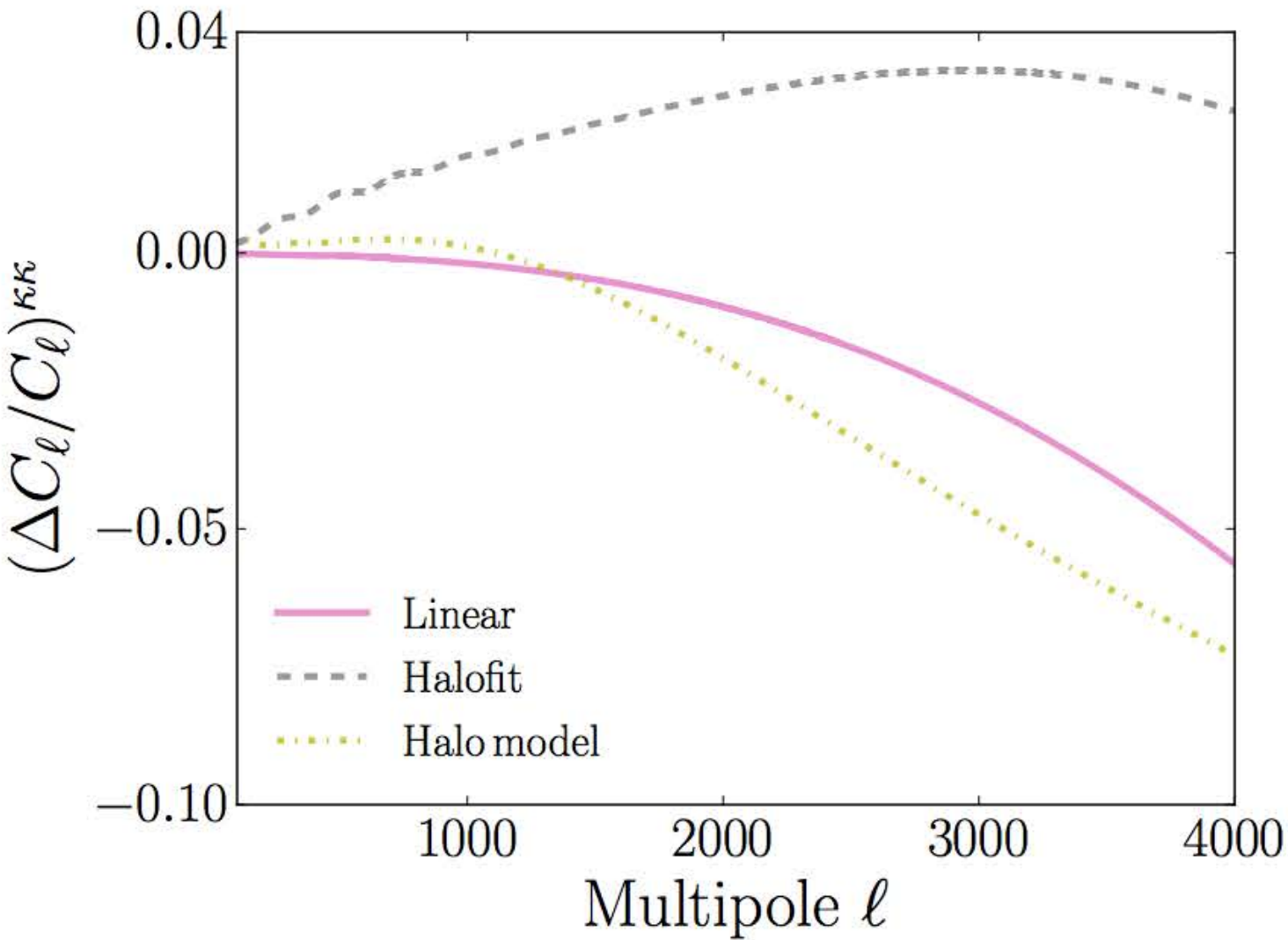


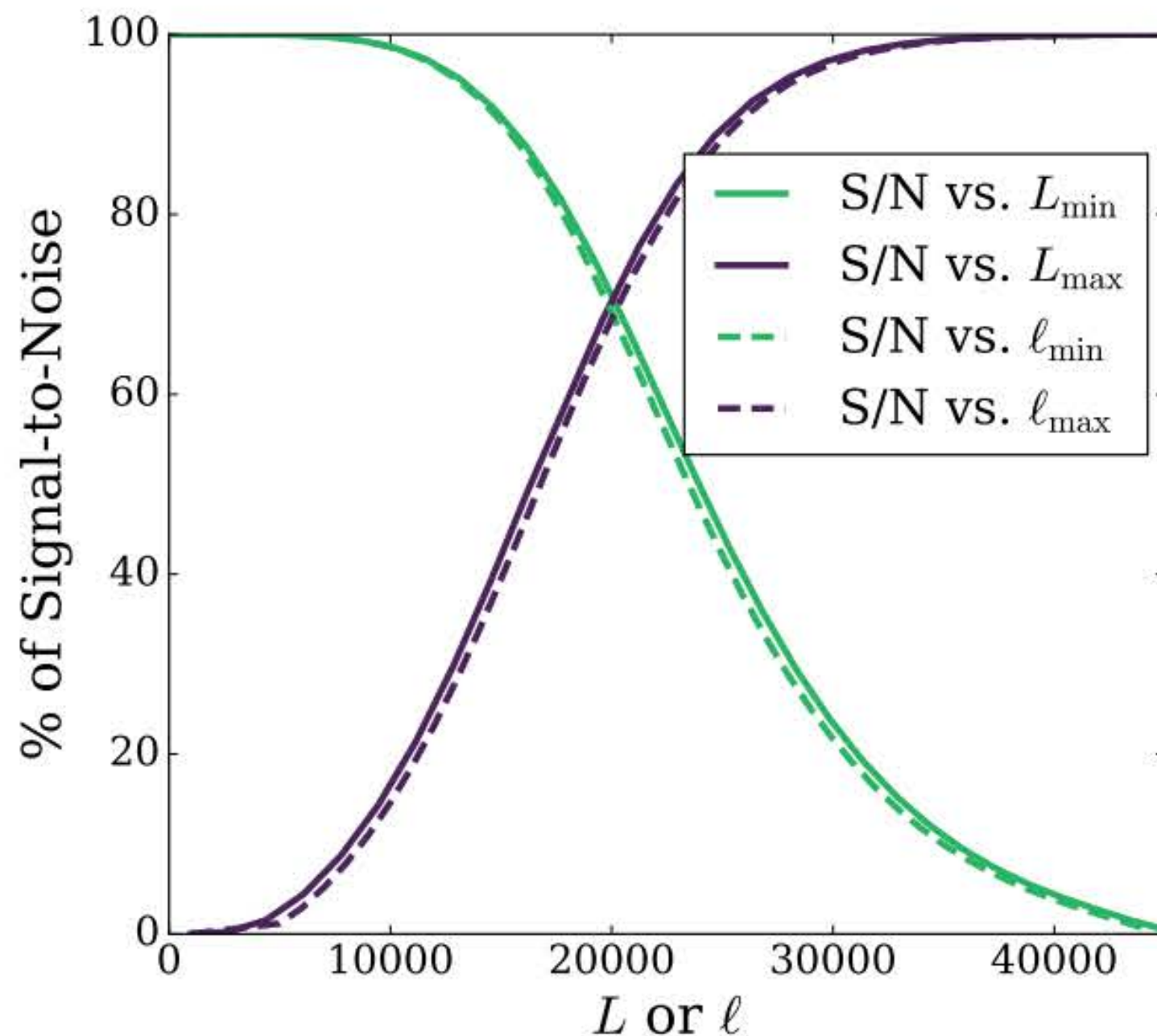
FIG. 3. Comparison of ULAs to CDM in lensing deflection power for different models of non-linearities, where ULAs with $m_a = 10^{-23}$ eV constitute all the DM. The unphysical power increase in the HALOFIT power for ULAs, seen in Figure 4, causes a similar unphysical increase in lensing power compared to the halo model. On the other hand, linear theory captures the sign and approximate magnitude of the effect seen in the halo model. Thus when forecasting constraints at high ULA mass we choose to use linear theory lensing as a reasonable approximation for the Fisher matrix derivative.

R.Hlozek, D.J.E. Marsh, D.G., J. Dunkley, R. Allison, E. Calabrese

arXiv: 1607.08208, Phys. Rev. D 95, 123511 (2017).

NON-LINEAR MATTERS

Nguyen, Sehgal, Madhavacheril, arXiv: 1710.03747

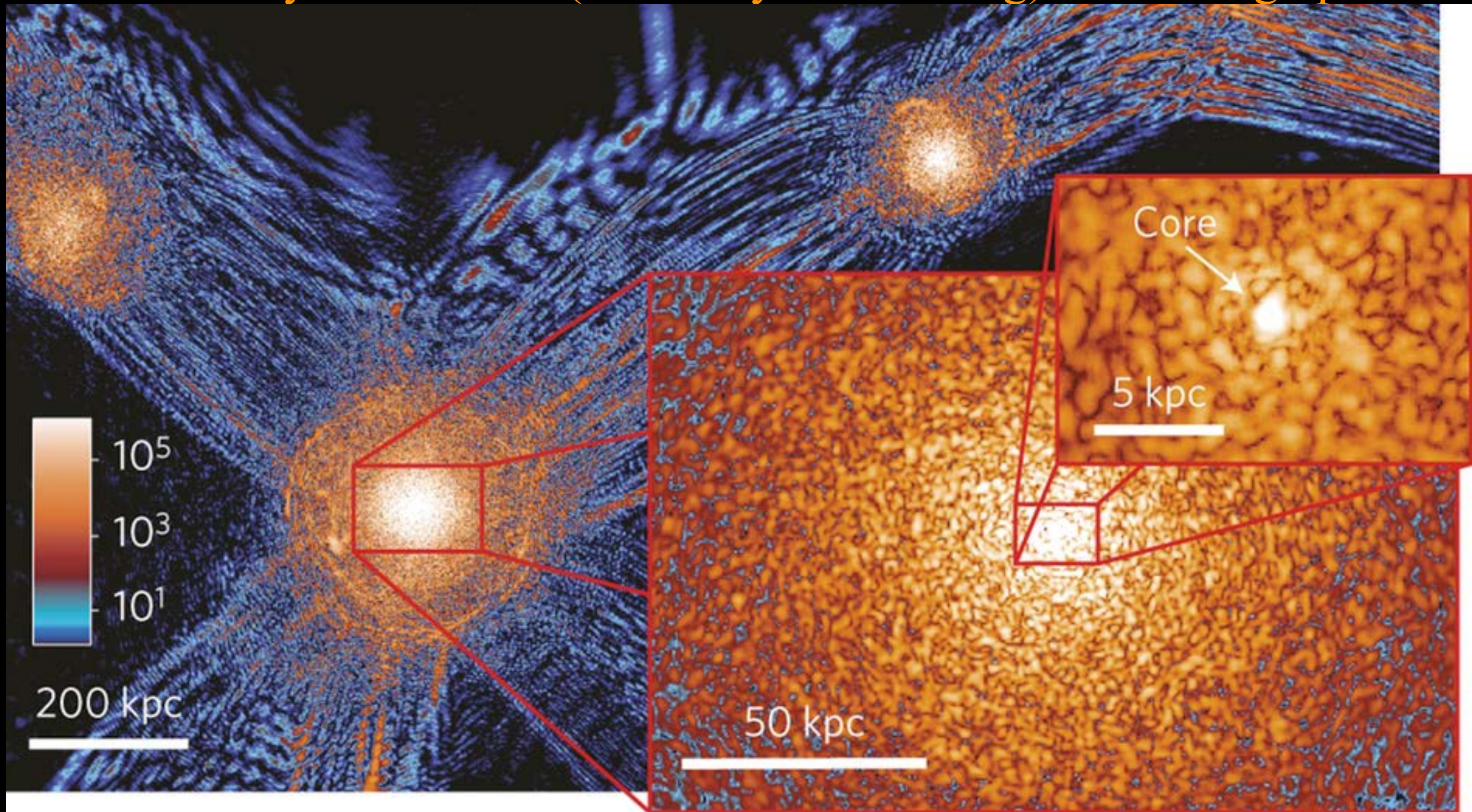


R.Hlozek, D.J.E. Marsh, D.G., J. Dunkley, R. Allison, E. Calabrese

arXiv: 1607.08208, Phys. Rev. D 95, 123511 (2017).

NON-LINEAR MATTERS

Fuzzy simulations (and analytic modeling) are heating up!



Cores! (Hu/Gruzinov/Barkana 2001, see also Marsh and Silk 2013, Marsh and Pop 2015, Matos 2012, Schive 2014, Vogelsberger 2017, and others)

Real Story

$$\frac{1}{R} \partial_t [R \partial_t a(\vec{x})] - (\nabla^2 - m_a^2 R^2) a(\vec{x}, t) \propto \Psi$$

Fluid Approximation

$$\delta\phi = A_c \Delta_c(k, \eta) \cos(m\eta) + A_s \Delta(k, \eta) \sin(m\eta)$$

$$c_s^2 = \frac{k^2 / (4m_a^2 a^2)}{1 + k^2 / (4m_a^2 a^2)} + \left(\frac{\mathcal{H}}{m_a} \right)^2 g(k, \eta, m_a)$$

Work in progress,
J. Cookmeyer
HC 2017, now
at Berkeley

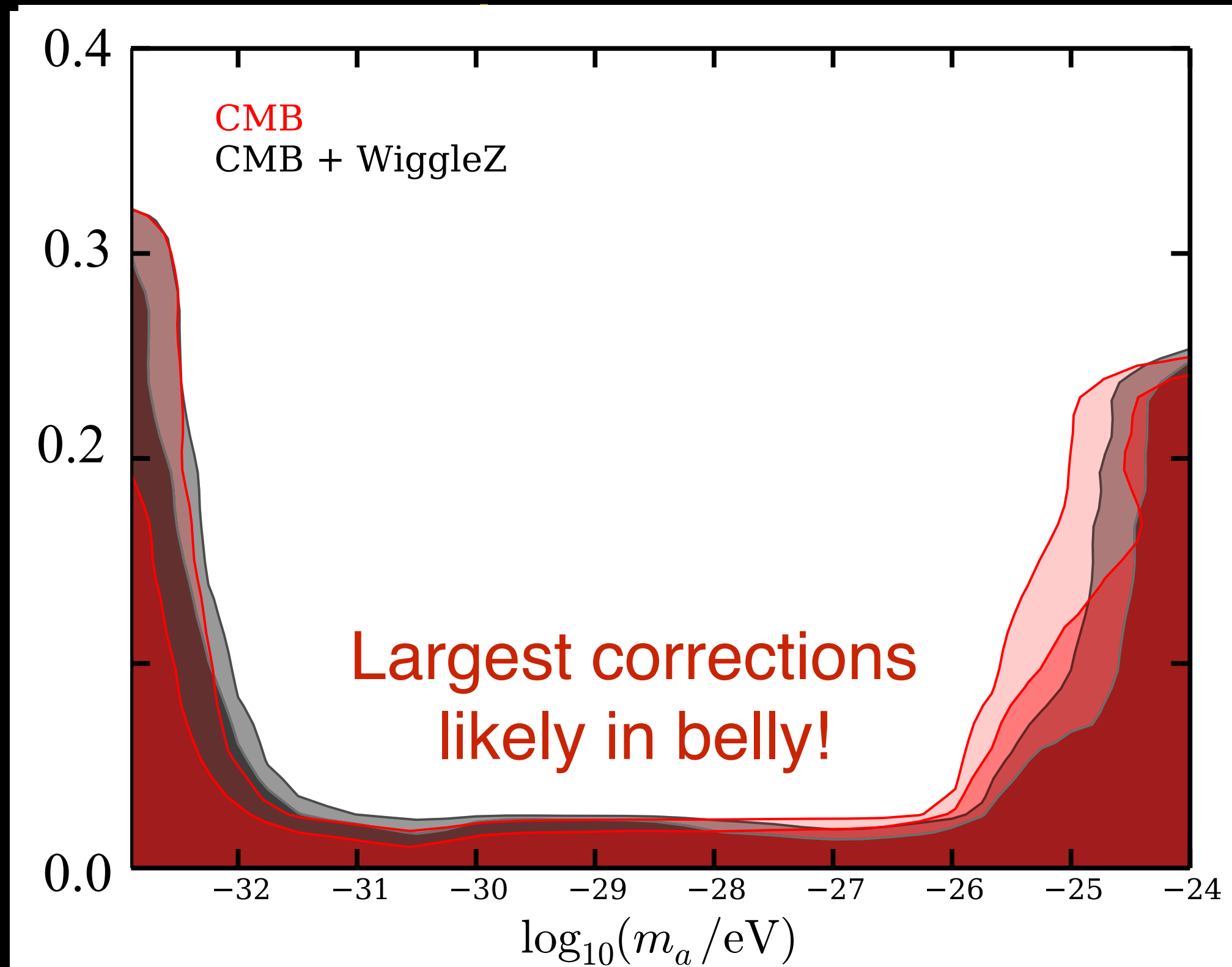


see also work by Urena-Lopez and Gonzalez-Morales, JCAP, arXiv: 1511.08195

IMPROVING THEORETICAL PREDICTIONS



Work in progress,
J. Cookmeyer
HC 2017, now
at Berkeley

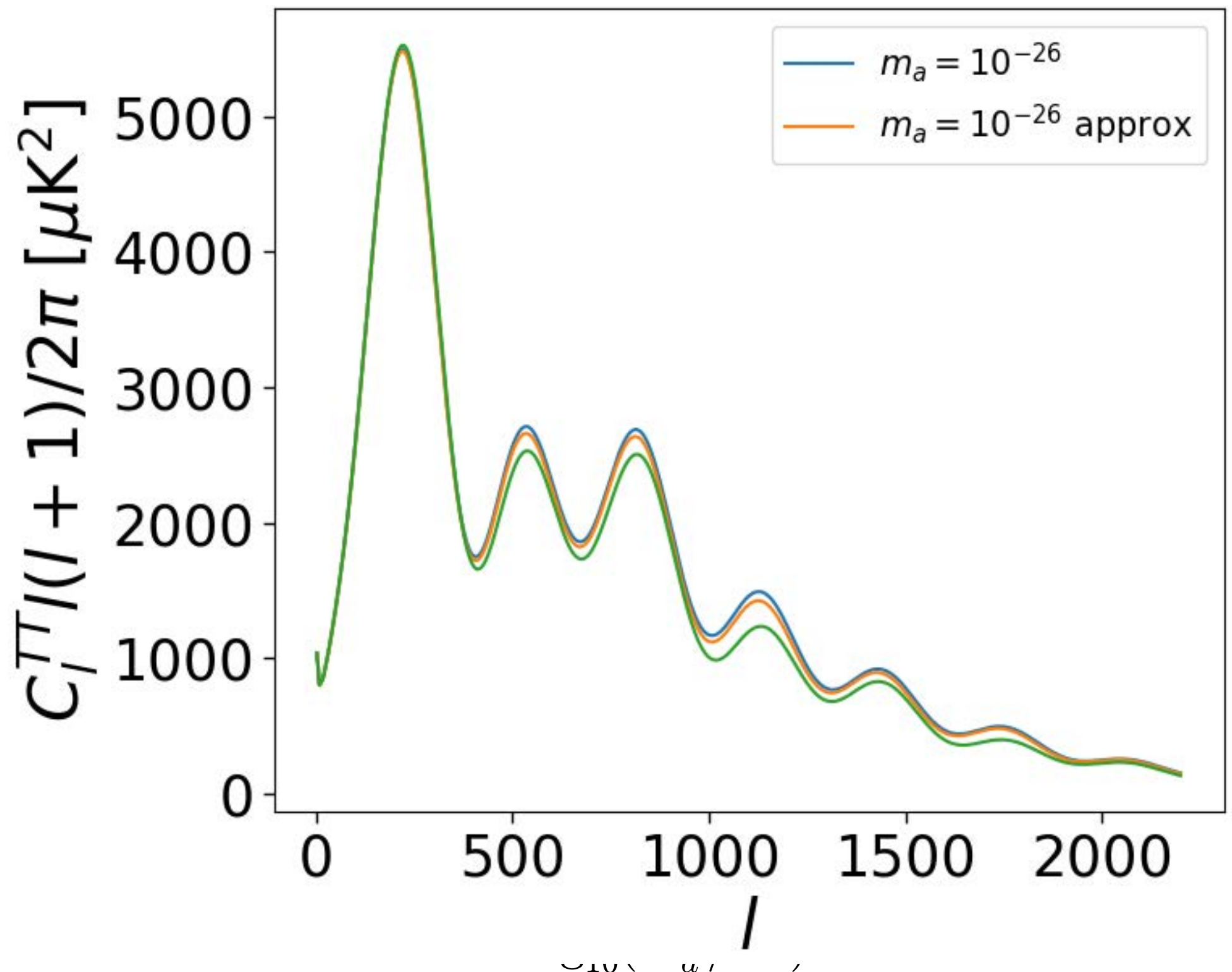


see also work by Urena-Lopez and Gonzalez-Morales, JCAP, arXiv: 1511.08195

IMPROVING THEORETICAL PREDICTIONS



Work in progress,
J. Cookmeyer
HC 2017, now
at Berkeley

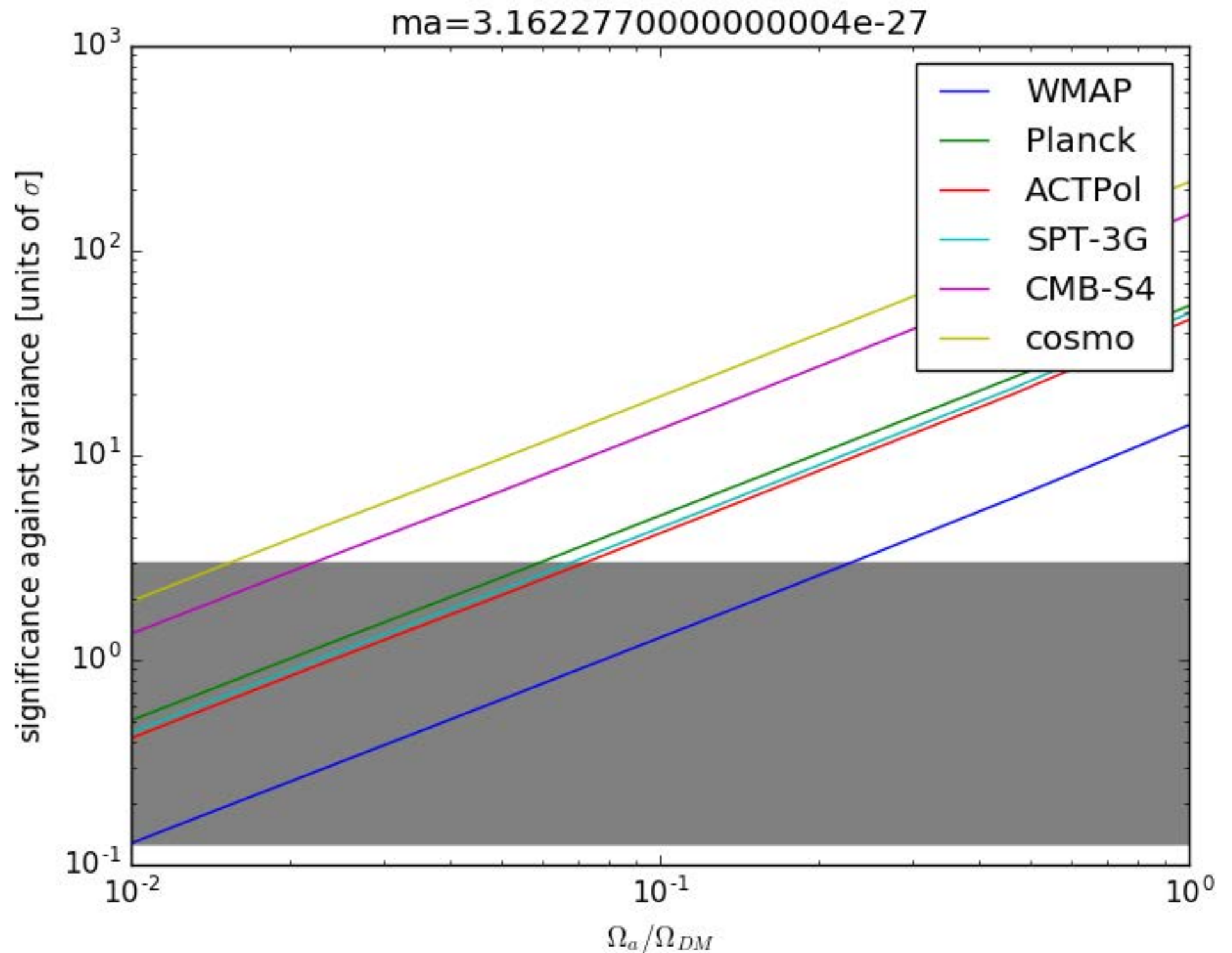


see also work by Urena-Lopez and Gonzalez-Morales, JCAP, arXiv: 1511.08195

IMPROVING THEORETICAL PREDICTIONS

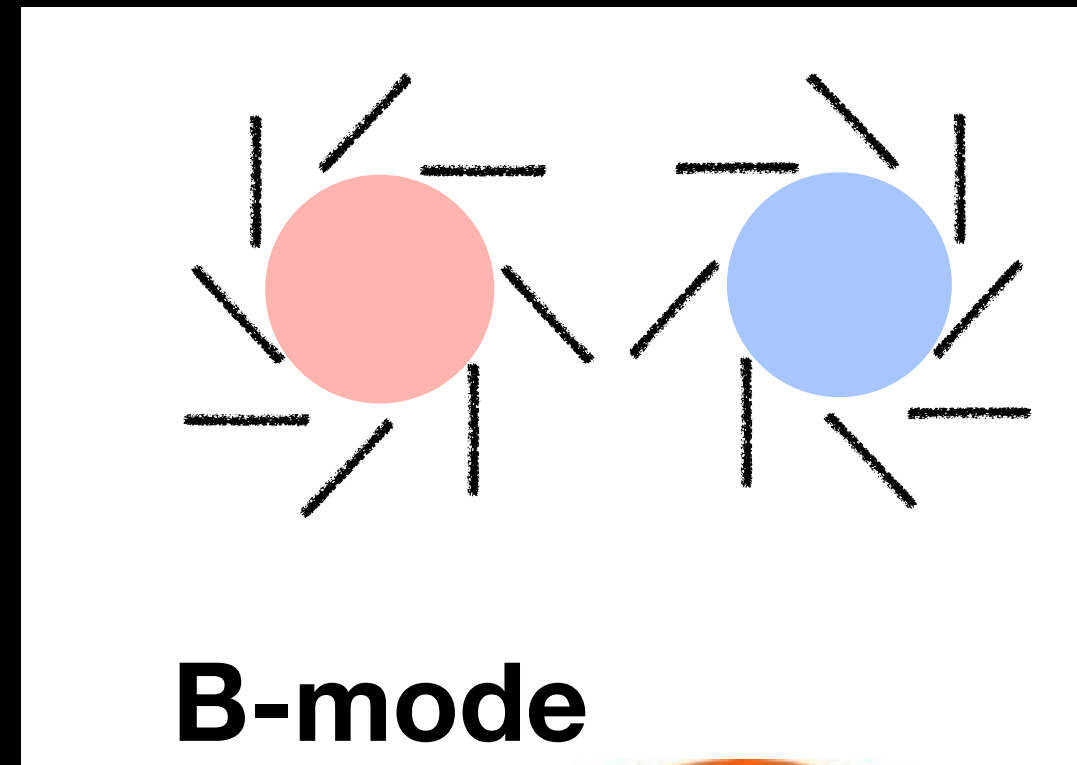
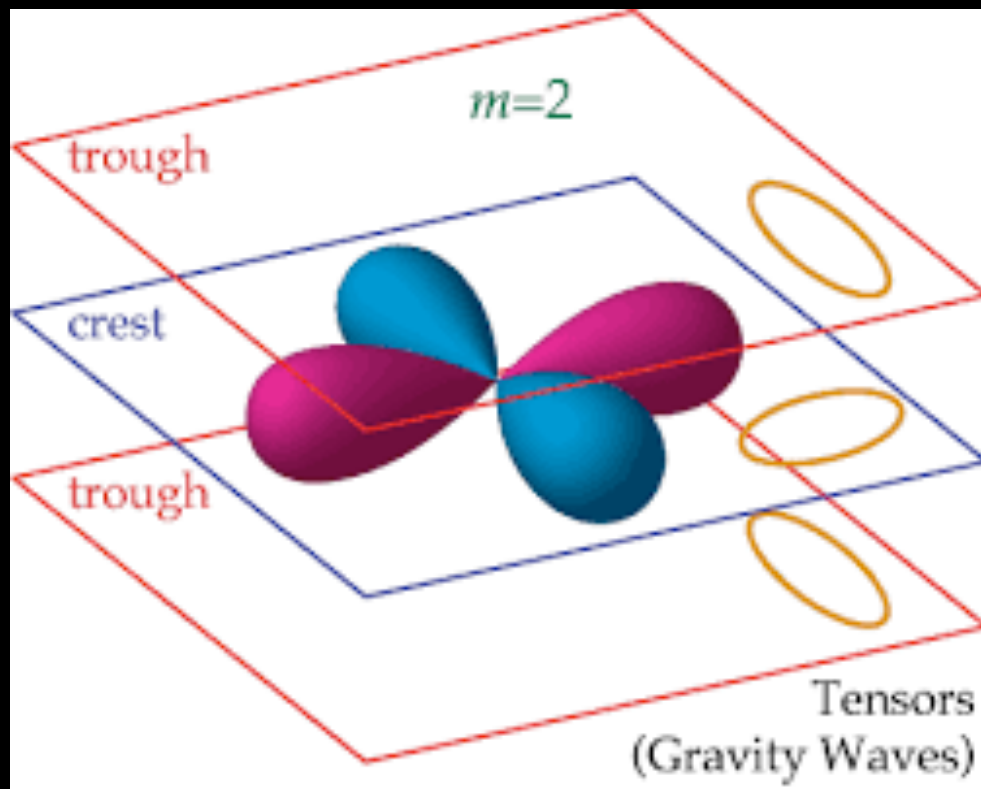


Work in progress,
J. Cookmeyer
HC 2017, now
at Berkeley



see also work by Urena-Lopez and Gonzalez-Morales, JCAP, arXiv: 1511.08195

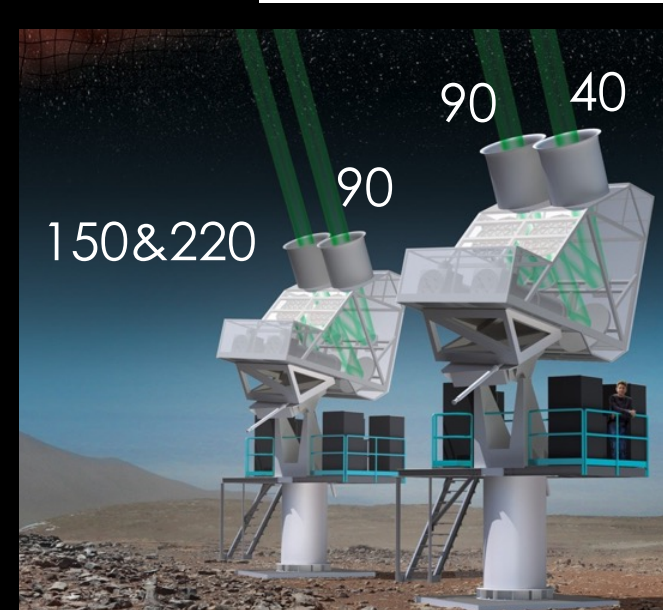
ULAS AS AN INFLATIONARY PROBE



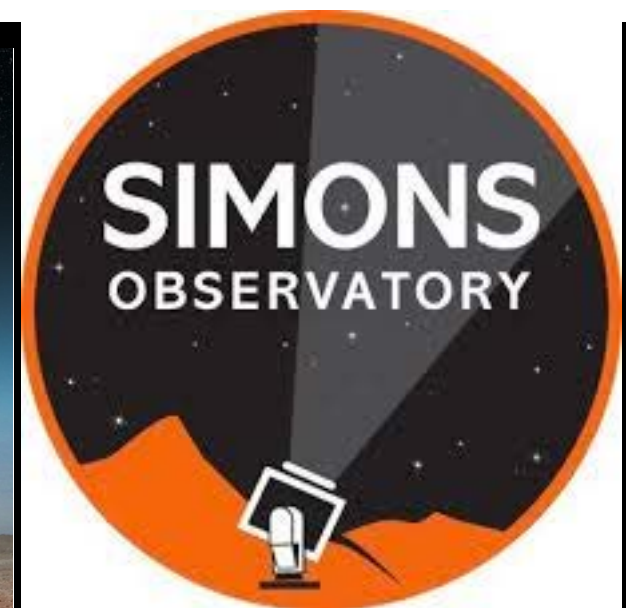
Spider



SPT/BICEP2-3/KECK



CLASS



PICO



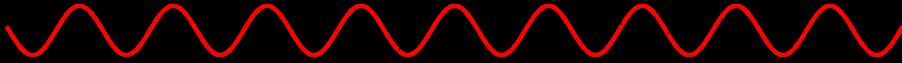
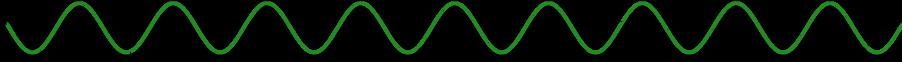
$$r = 16\varepsilon \approx 0.17 \left(\frac{2.1 \times 10^{-9}}{A_s} \right) \left(\frac{H_I}{10^{14} \text{ GeV}} \right)^2$$

AXIONS AND ISOCURVATURE

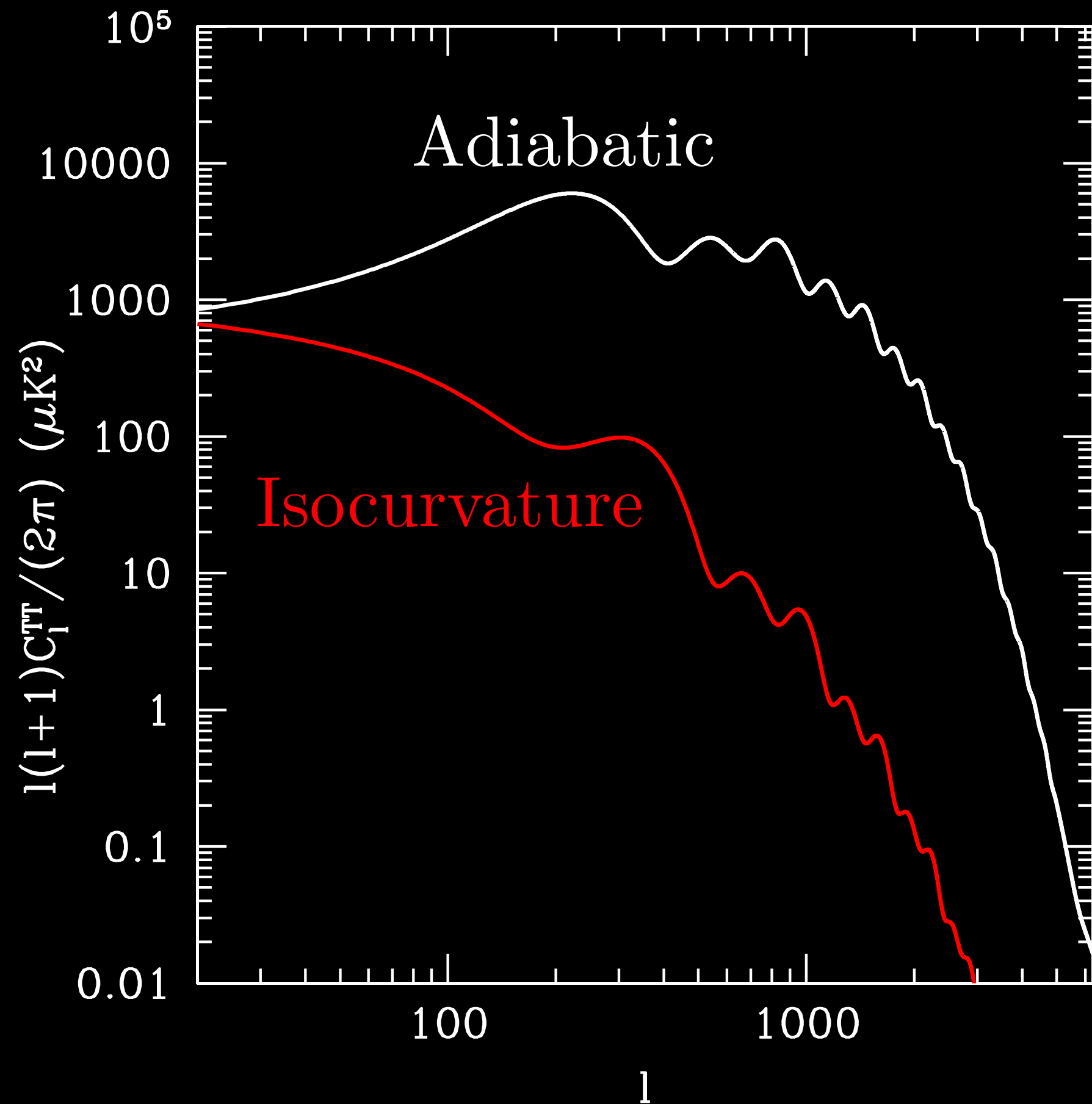
* Quantum zero-point fluctuations in axion field

$$\sqrt{\langle a^2 \rangle} = \frac{H_I}{2\pi}$$

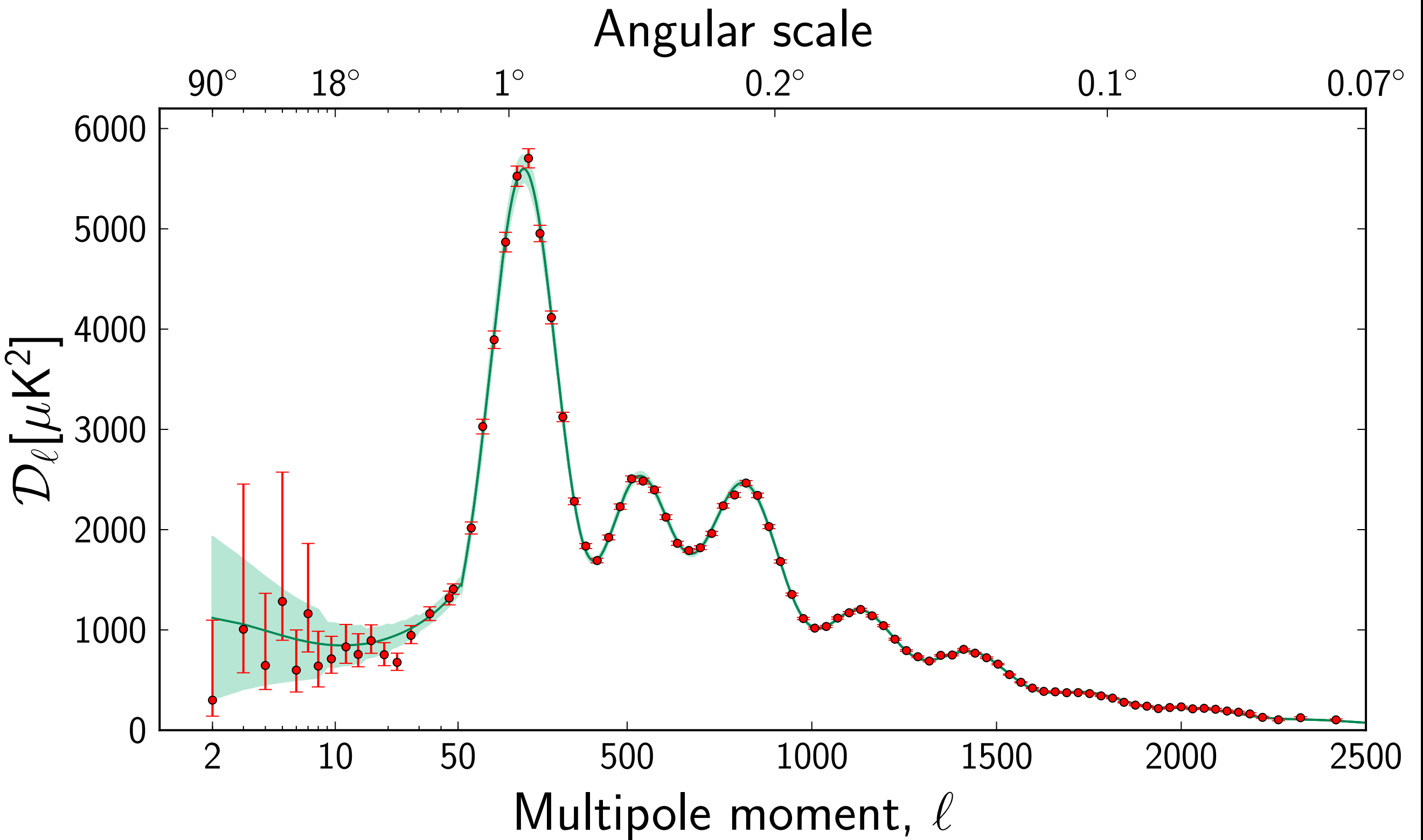
* Subdominant species seed isocurvature fluctuations

	Neutrinos
	CDM
	Photons
	Baryons

AXIONS AND ISOCURVATURE



AXIONS AND ISOCURVATURE



FORECAST/FUTURE WORK: TENSORS AND ULAS

* Planck TT constraints

$$\frac{H_I}{f_a \bar{\theta}} \frac{\Omega_a}{\Omega_d} \lesssim 4 \times 10^{-5}$$

$$\frac{P_{\text{iso}}}{P_{\text{tot}}} \lesssim 1.6 \times 10^{-2}$$

Also see Gondolo and Visinelli 2012

$$H_I \simeq 10^{14} \text{ GeV}$$

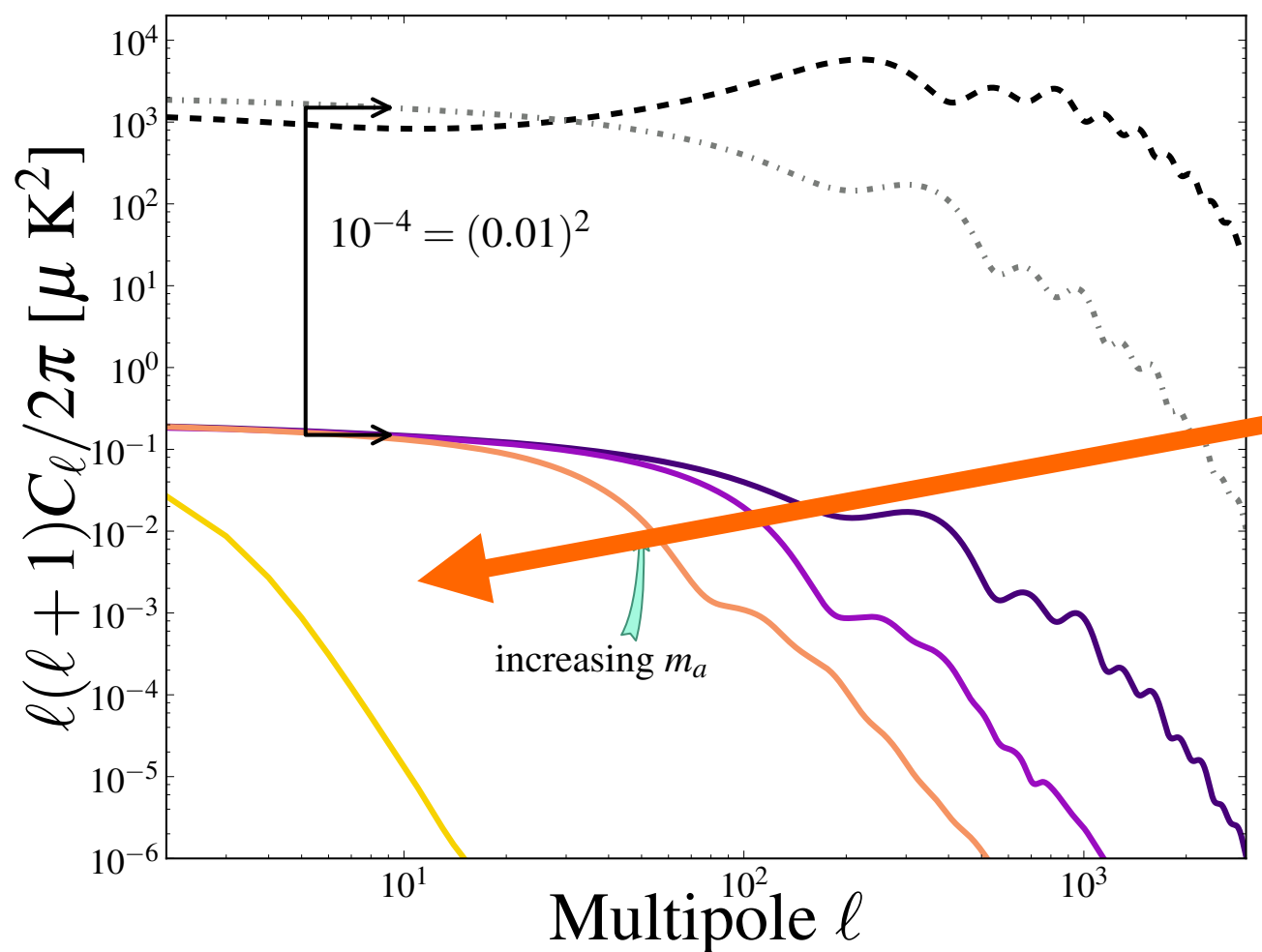
$$\frac{\Omega_a}{\Omega_a + \Omega_c} \lesssim 10^{-12} \left(\frac{0.2}{r} \right)^{7/2}$$

**QCD
axion**

$$\frac{\Omega_a}{\Omega_a + \Omega_c} \lesssim 10^{-3} \left(\frac{0.2}{r} \right)$$

ULAs

FORECAST/FUTURE WORK: TENSORS AND ULAS

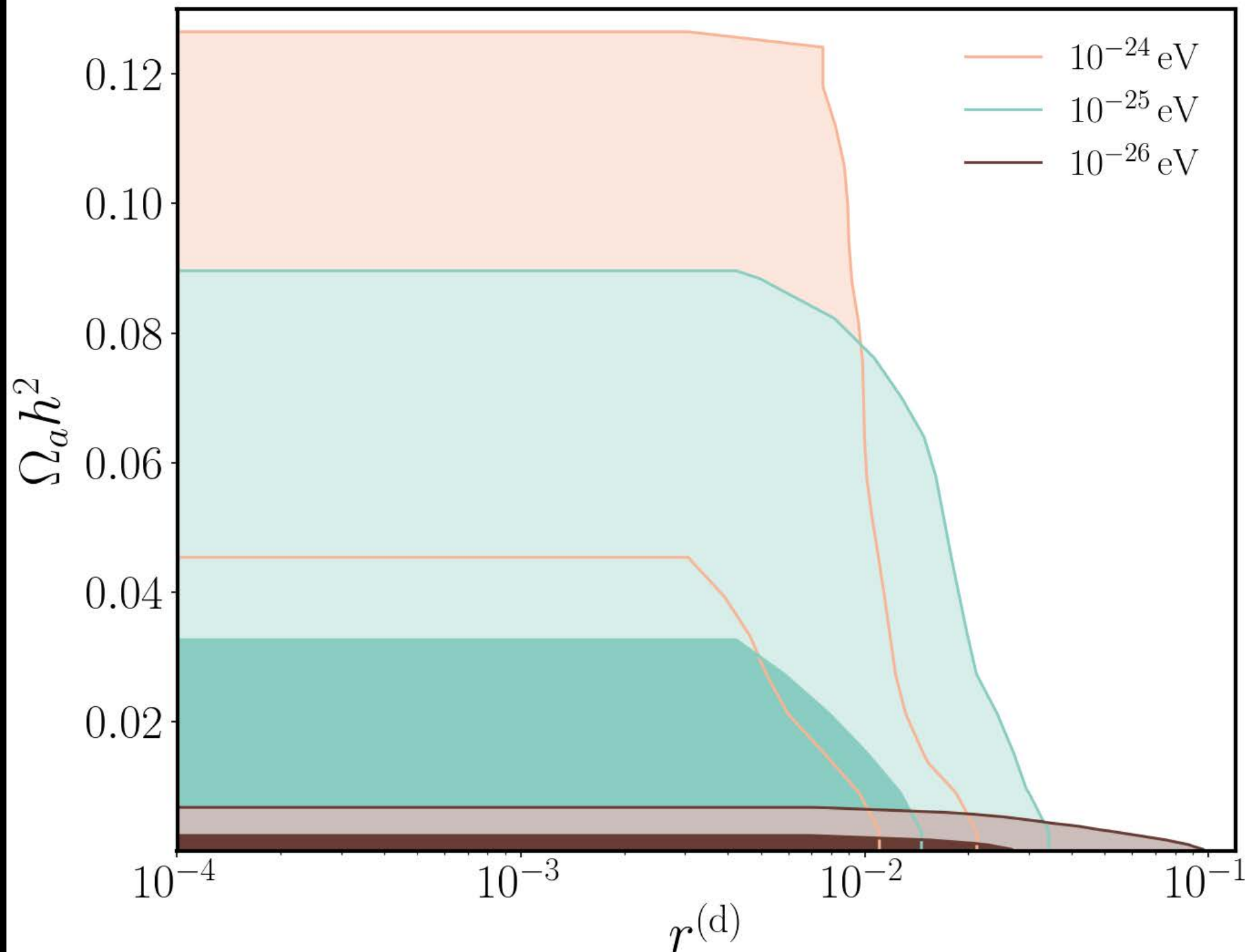


- * Low- ℓ plateau disappears
- * Information lost
- * Planck limits assume CDM isocurvature

* For $m_a \leq 10^{-27}$ eV, constraints cannot be simply remapped.

TENSORS + ISOCURVATURE (RESULTS!)

FROM ARXIV: 1708.05681

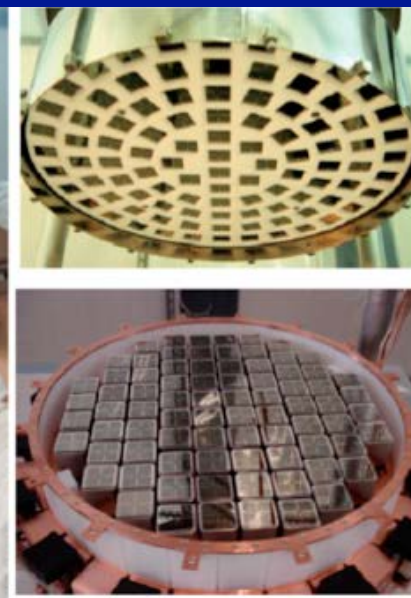
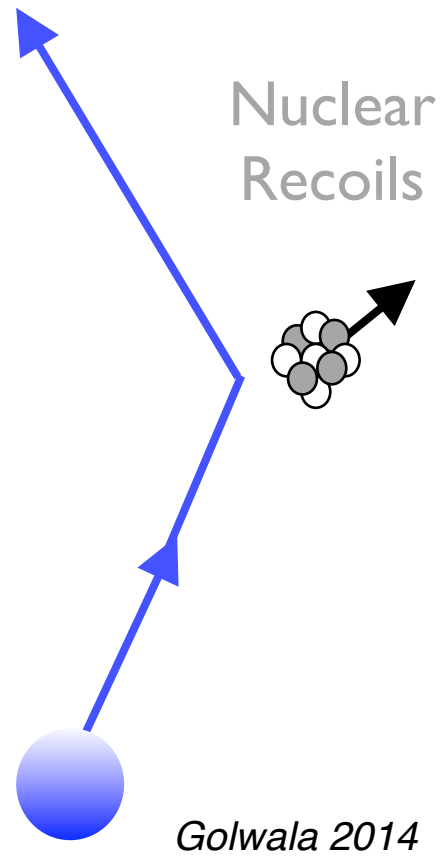


CONCLUSIONS

- * $\sim 5\%$ level constraints on ultra-light axions from CMB
- * CMB lensing can probe ultra-light axions:
 - * 1% sensitivity with next-generation experiments
- * Complementary constraints to inflationary energy scale

Most likely and desired overflow slides

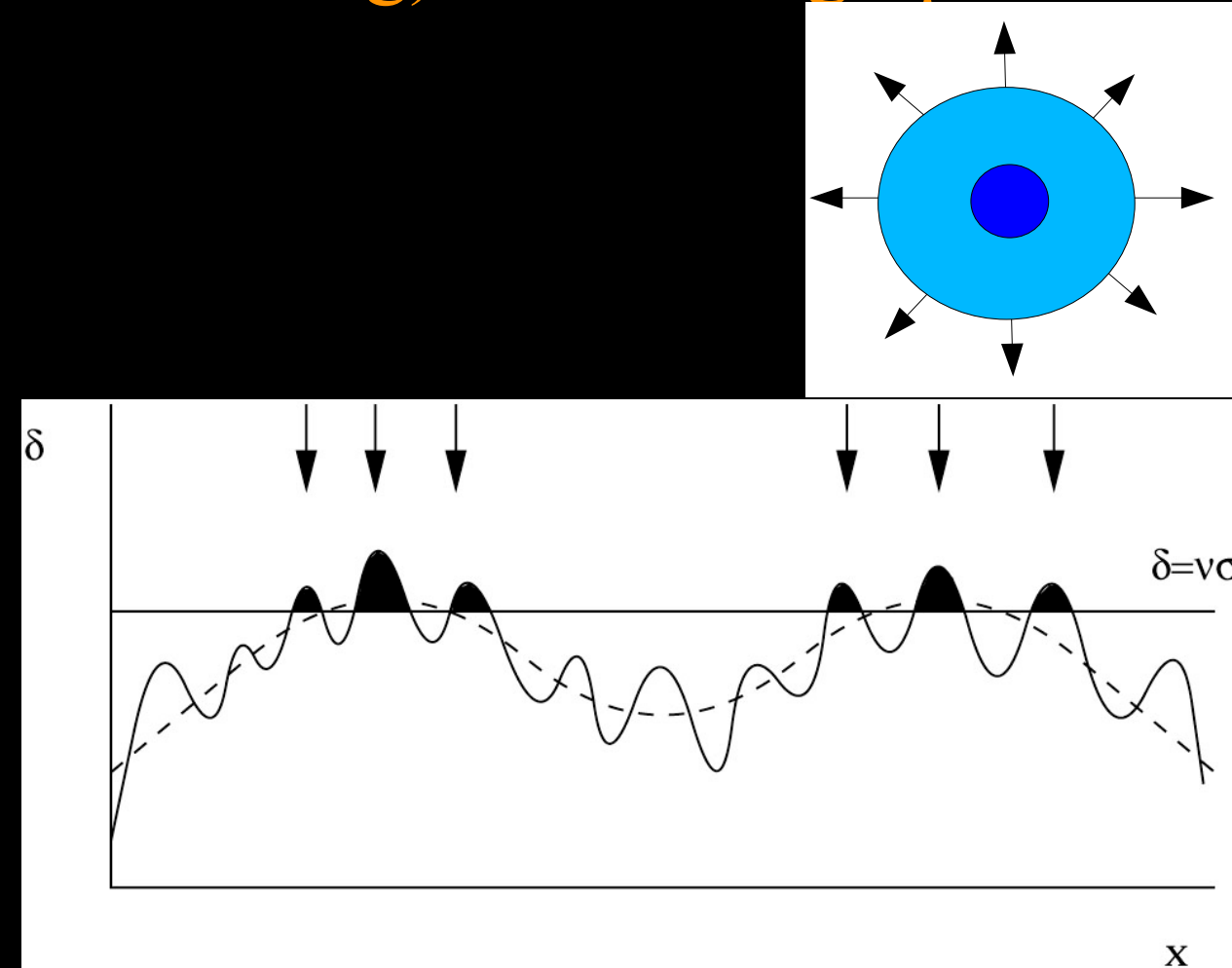
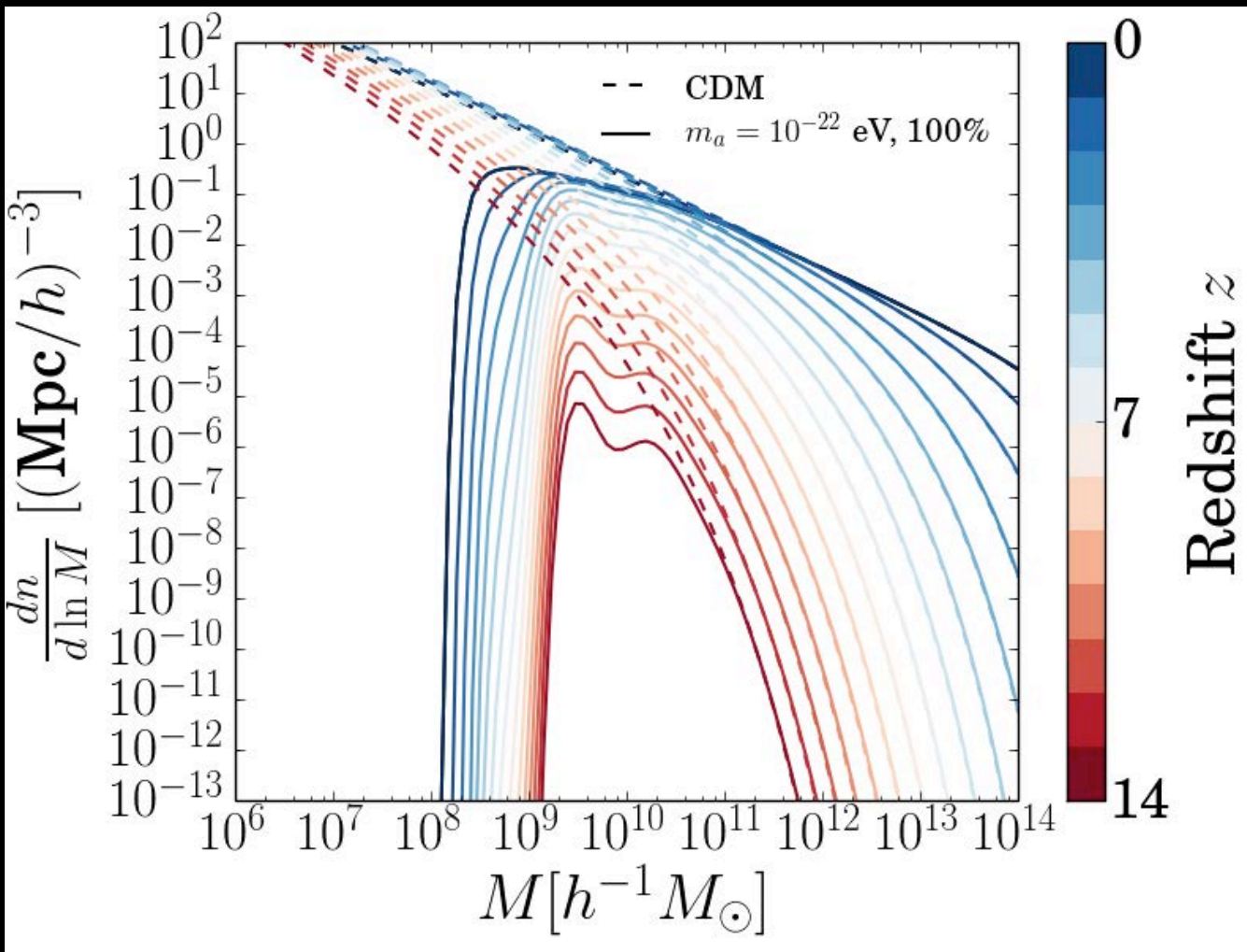
DARK MATTER: TERRESTRIAL EXPERIMENT



Search for WIMP (weakly interacting massive particle)
with $m \sim 100$ GeV: So far, no dice!

NON-LINEAR MATTERS

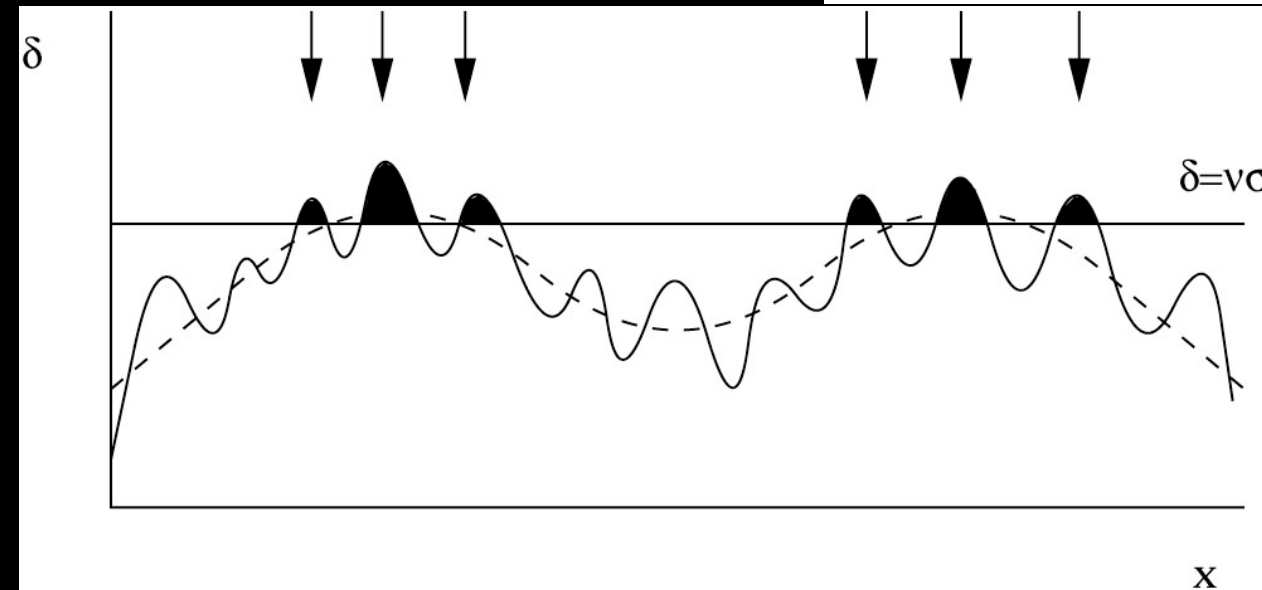
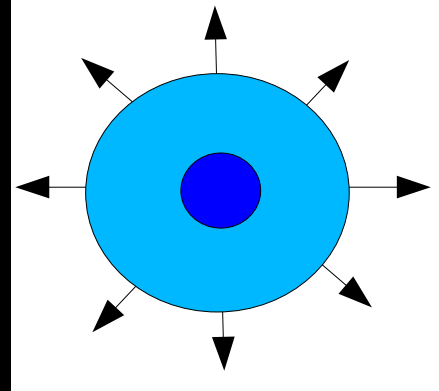
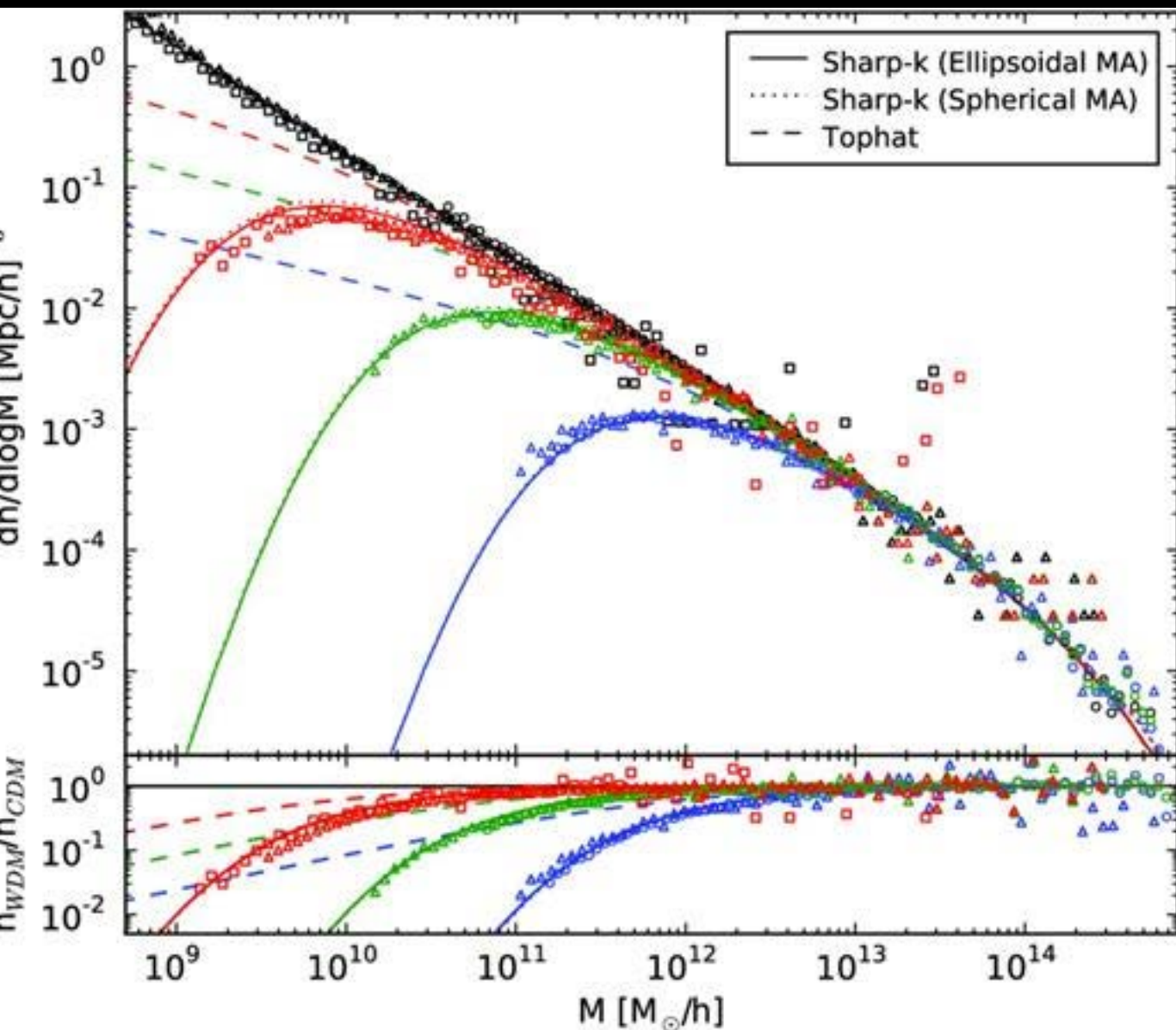
Fuzzy simulations (and analytic modeling) are heating up!



Cores! (Hu/Gruzinov/Barkana 2001, see also Marsh and Silk 2013, Marsh and Pop 2015, Matos 2012, Schive 2014, Vogelsberger 2017, and others)

NON-LINEAR MATTERS

Fuzzy simulations (and analytic modeling) are heating up!



Schneider 2015

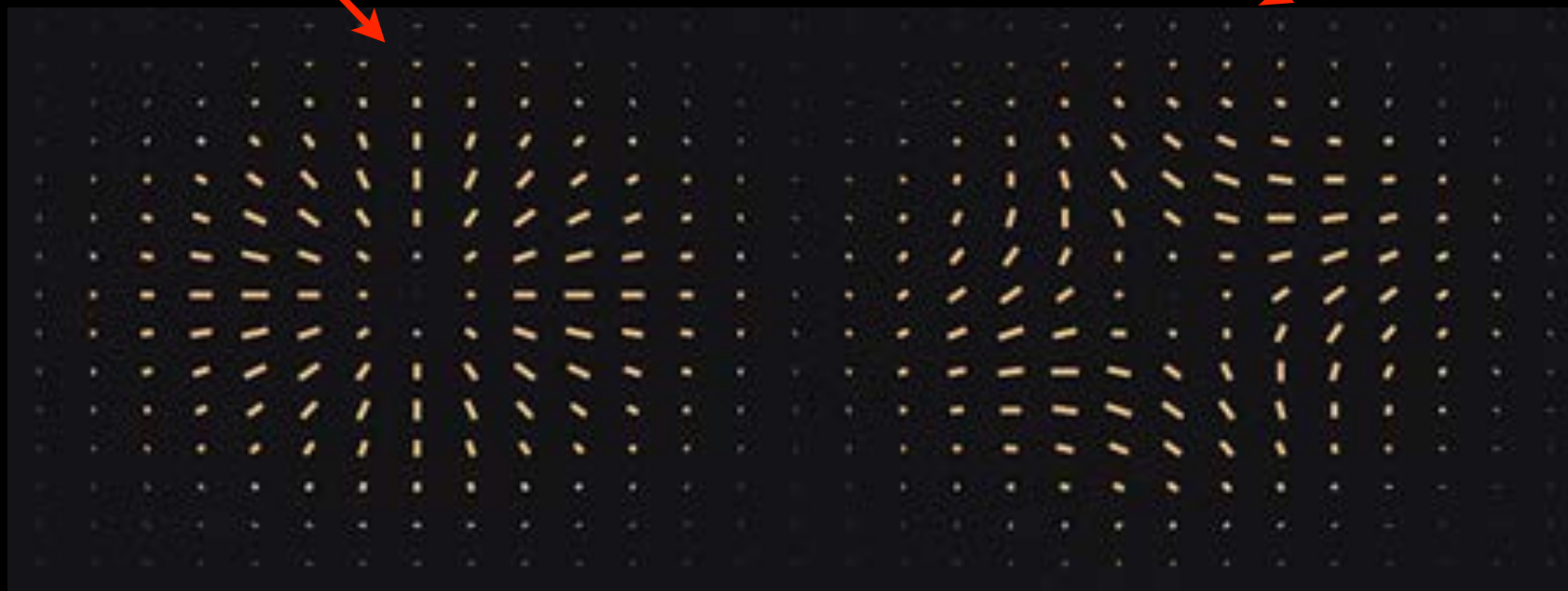
Cores! (Hu/Gruzinov/Barkana 2001, see also Marsh and Silk 2013, Marsh and Pop 2015, Matos 2012, Schive 2014, Vogelsberger 2017, and others)

BIREFRINGENCE AND B-MODES

$$\mathcal{L} \sim \frac{a}{f_a} \vec{E} \cdot \vec{B}$$

✳️ Funnels E modes to B modes

(μK^2)



BIREFRINGENCE AND B-MODES

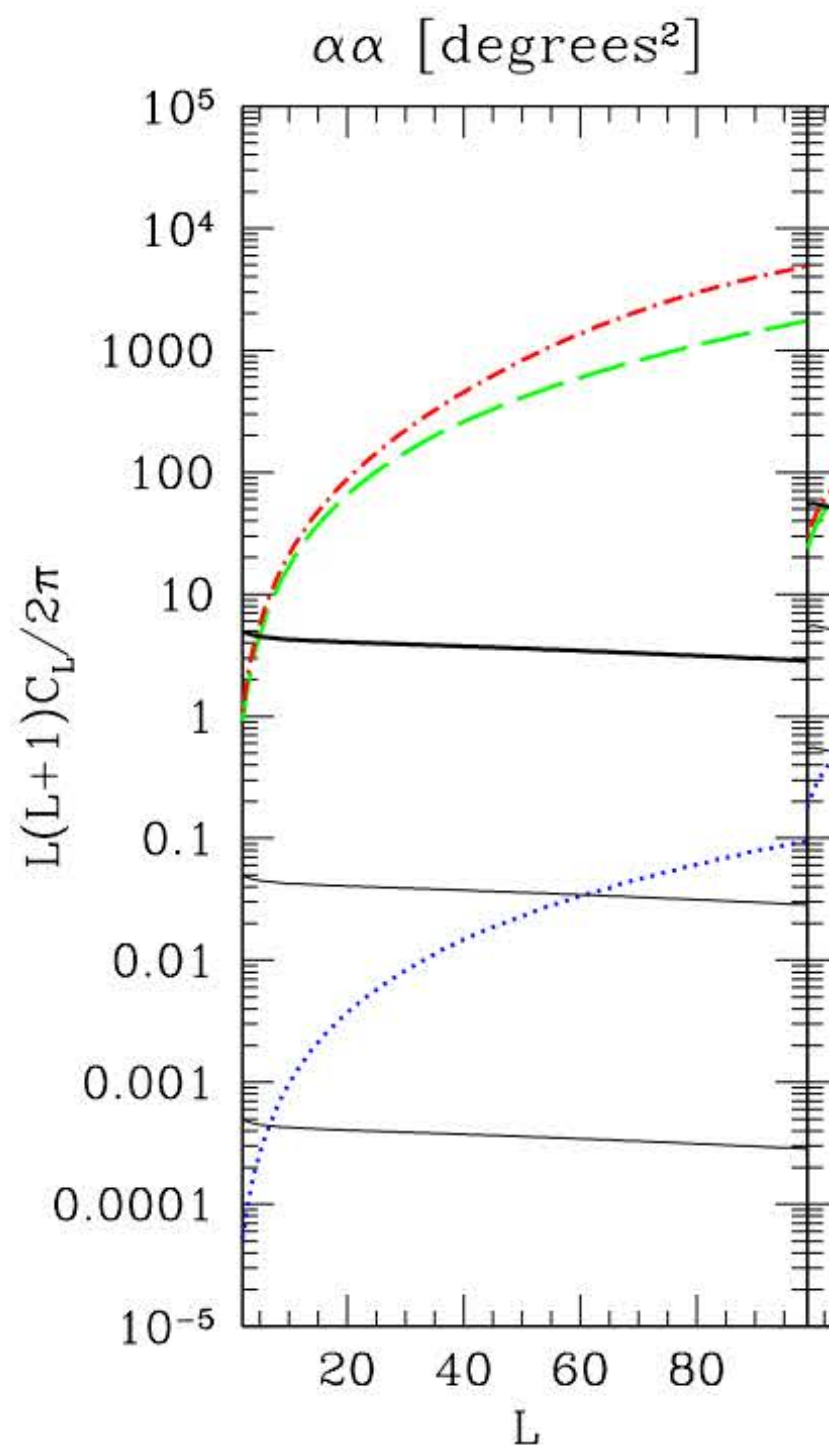
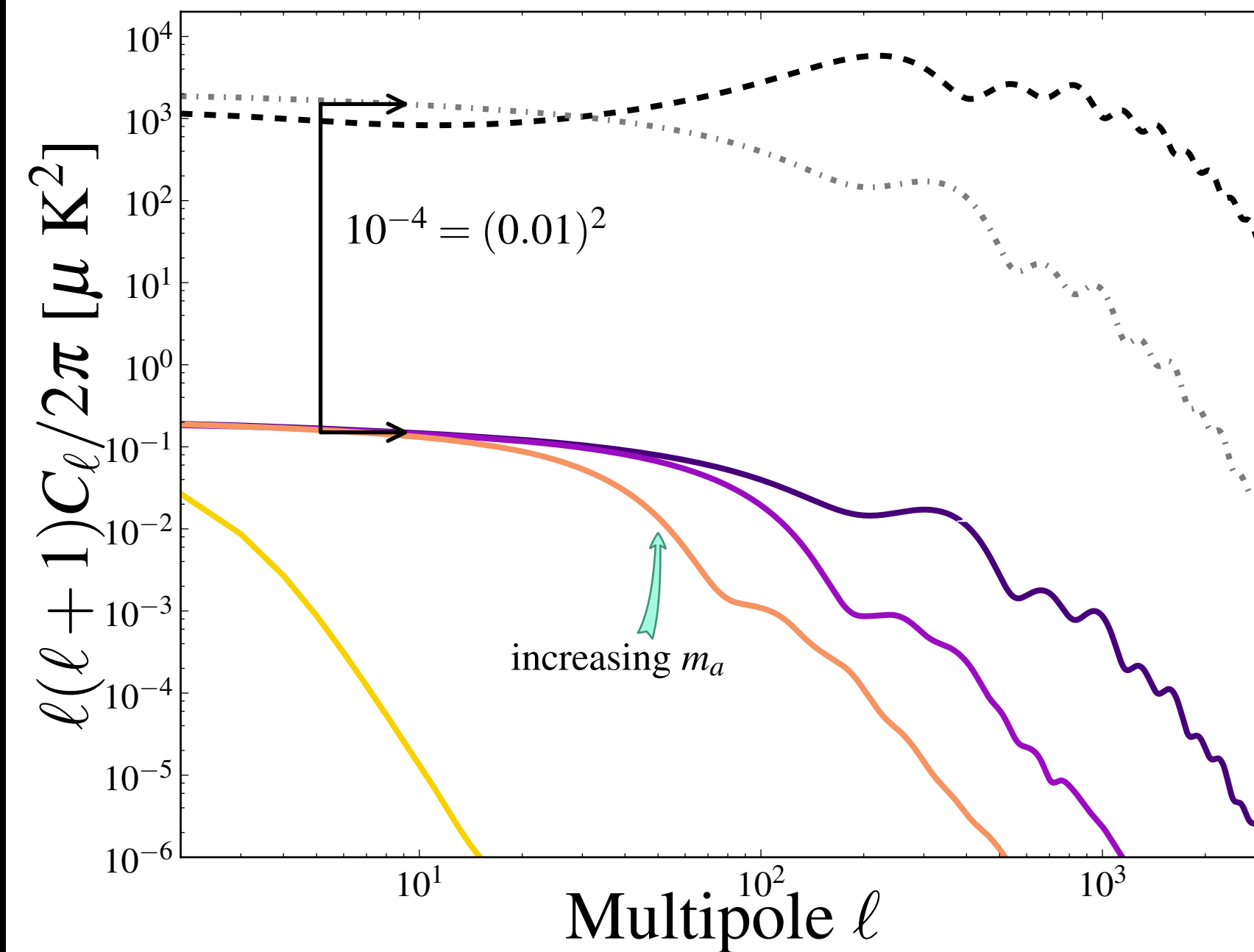


Figure 1: Shown are the power spectra for the cosmological-birefringence rotation angle $C_L^{\alpha\alpha}$ and its cross-correlation with the CMB temperature $C_L^{\alpha T}$ (logarithm of the absolute value), for a generic quintessence model in which the CB-angle fluctuations are due to scalar-field fluctuations at the LSS. The black solid curves are the theoretical prediction for (from top to bottom) $\alpha_4 = 1, 0.1$, and 0.01 , where α_4 is the fluctuation amplitude for the CB angle in units of the maximum currently allowed amplitude [12]. We also show the noise power spectra anticipated for SPIDER (red, dot-dashed), Planck (green, dashed), and CMBPol (blue, dotted).

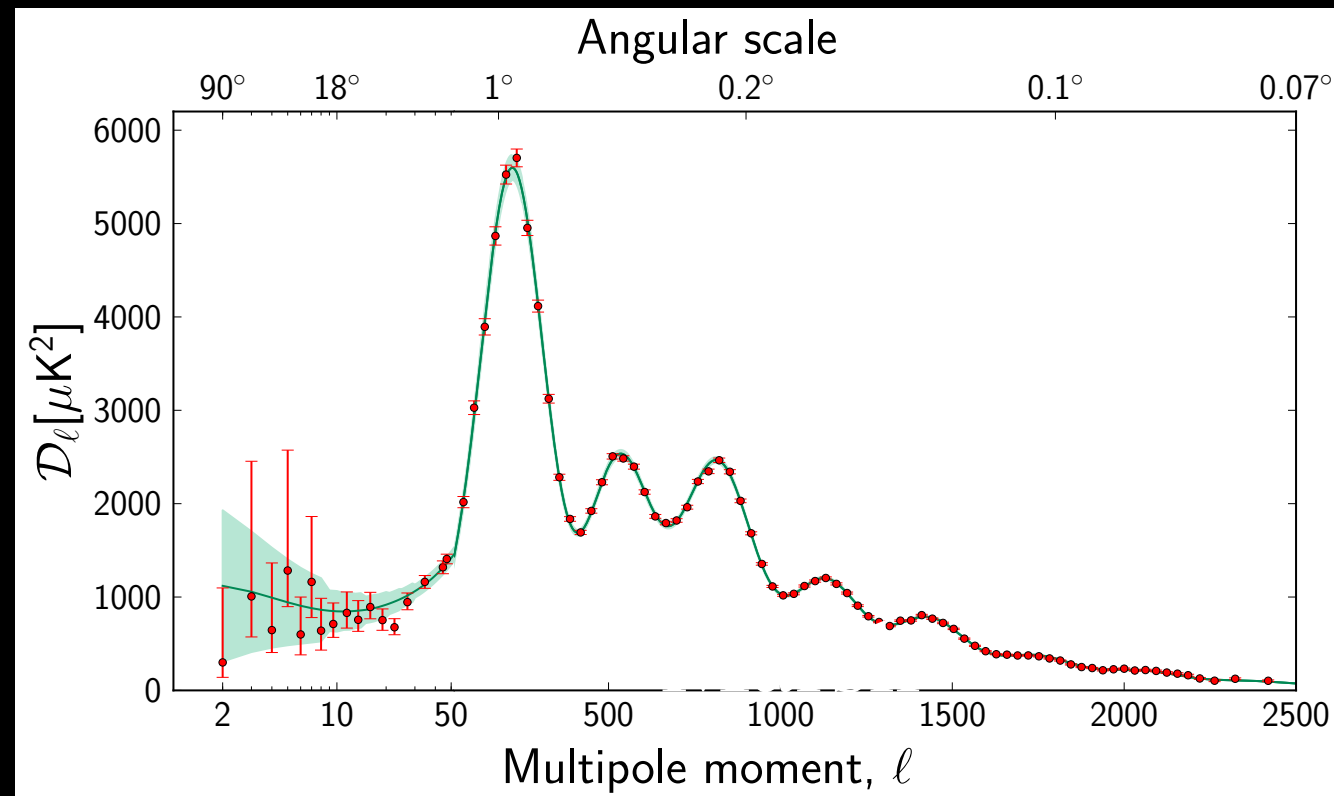
ULAS AND ISOCURVATURE FLUCTUATIONS



$$\begin{aligned} m_a &= 10^{-32} \text{ eV} \\ m_a &= 10^{-29} \text{ eV} \\ m_a &= 10^{-28} \text{ eV} \\ m_a &= 10^{-20} \text{ eV} \end{aligned}$$

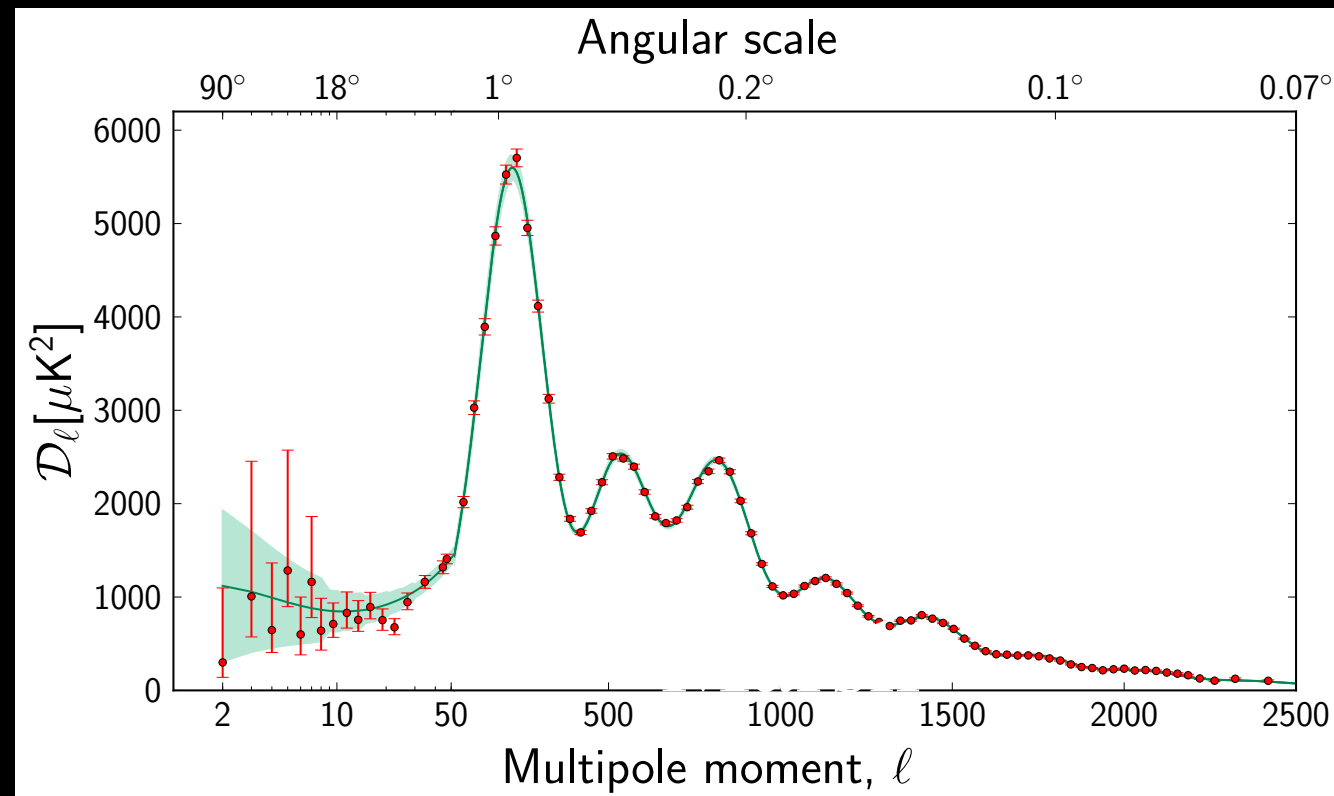
Spectra from AXICAMB using initial conditions obtained in DG+ (2015 in prep)

Planck 2013 TT



$$\alpha \equiv \frac{P_{S_{c\gamma}}(k)}{P_{S_{c\gamma}}(k) + P_{\mathcal{R}}(k)} \leq 0.039$$

Planck 2013 TT



QCD axion

$$\frac{\Omega_a}{\Omega_a + \Omega_c} \lesssim 10^{-12} \left(\frac{10^{14} \text{GeV}}{H_I} \right)^{7/2}$$

ULAs

$$\frac{\Omega_a}{\Omega_a + \Omega_c} \lesssim 10^{-3} \left(\frac{10^{14} \text{GeV}}{H_I} \right)$$

D.J.E. Marsh, DG +, arXiv:1403.4216, Phys. Rev. Lett. 113, 011801

D.J.E. Marsh, DG +, arXiv:1303.3008, Phys. Rev. D 87, 121701(R)

AXION ISOCURVATURE AS AN INFLATIONARY PROBE

* Discovery of QCD axion/ULA dark matter —————> trouble for

* GUT-scale inflation $H_I \sim 10^{14}$ GeV

QCD
axion

$H_I \sim 10$ GeV

ULA

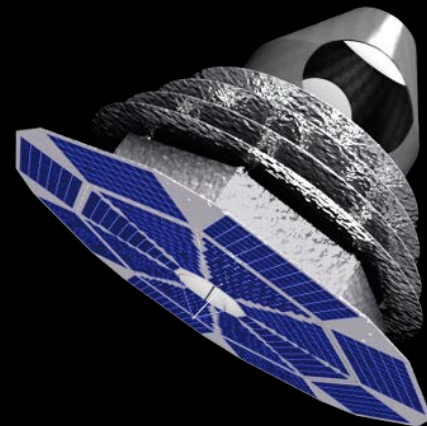
$H_I \sim 10^5$ GeV

* Null prediction for primordial B-mode searches

SPT/BICEP2-3/KECK/CMB-S4



Spider

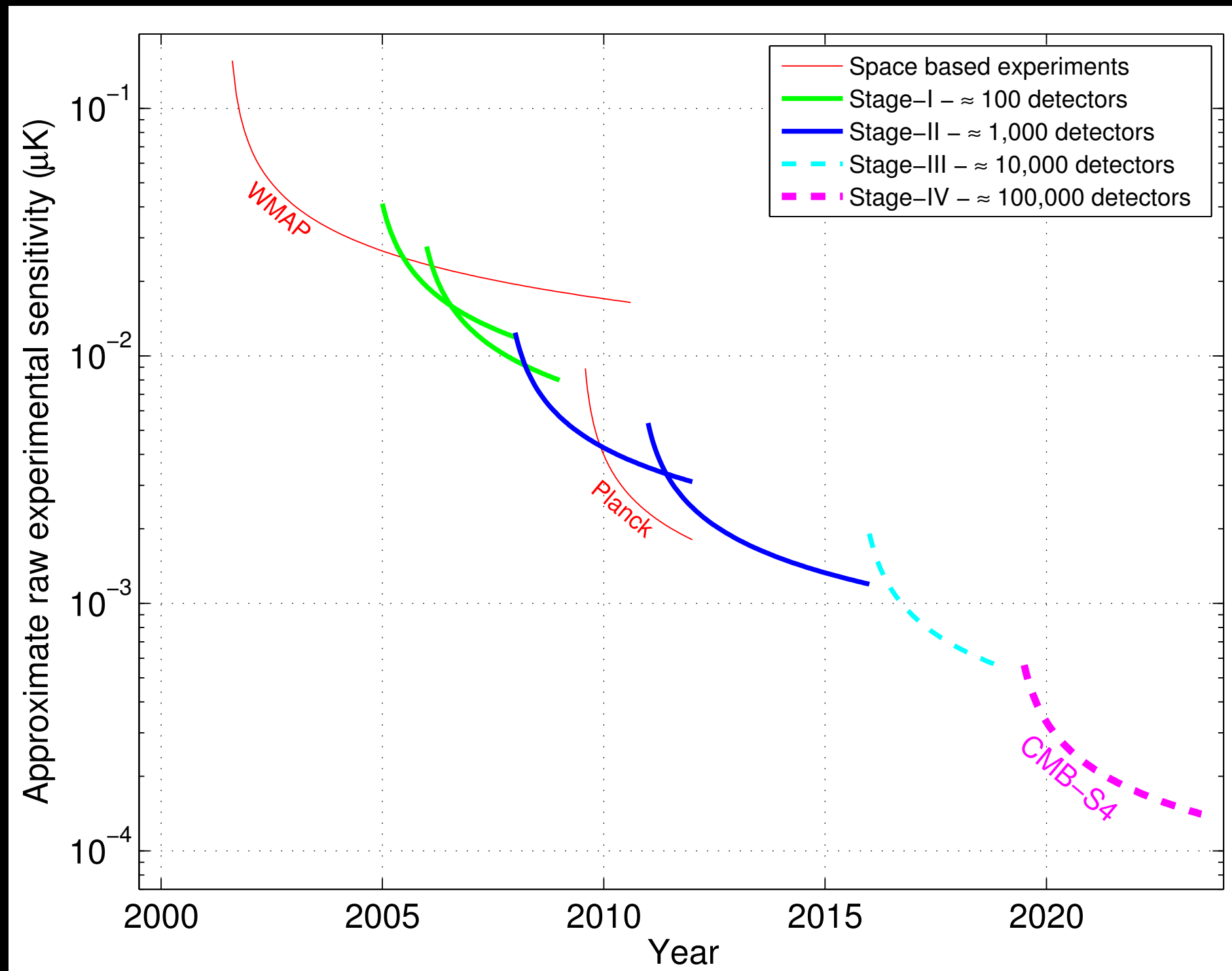


CORE

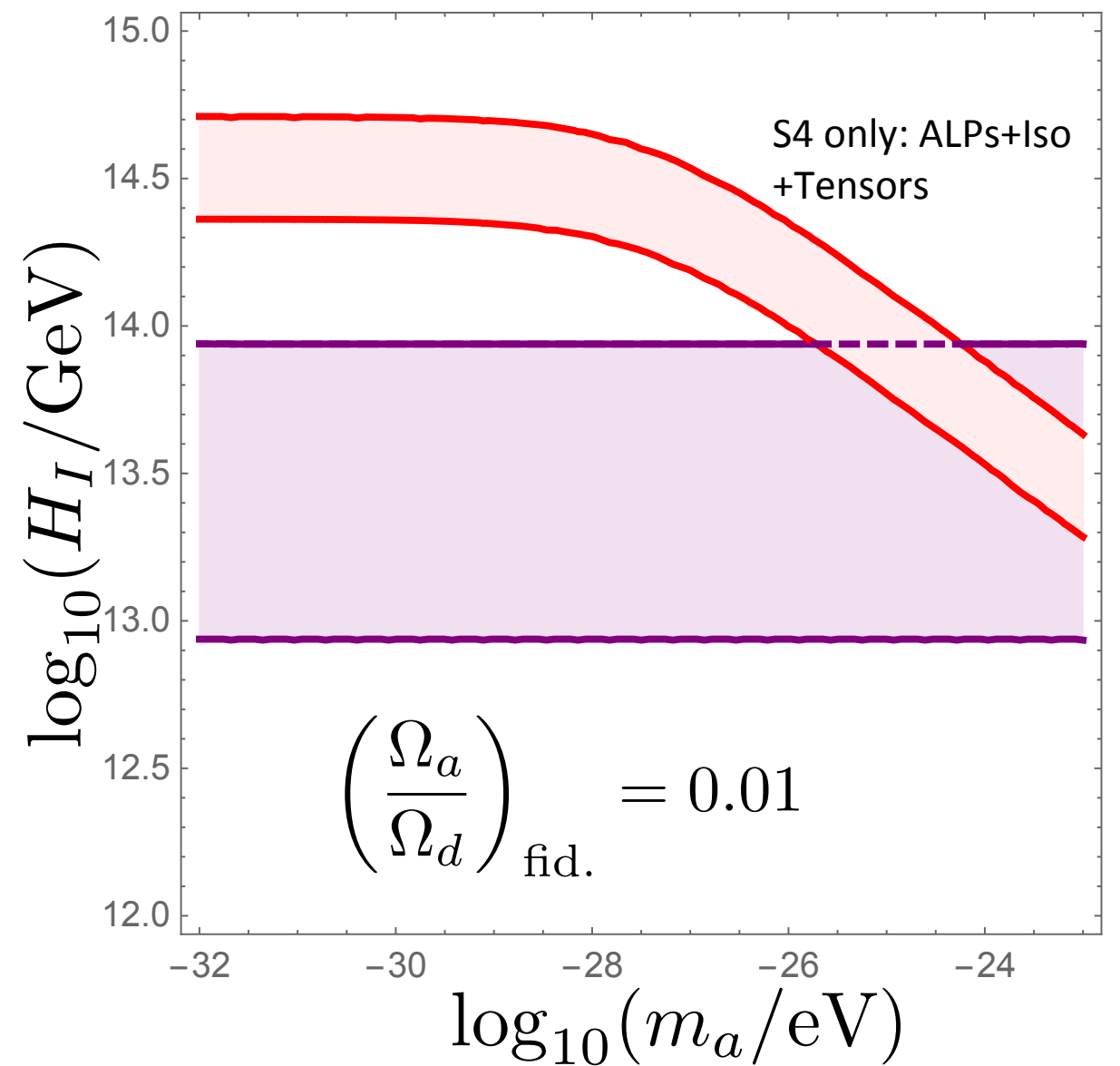
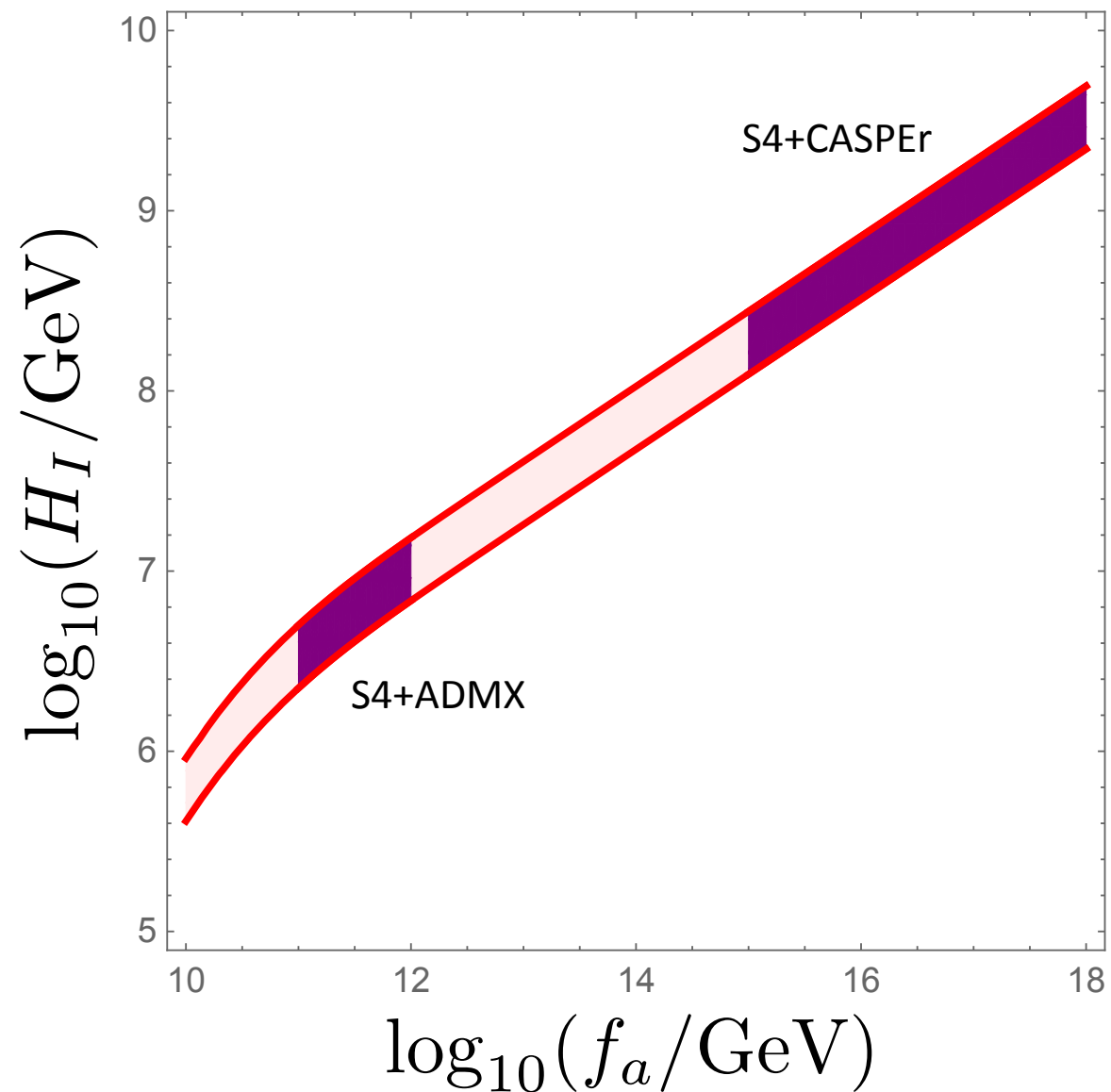


* Avoidable with non-trivial thermal history/richer PQ symmetry breaking story

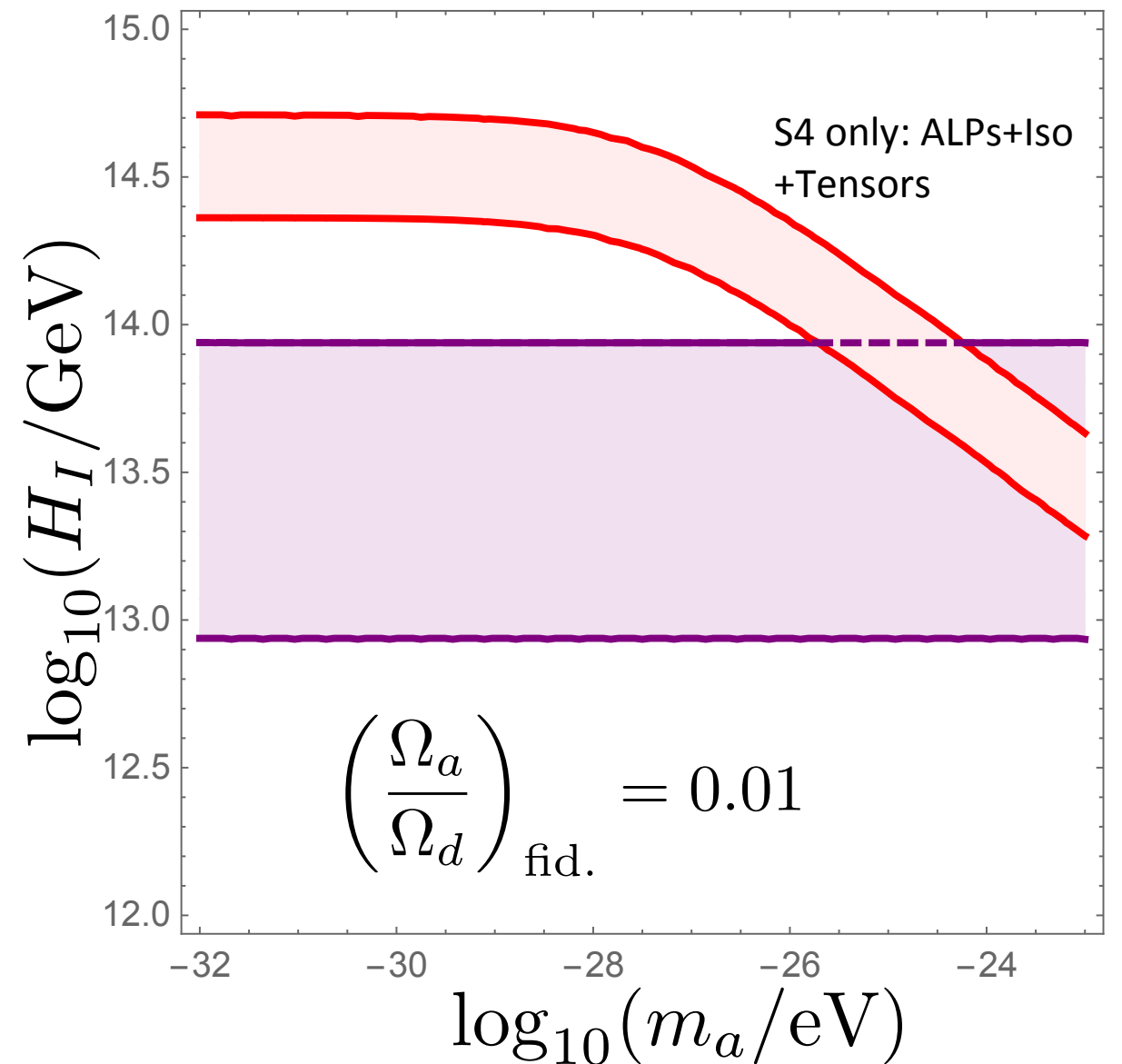
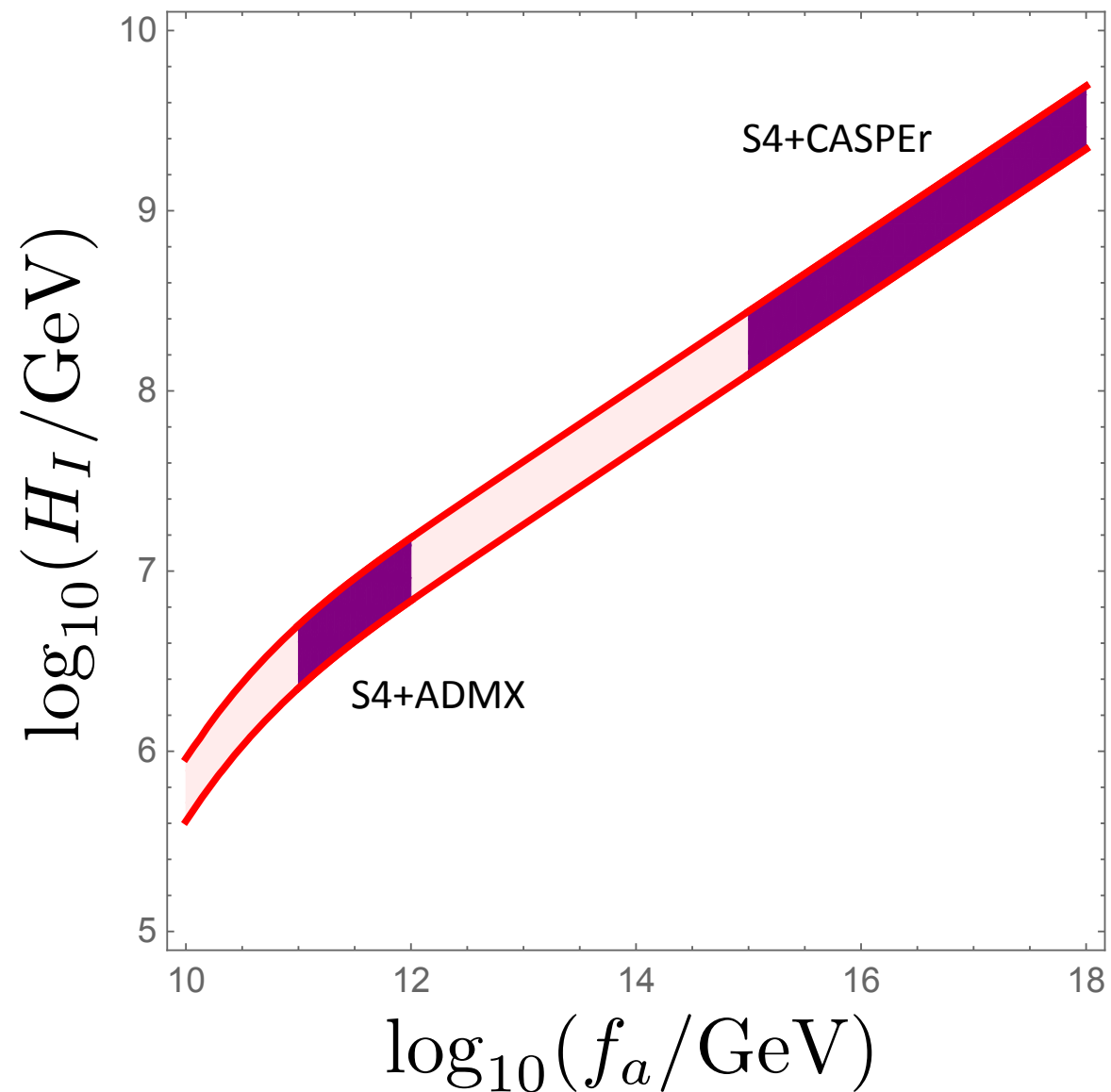
AXION ISOCURVATURE AS AN INFLATIONARY PROBE



HIGH-ENERGY COSMOLOGY WITH AXION ISOCURVATURE



HIGH-ENERGY COSMOLOGY WITH AXION ISOCURVATURE

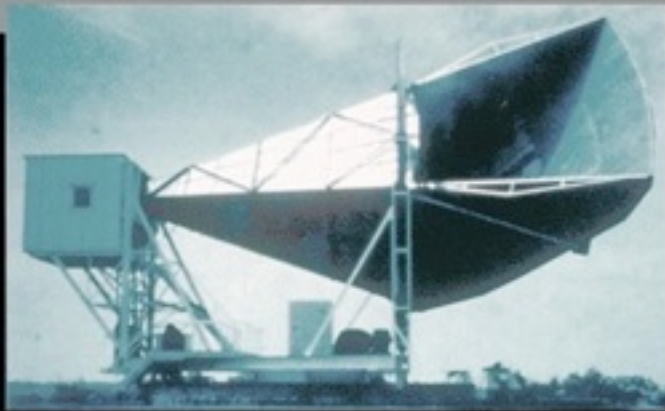


From forthcoming CMB-S4 Science book....

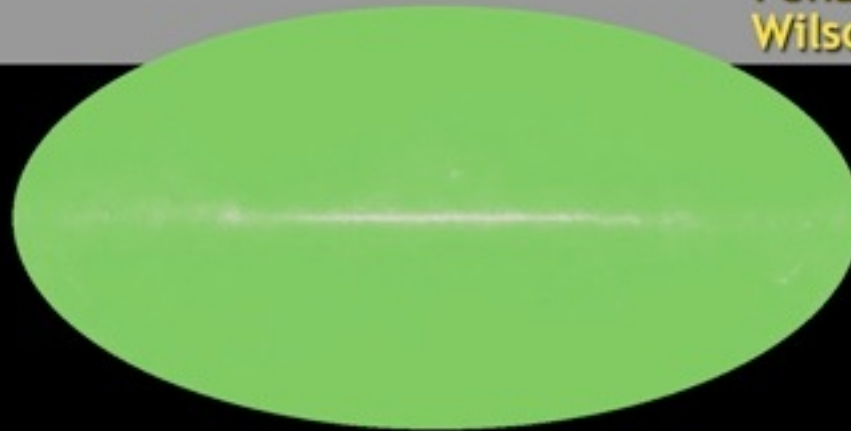
Backup slides

COSMIC MICROWAVE BACKGROUND (CMB): EXPERIMENTAL PROGRESS

1965



Penzias and
Wilson

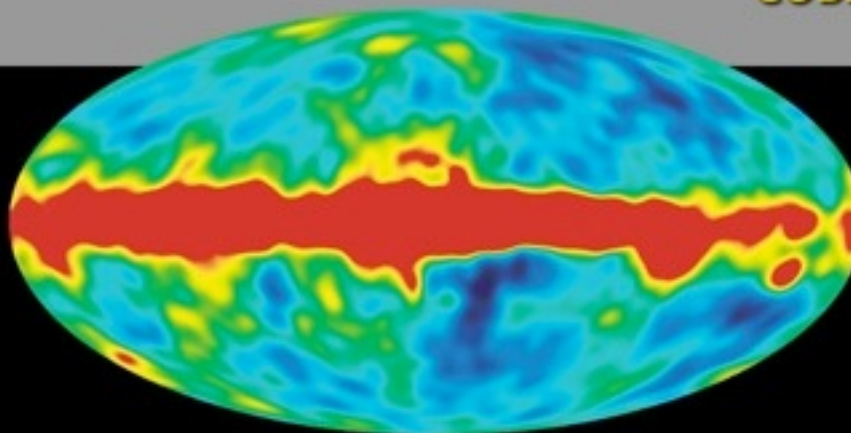


*A uniform glow outside the
Galactic Plane:
 $T = 2.7$ Kelvin*

1992



COBE

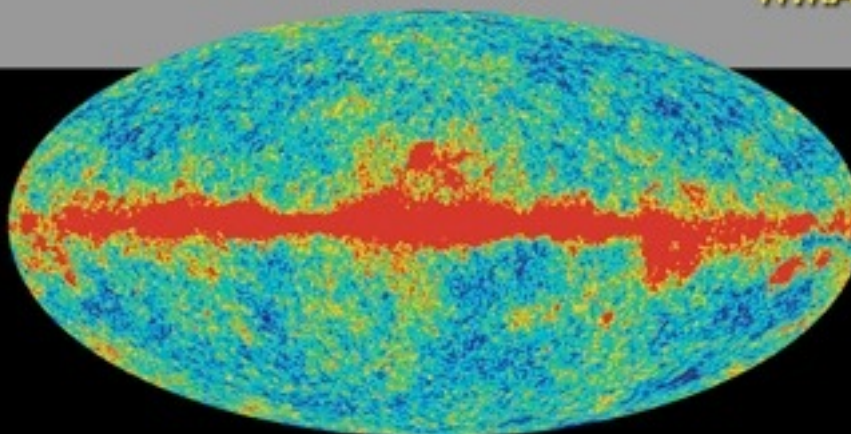


*First detection of
fluctuations:
one part in 100,000*

2003

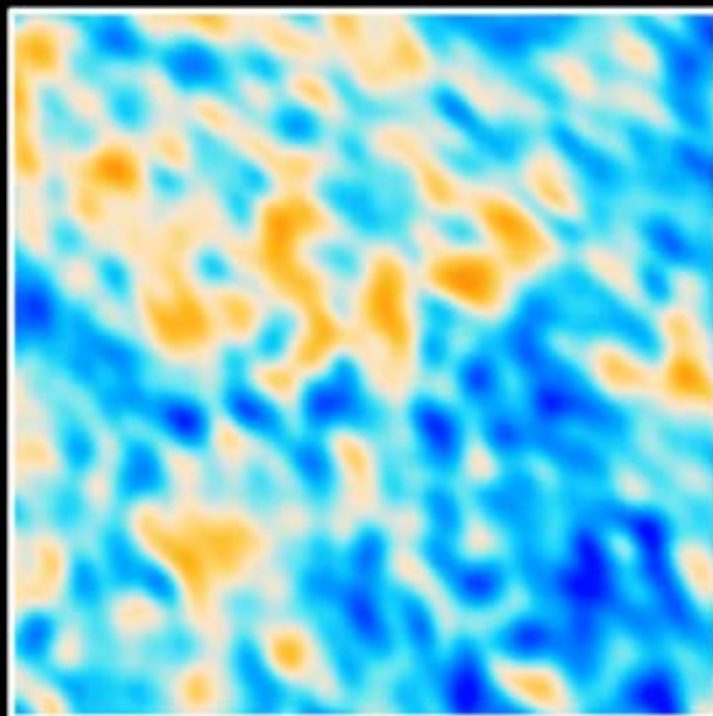
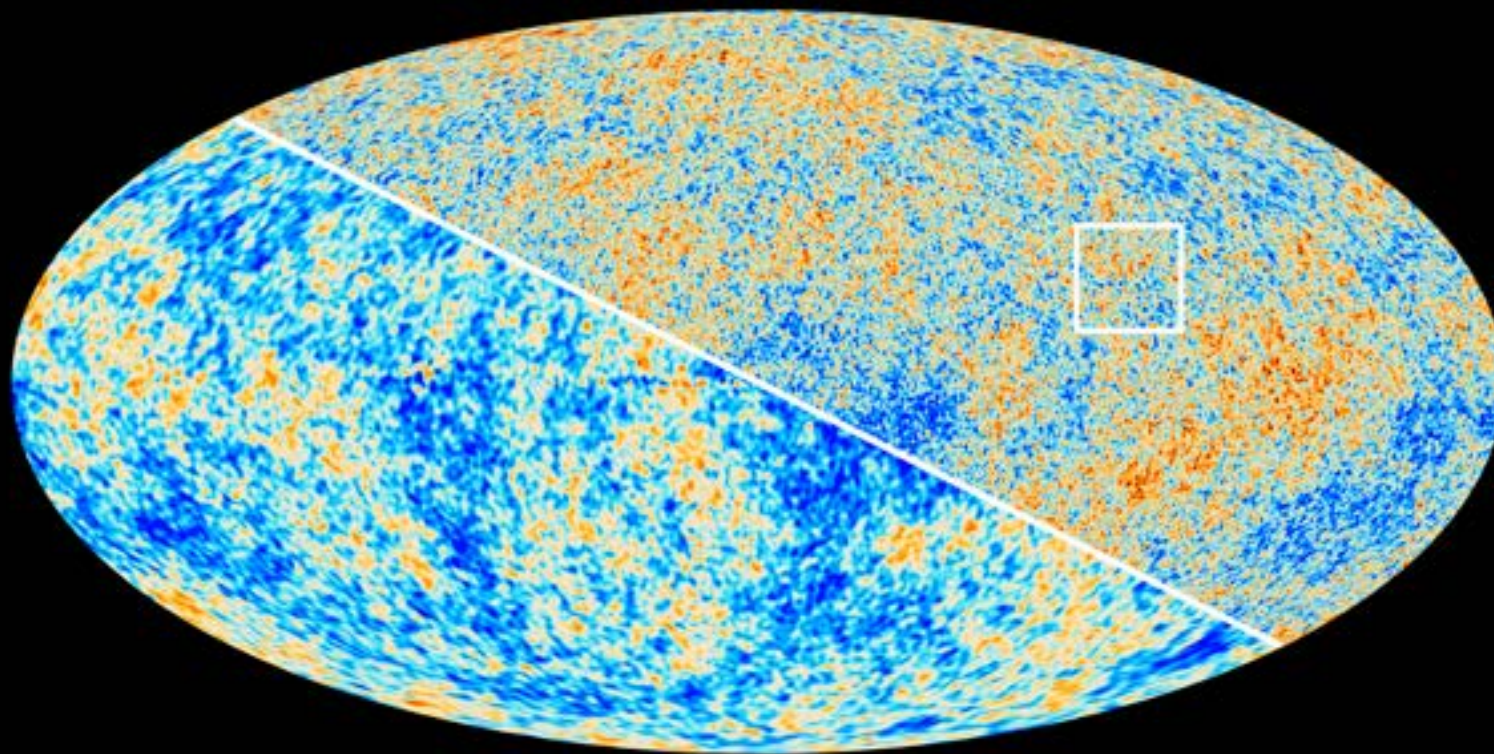


WMAP

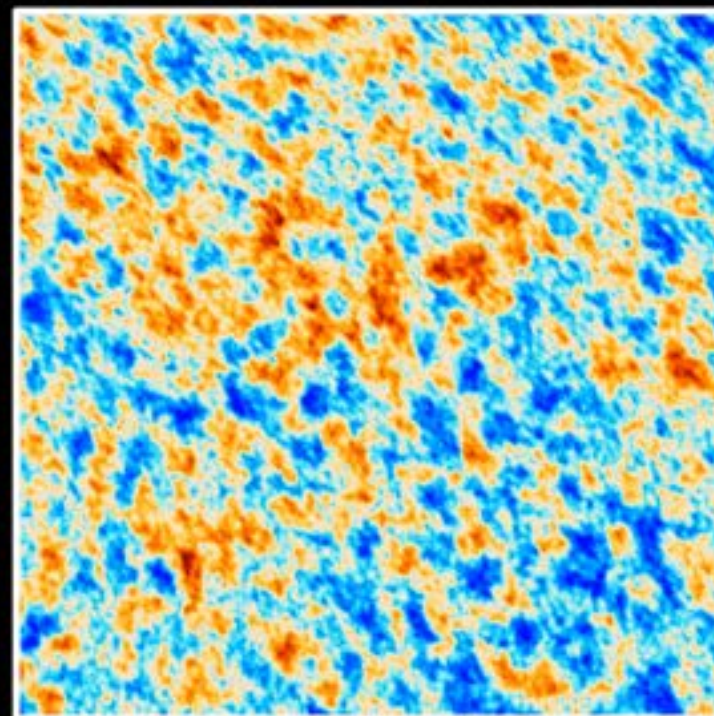


COSMIC MICROWAVE BACKGROUND (CMB): EXPERIMENTAL PROGRESS

The Cosmic Microwave Background as seen by Planck and WMAP

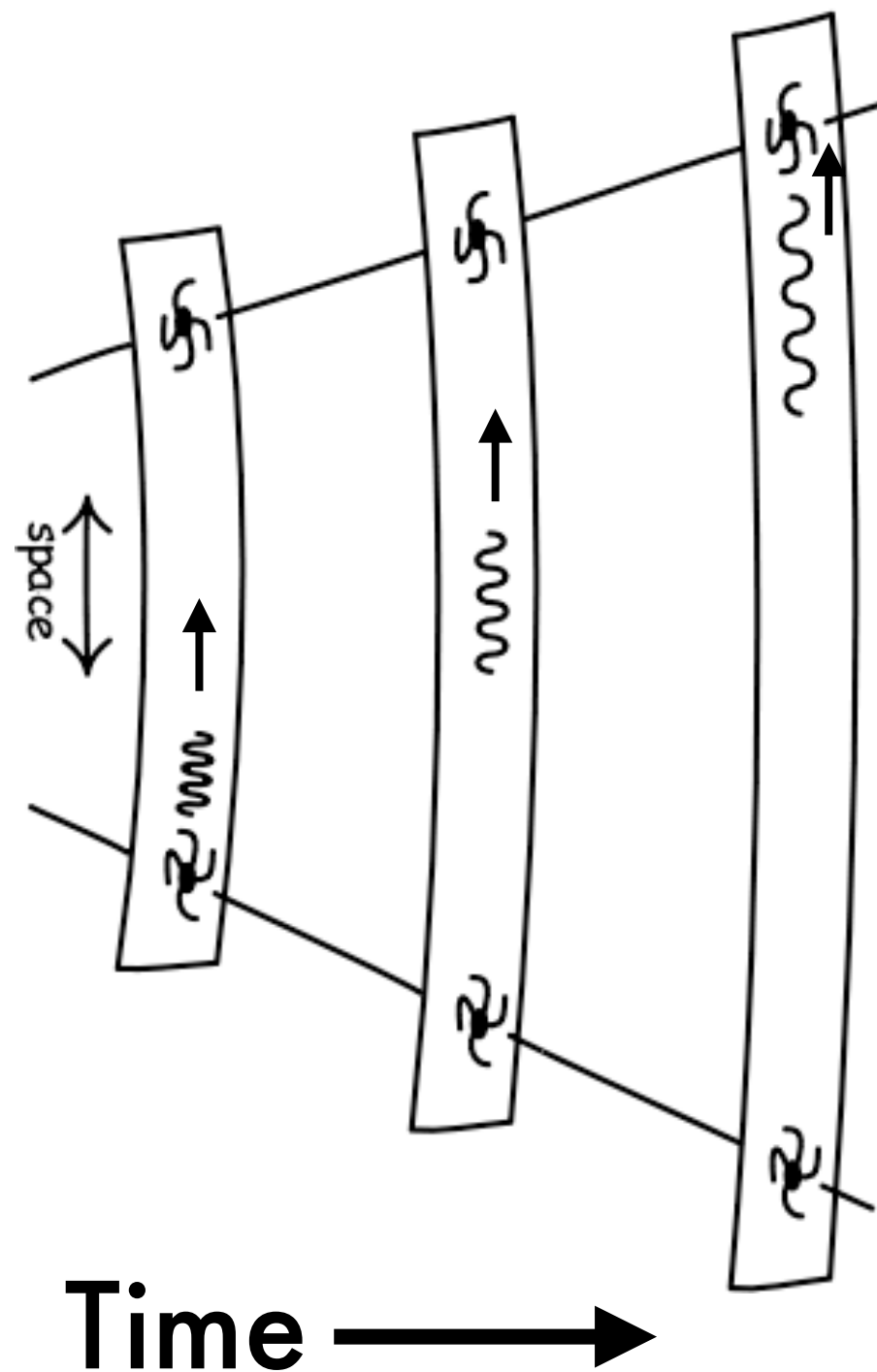


WMAP

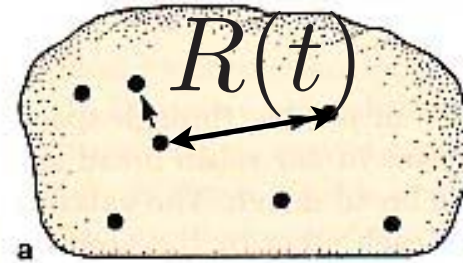


Planck

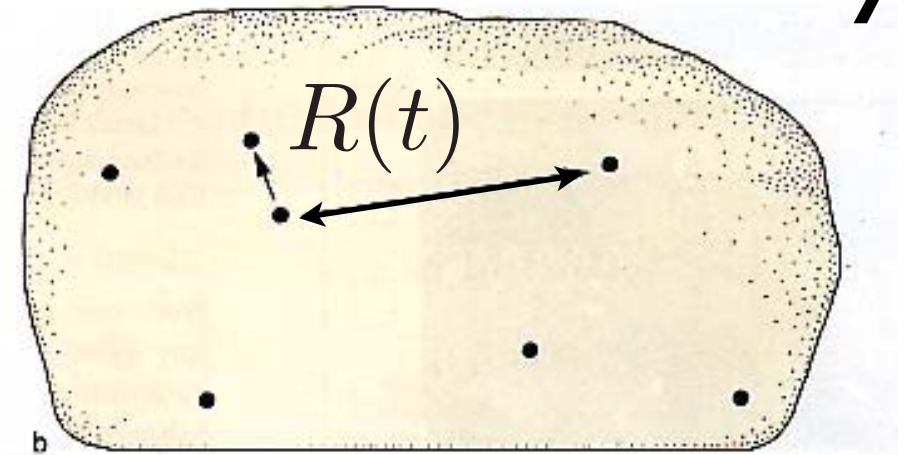
THE EXPANDING UNIVERSE



Past



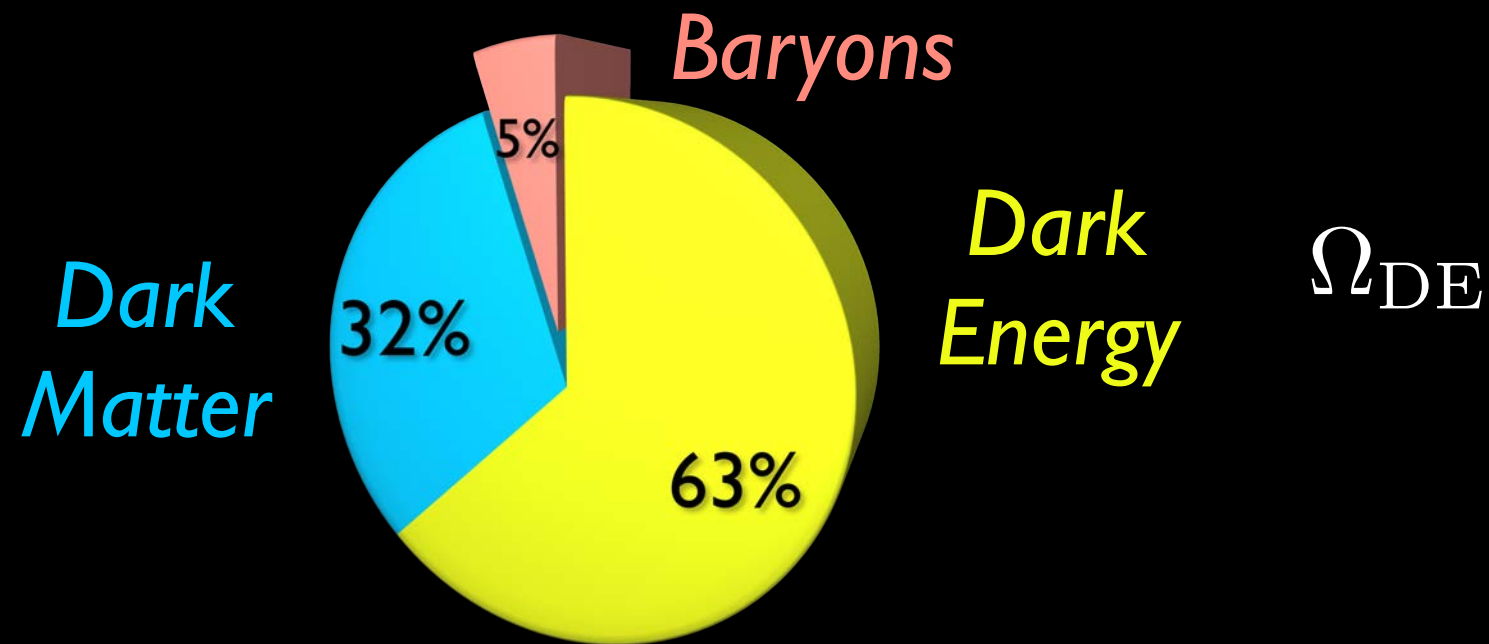
Today



With expansion

$$z = \frac{\lambda_{\text{observed}}}{\lambda_{\text{emitted}}} - 1$$

COSMIC ENERGY BUDGET



5% baryonic matter: protons, electrons, atoms

*“stuff we know”

32% cold dark matter (CDM)

*Stable, neutral, non-relativistic particle

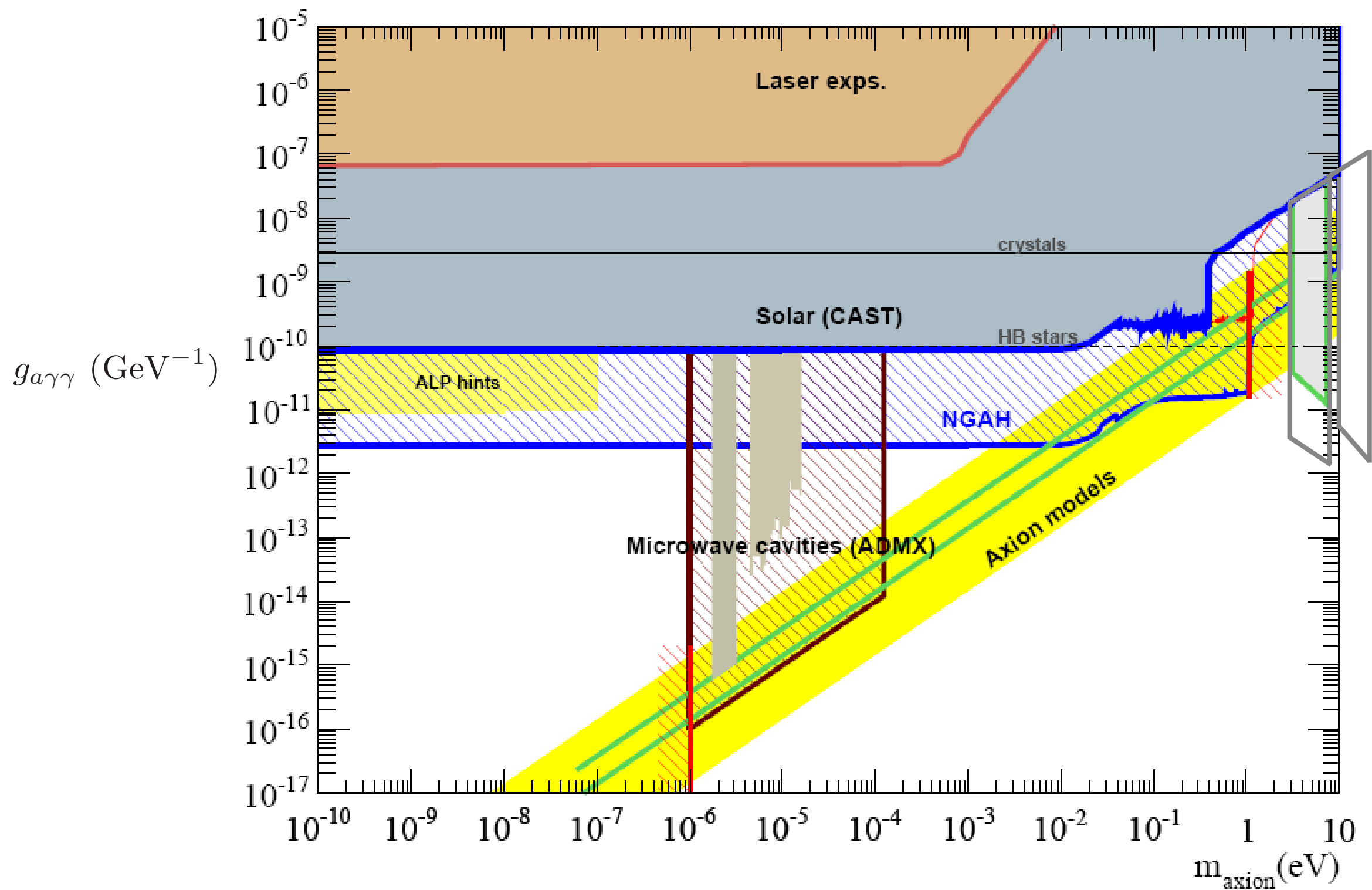
*Weak interactions with standard model

63% dark energy

Stuff we don't know!

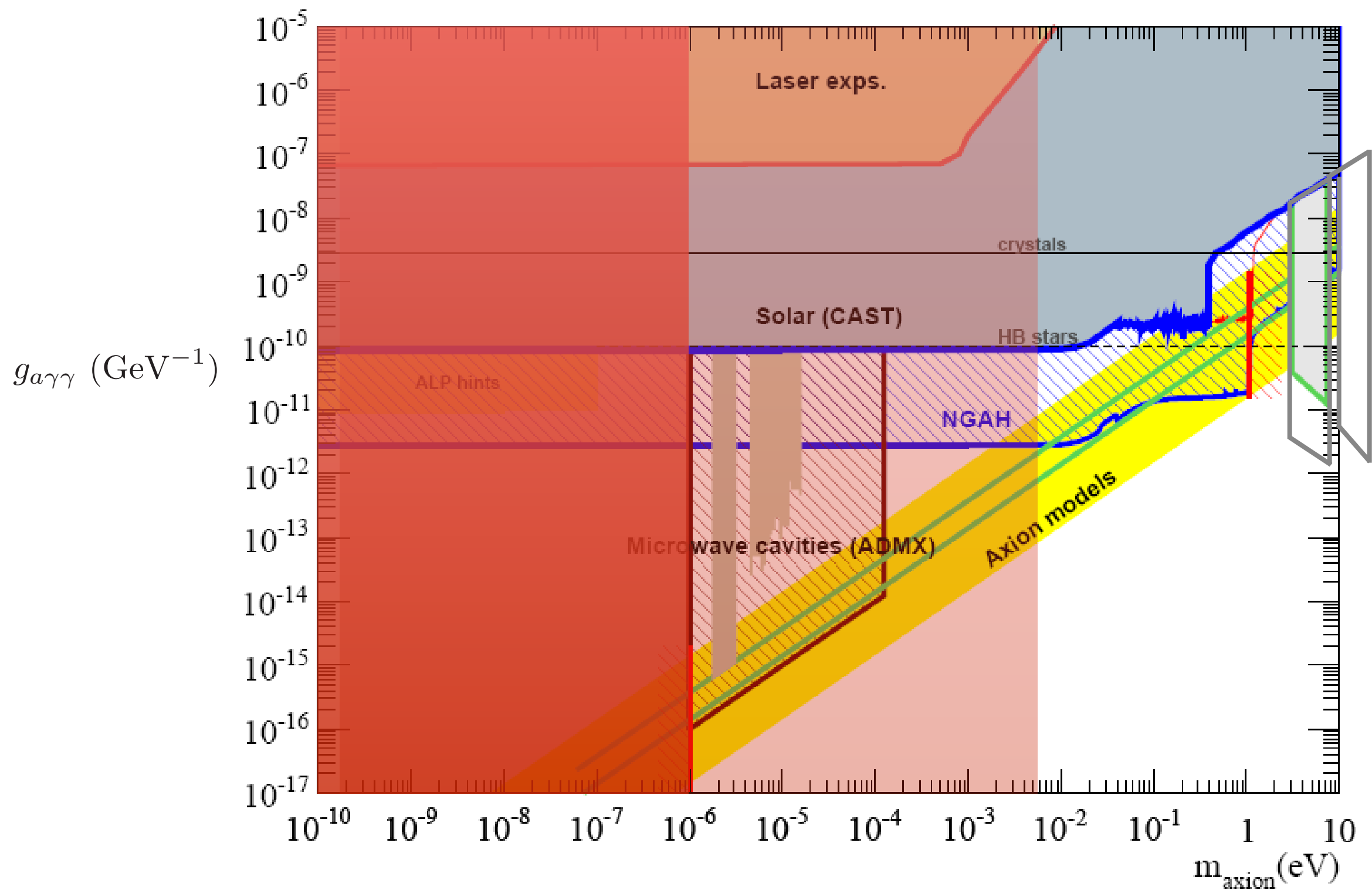
Axion Fundamentals

LIMITS



LIMITS

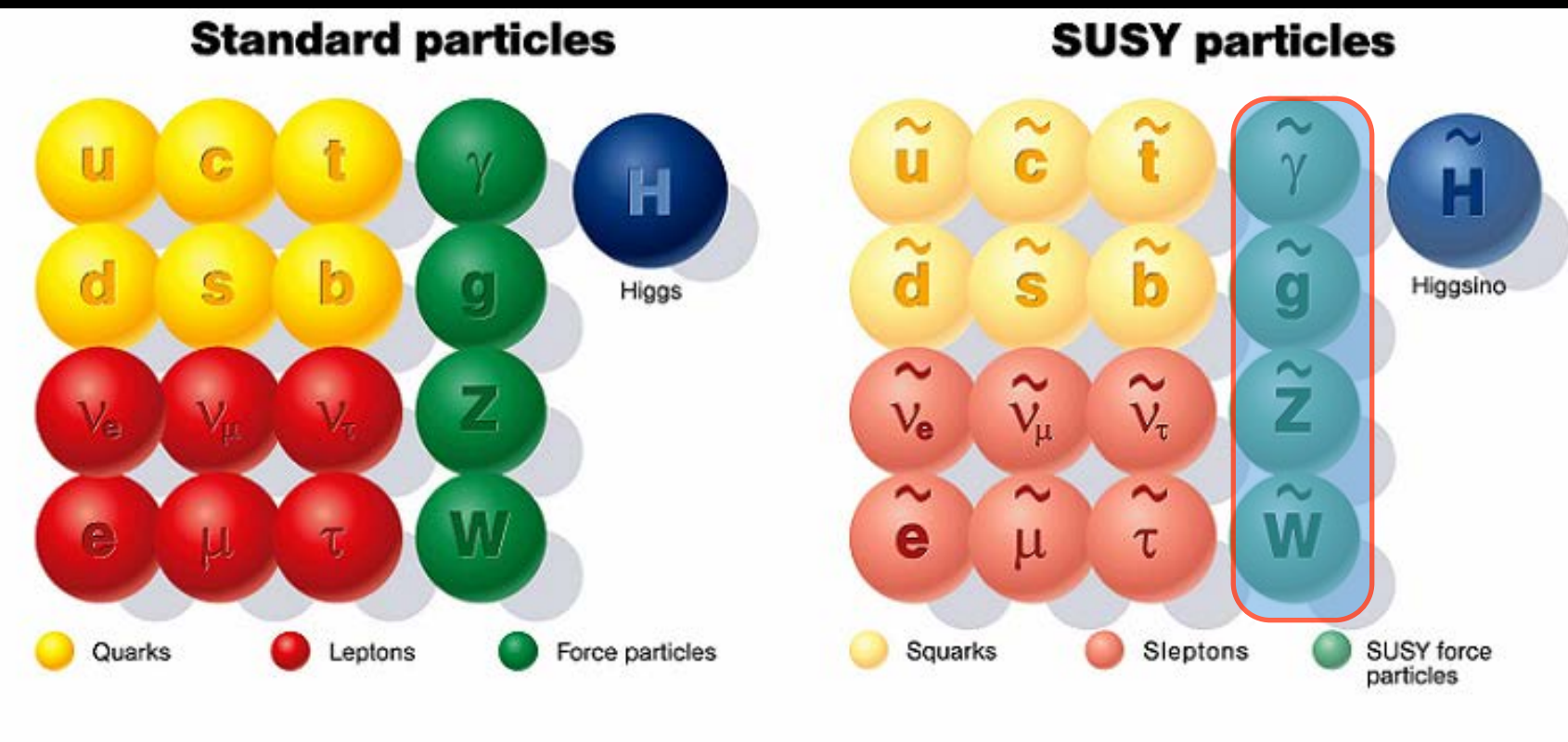
Cosmological dark matter



SUPERSYMMETRY THEORY

✴Solves many of SM's problems!

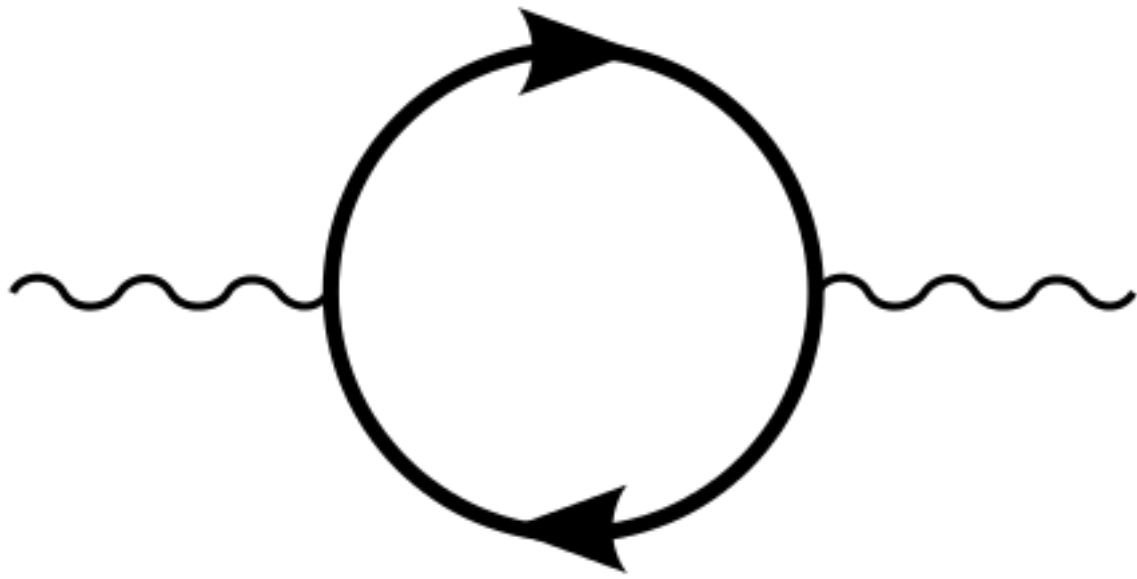
Dark matter?



✴Heavy! $m_{\text{dark matter}} \sim 10^2 \text{ GeV}$ vs $m_{\text{proton}} \sim 1 \text{ GeV}$

✴Correct dark-matter abundance! 32% of cosmic mean density

DARK ENERGY: SM VACUUM ENERGY?



Crudely:

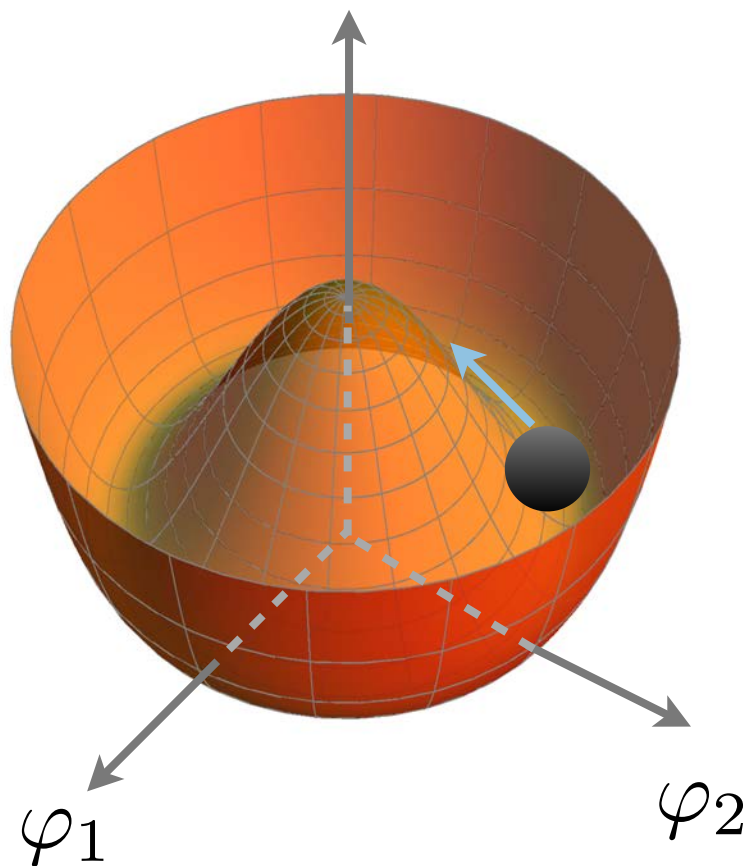
$$\Delta E \sim \frac{\hbar}{\Delta t}$$

Full standard model vacuum energy predicts....

$$\Omega_{\Lambda} \sim 10^{120} \quad \text{vs} \quad \Omega_{\Lambda} \simeq 0.63$$

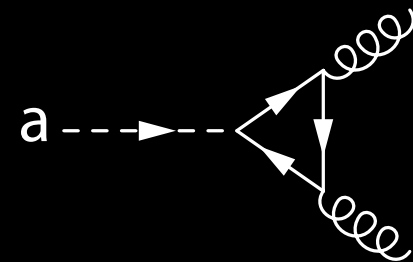
This is what you call a colossal failure

WHAT ARE AXIONS?



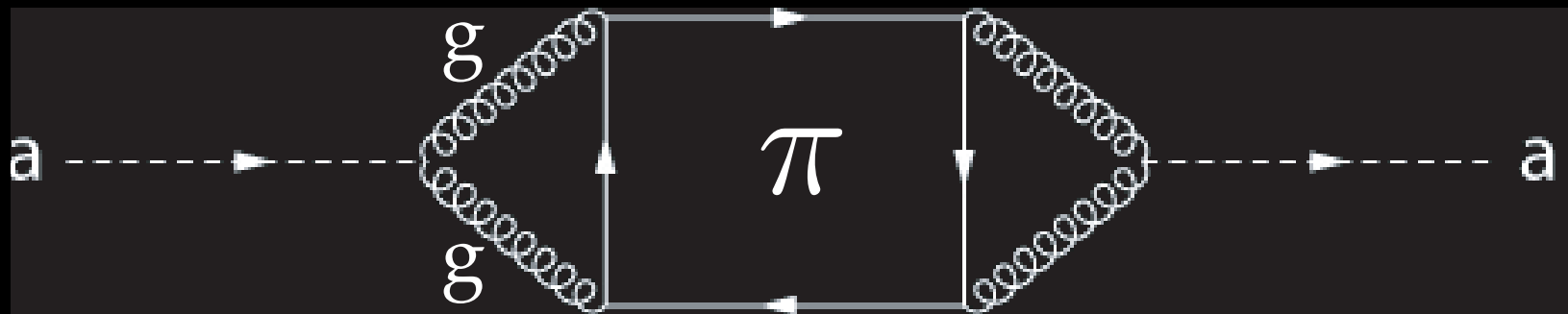
New scalar field with global U(1) symmetry!

$$\mathcal{L}_{\text{CPV}} = \frac{\theta g^2}{32\pi^2} G\tilde{G} - \frac{a}{f_a} g^2 G\tilde{G}$$



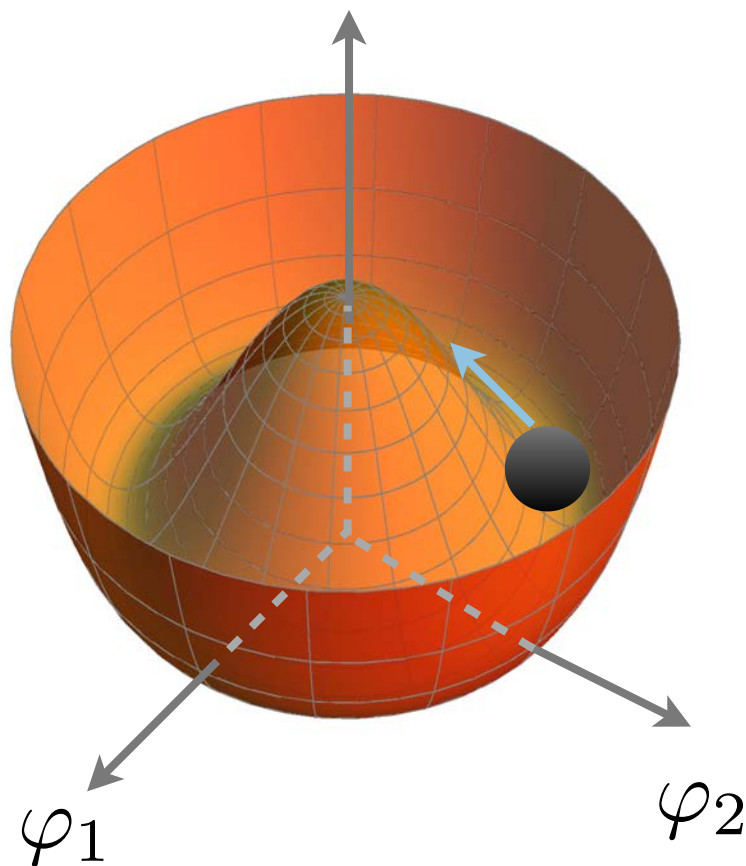
- * Couples to SM gauge fields (via fermions)
- * Dynamically erases QCD CP-violation

* Mass through pion mixing

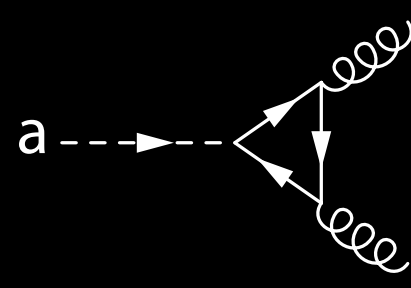


Peccei + Quinn (1977), Weinberg +Wilczek (1978), Kim (1979), Shifman et. al (1980), Zhitnitsky (1980), Dine et al. (1981), D.B. Kaplan (1985), A.E Nelson (1985,1990)

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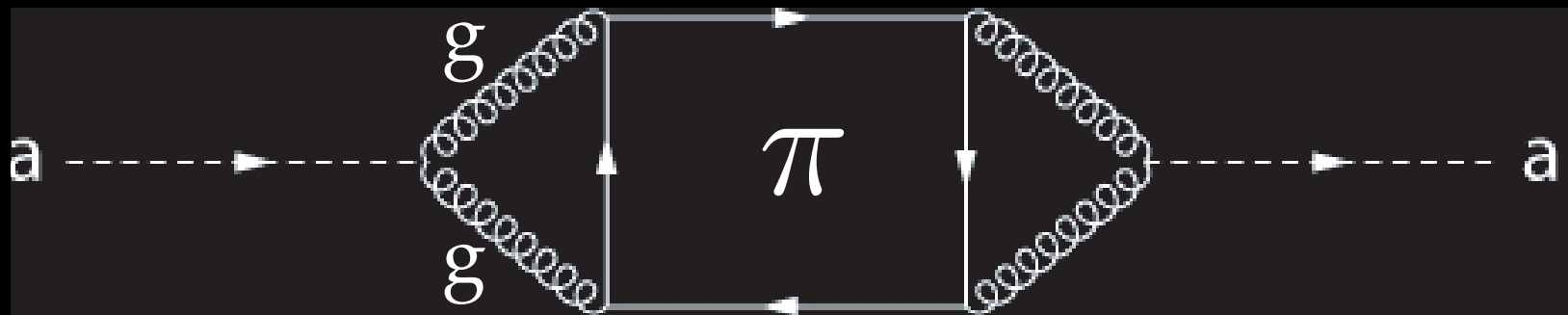


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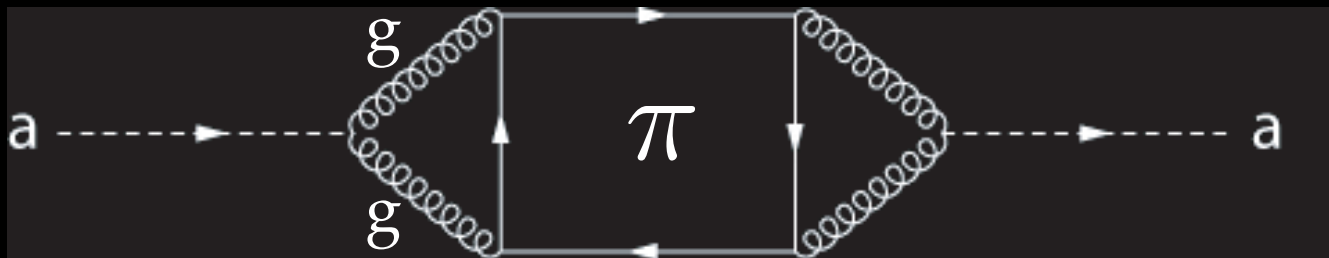
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- ✴ New field (axion) and U(1) symmetry dynamically drive net CP-violating term to 0

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- ✴ Through coupling to pions, axions pick up a mass



$$m_a \simeq \frac{\Lambda_{\text{QCD}}^2}{f_a}$$

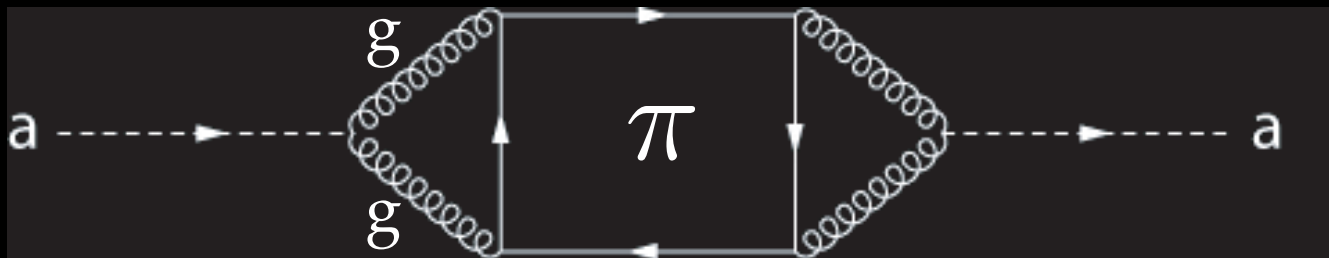
$$\Lambda_{\text{QCD}} \simeq 200 \text{ MeV}$$

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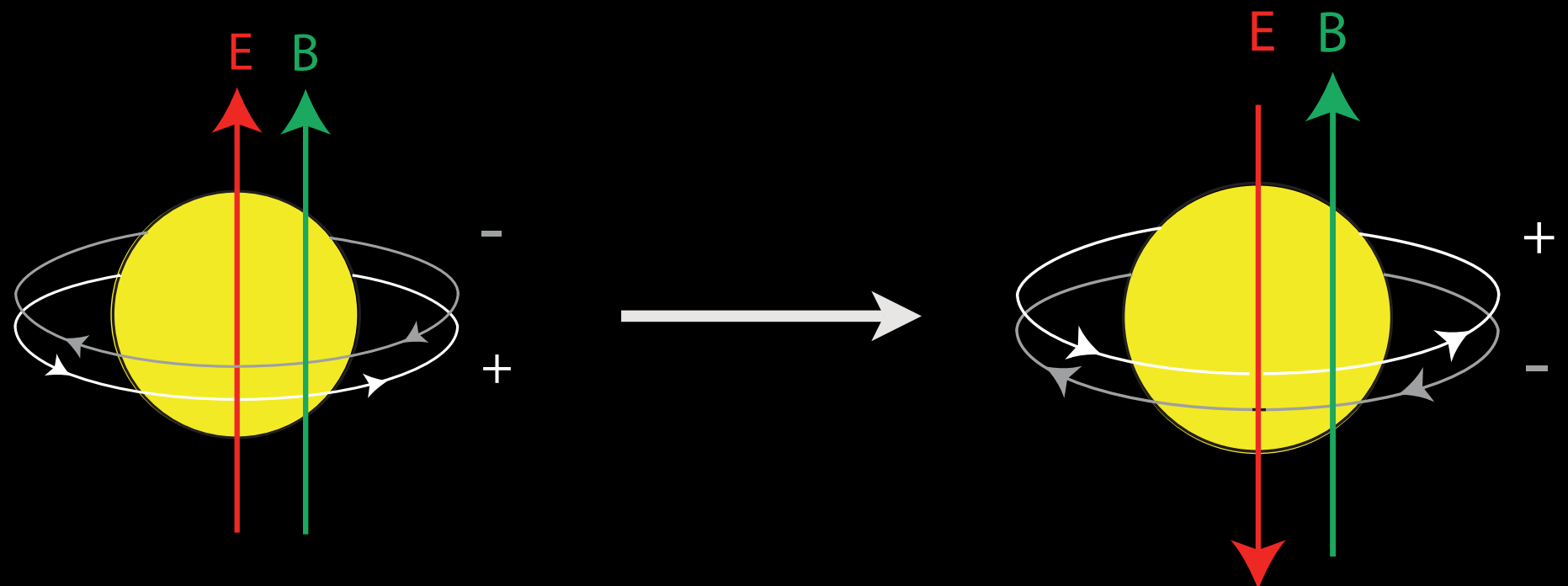
STRONG CP PROBLEM

- * Strong interaction violates CP through θ -vacuum term

QCD strong-CP problem $\mathcal{L}_{\text{CPV}} = \frac{\theta g^2}{32\pi^2} G\tilde{G}$

- * Limits on the neutron electric dipole moment are strong. Fine tuning?

$$d_n \simeq 10^{-16} \theta \text{ e cm}$$
$$\theta \lesssim 10^{-10},$$



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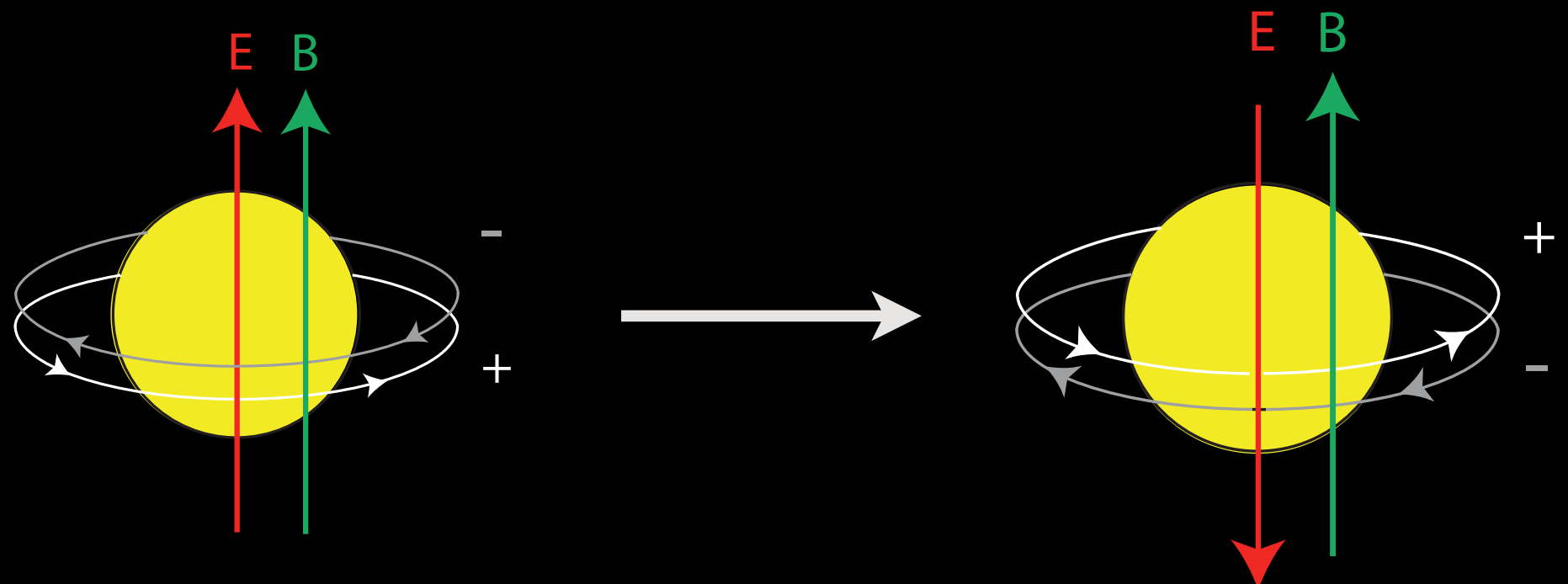
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KEY QUESTIONS:

- * *Can the dark matter or dark energy be an ultra-light boson, like an axion?*
- * What is the connection between the physics of inflation and the physics of the dark sector? Are initial fluctuations in different species spatially locked?
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in collaboration with R. Hlořek (Princeton), D. J. E. Marsh (Perimeter Institute), P. Ferreira (Oxford):



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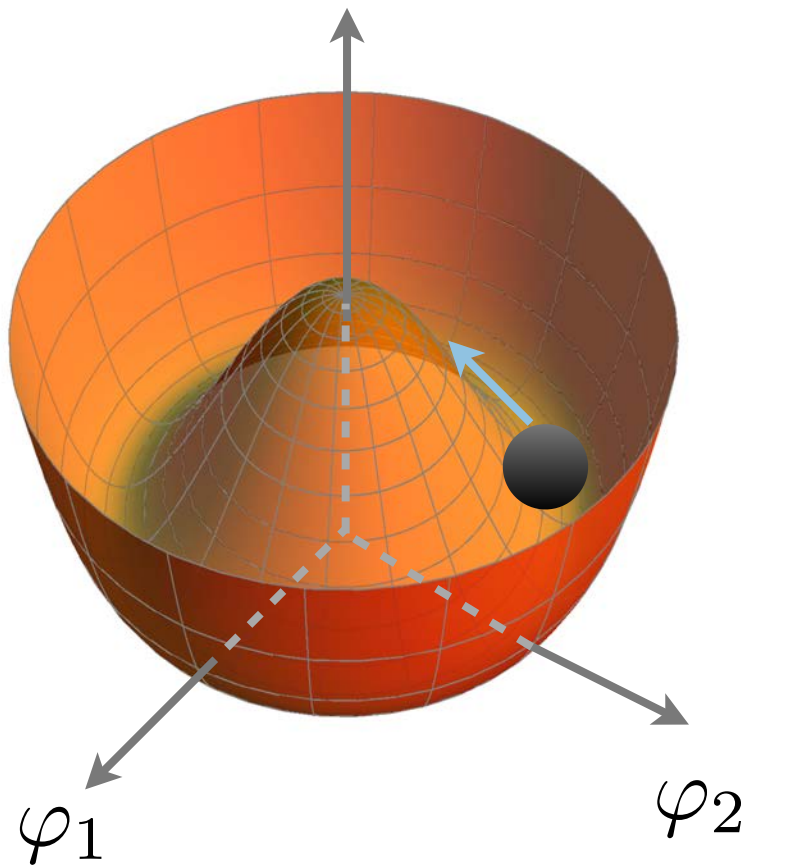
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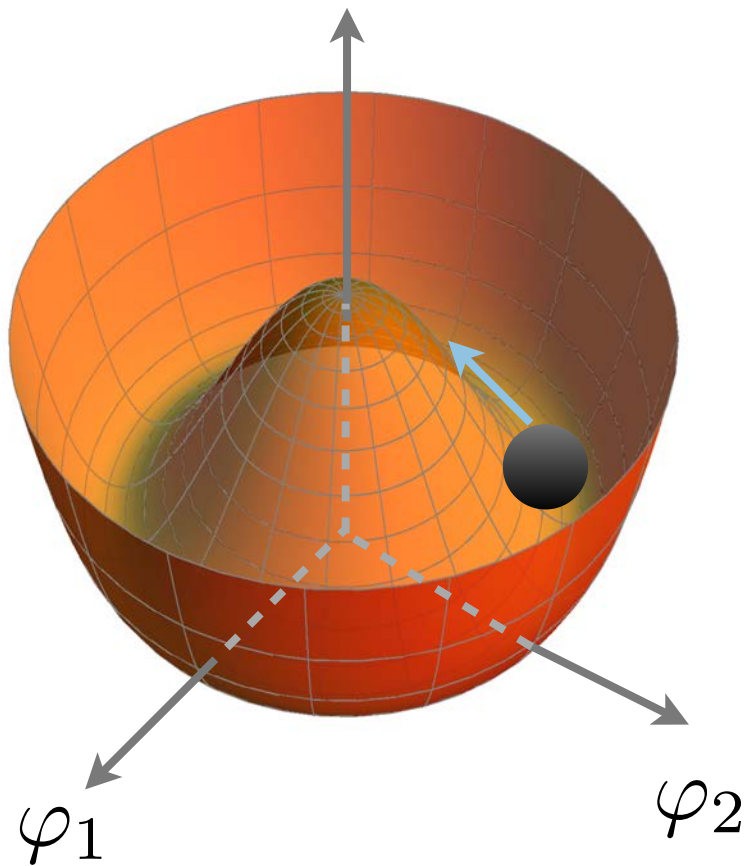
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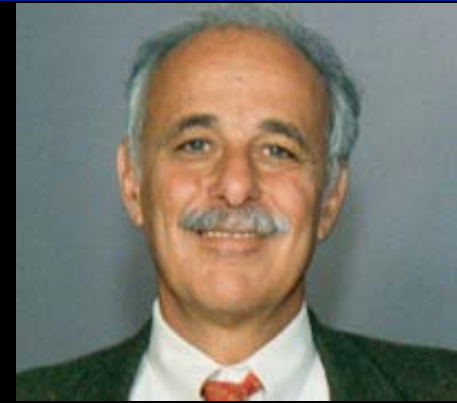
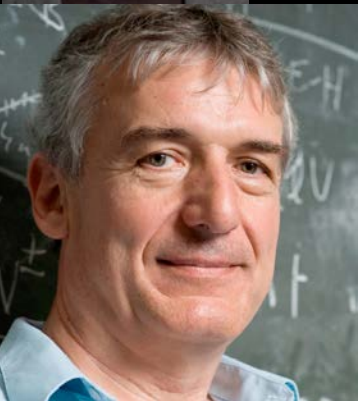
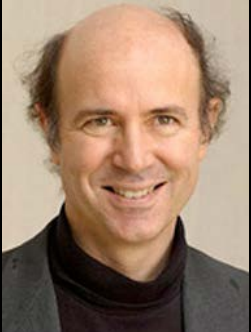


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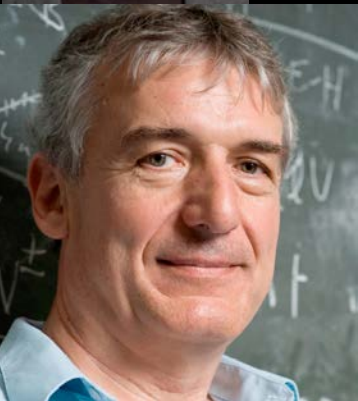
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Cleaning up the dark matter mess?

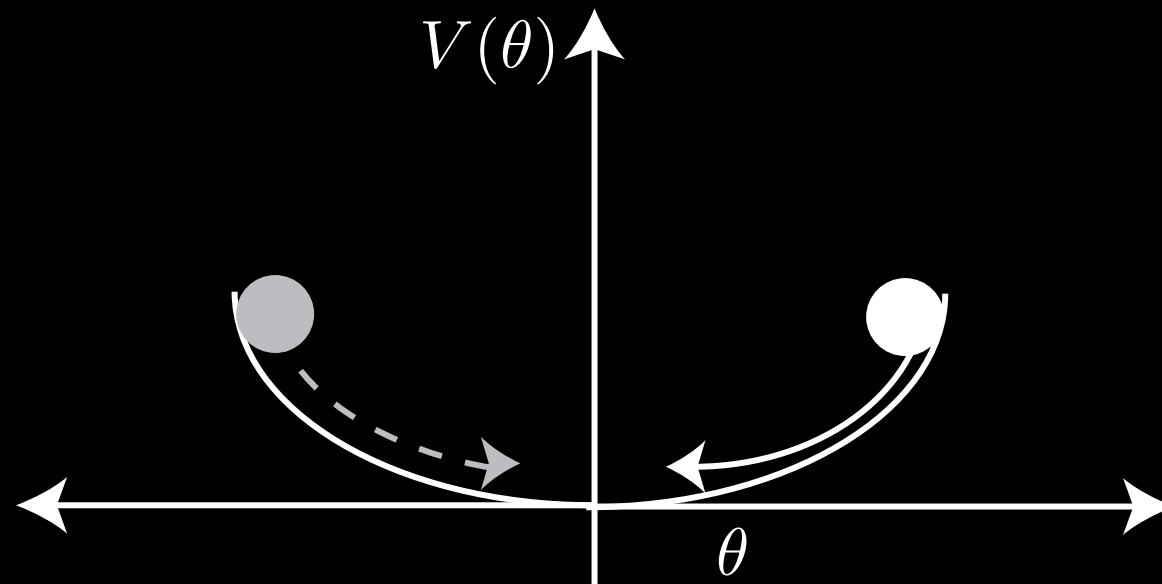


Cleaning up the dark matter mess?



QCD AXIONS ARE DM CANDIDATES

$$m_a \lesssim 10^{-2} \text{ eV}$$



* Field misaligned $m_a \gg 3H \rightarrow$ oscillation

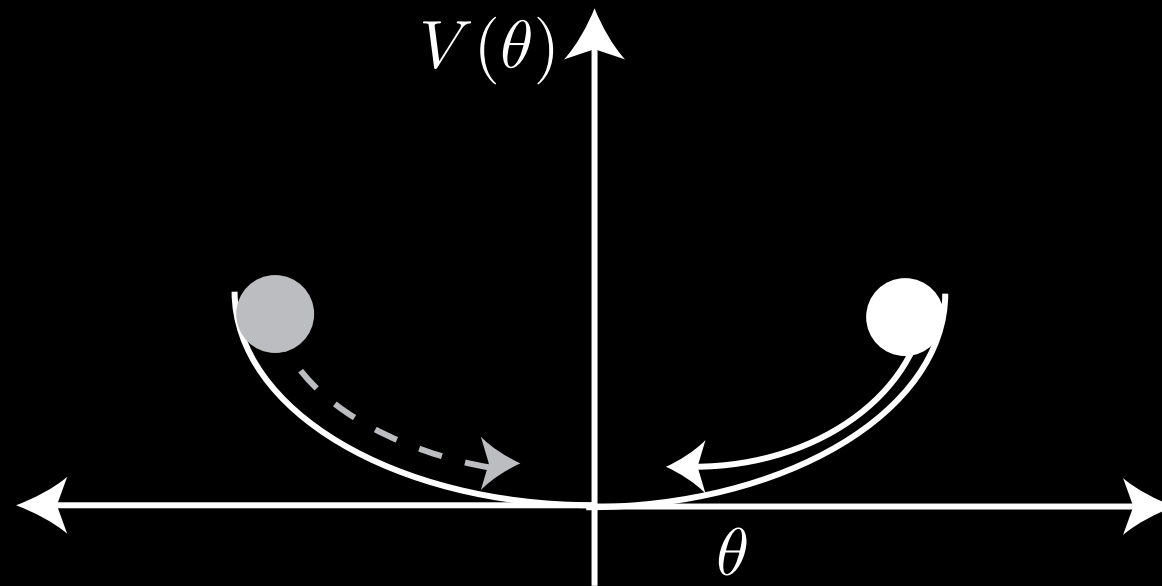
* $\rho_a \propto (1+z)^3$ [as cold dark matter should]

* Axions **ARE** cold

$$v_a/c \lesssim 10^{-13} \text{ at CMB decoupling timescales}$$

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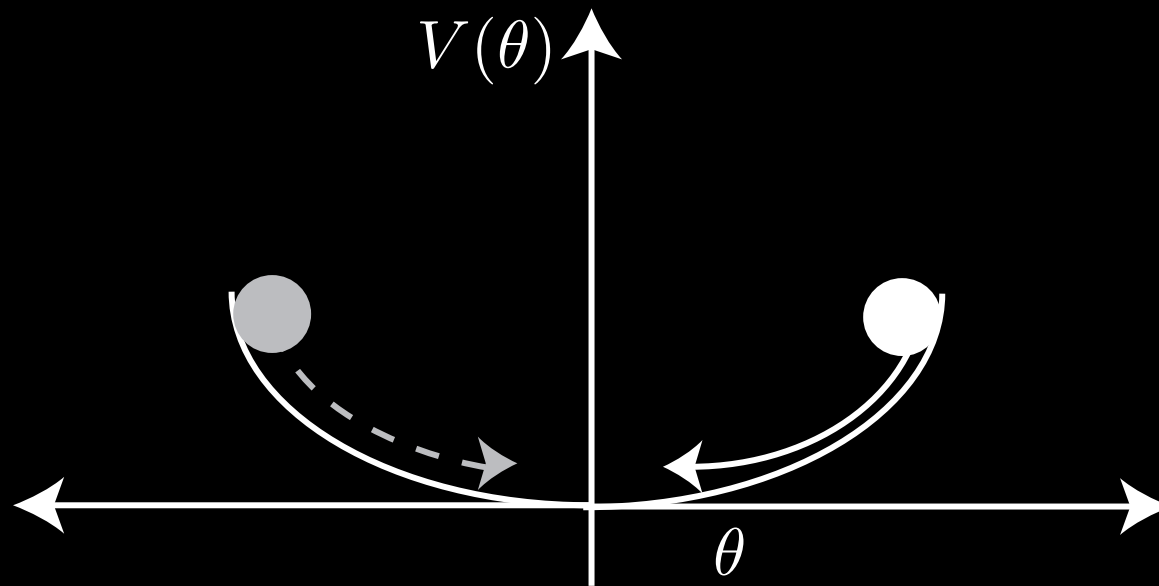
The QCD axion is a cold dark matter candidate

$$\Omega_{\text{mis}} h^2 = 0.236 \langle \theta_i^2 f(\theta_i) \rangle \left(\frac{m_a}{6.2 \mu\text{eV}} \right)^{-7/6}$$

*Solves a problem in particle physics:
Gives us a dark matter candidate for free!*

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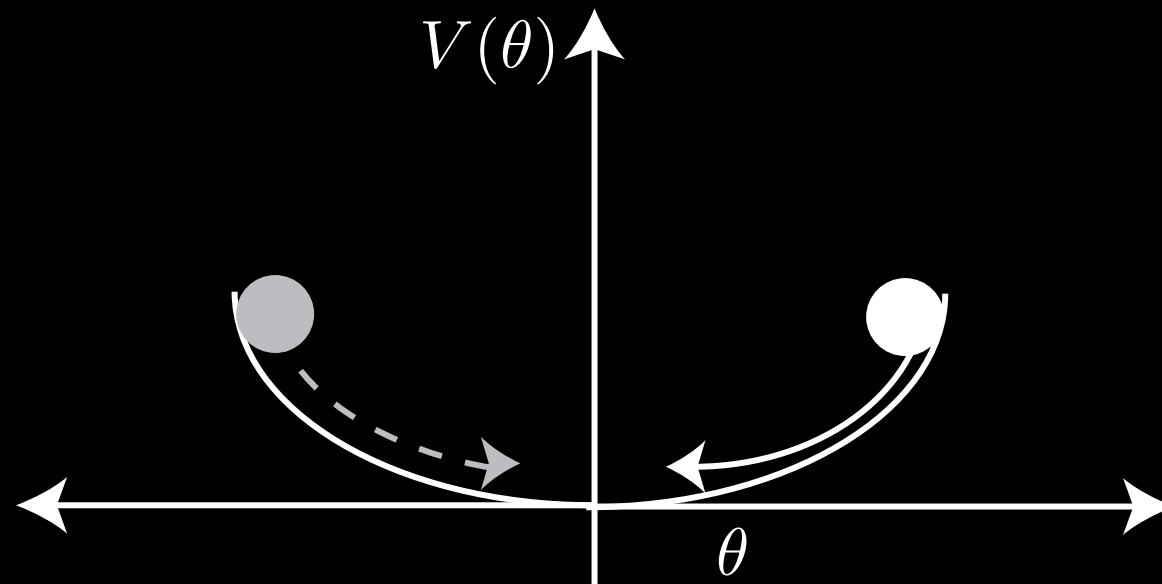
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Anthropic axion window: $f_a > \max \{T_{\text{RH}}, H_{\text{I}}\}$

- * Axion field is relatively homogeneous

$$\langle \theta^2 \rangle = \bar{\theta}^2 + \left(\frac{H_I}{2\pi f_a} \right)^2$$

- * Abundance

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Misalignment in our Hubble Patch

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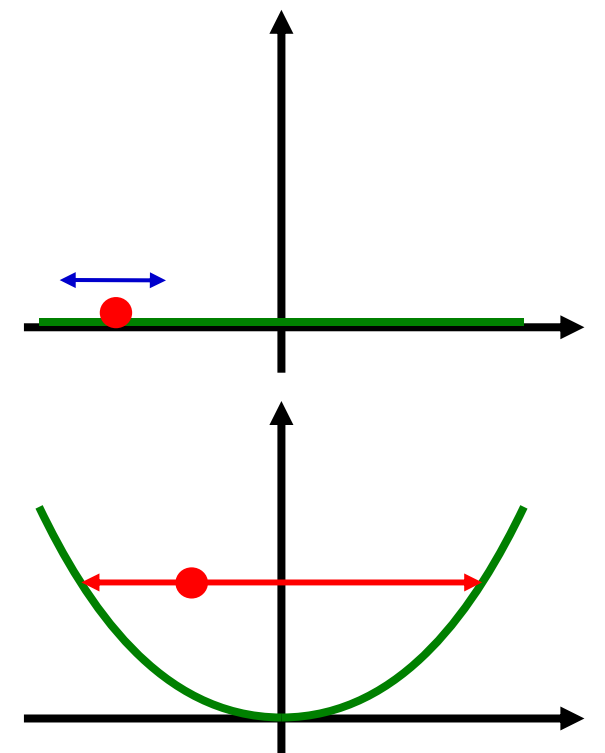
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Vacuum fluctuations from inflation

- * Abundance

De Sitter expansion imprints
scale invariant fluctuations



From Raffelt 2012

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$$\Omega_a h^2 \simeq 0.43 \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{7/6} \theta_i^2$$

$$\Omega_a h^2 \simeq 0.005 \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{3/2} \theta_i^2$$

- * $\bar{\theta}$ can be tuned to get DM abundance for many axion masses

Classic axion window: $f_a < \max \{T_{\text{RH}}, H_{\text{I}}\}$

✳ Axion field is very inhomogeneous

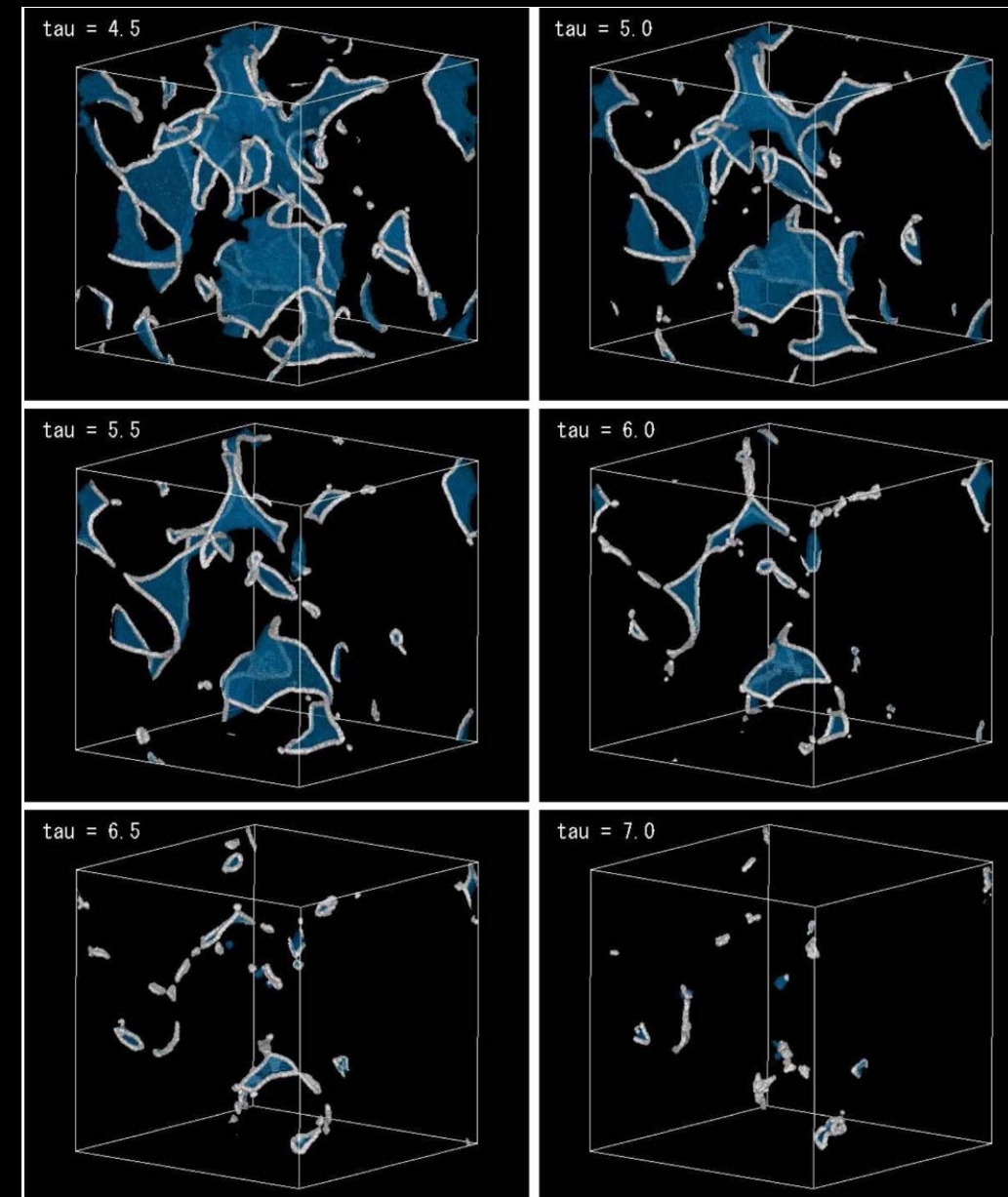
$$\langle \bar{\theta}_i^2 \rangle = \frac{\pi^2}{6}$$

✳ Defects [domain walls, strings, etc..]

$$\mathcal{O}(1) \lesssim \alpha_{\text{defect}} \lesssim \mathcal{O}(10^2)$$

✳ Abundance

$$\Omega_a h^2 \simeq 2.0 \{1 + f_{\text{defect}}\} \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{7/6}$$



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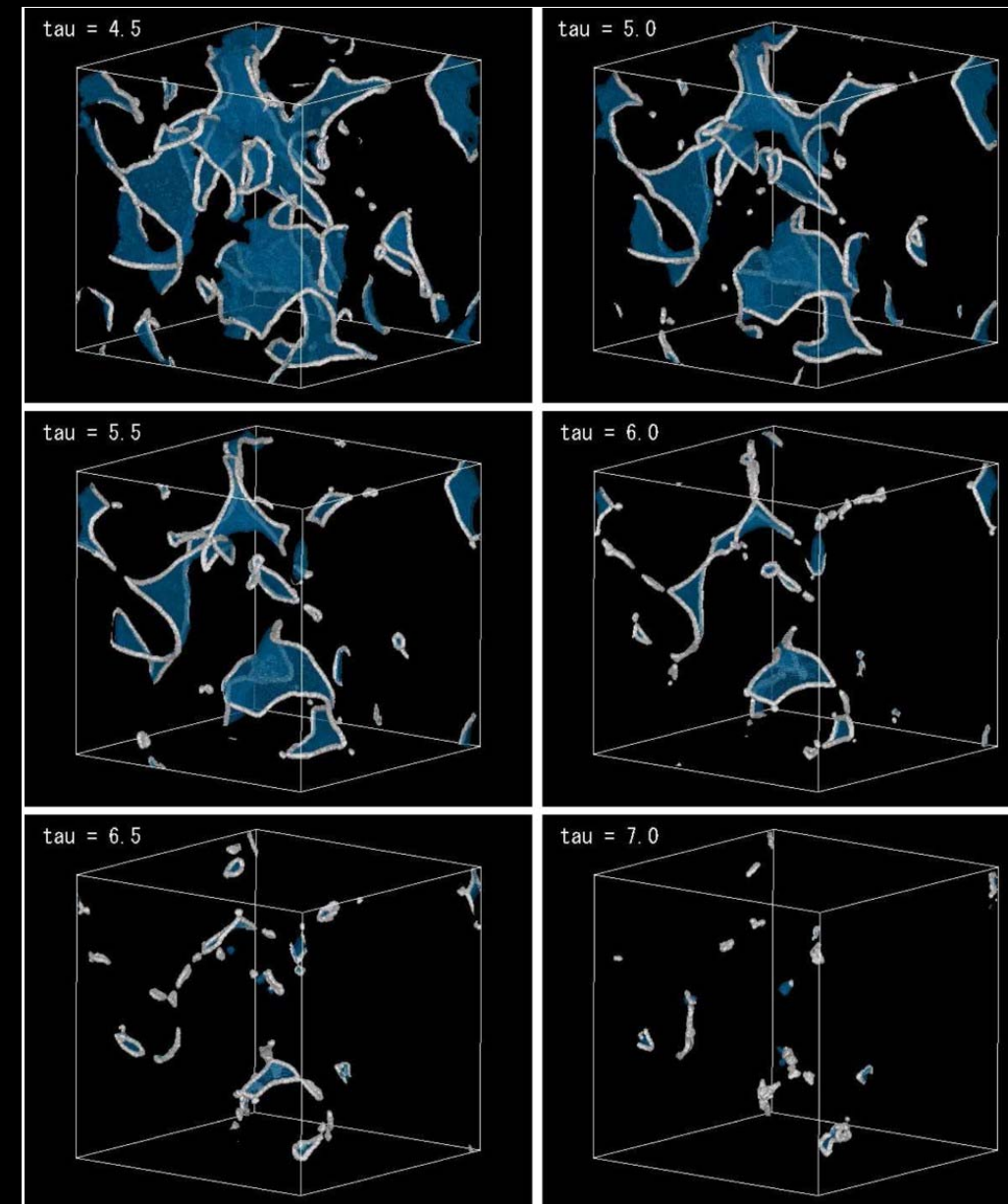
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CONTROVERSY!

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Dark matter axion abundance

* QCD axion couples to quarks/pions, temp-dependent mass

* High-temp regime

$$m_a = 0.02 m_a^{(T=0)} \left(\frac{\Lambda_{\text{QCD}}}{T} \right)^4 \quad \text{if } T \gg \Lambda_{\text{QCD}}$$

* Low-temp regime $m_a = m_a^{(T=0)}$ if $T \lesssim \Lambda_{\text{QCD}}$

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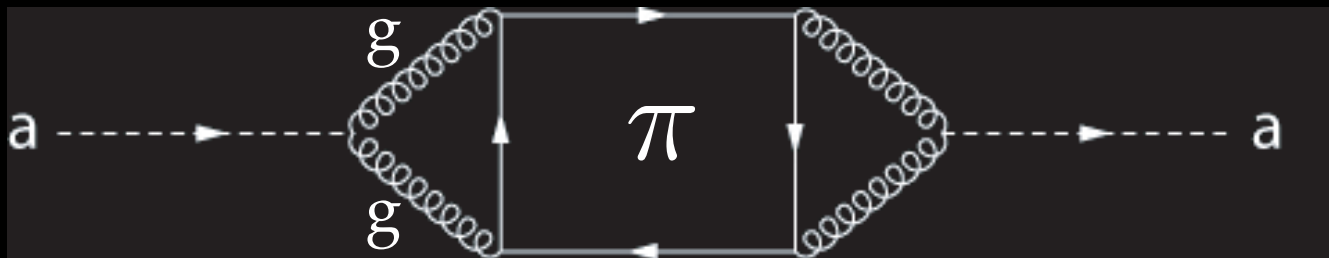
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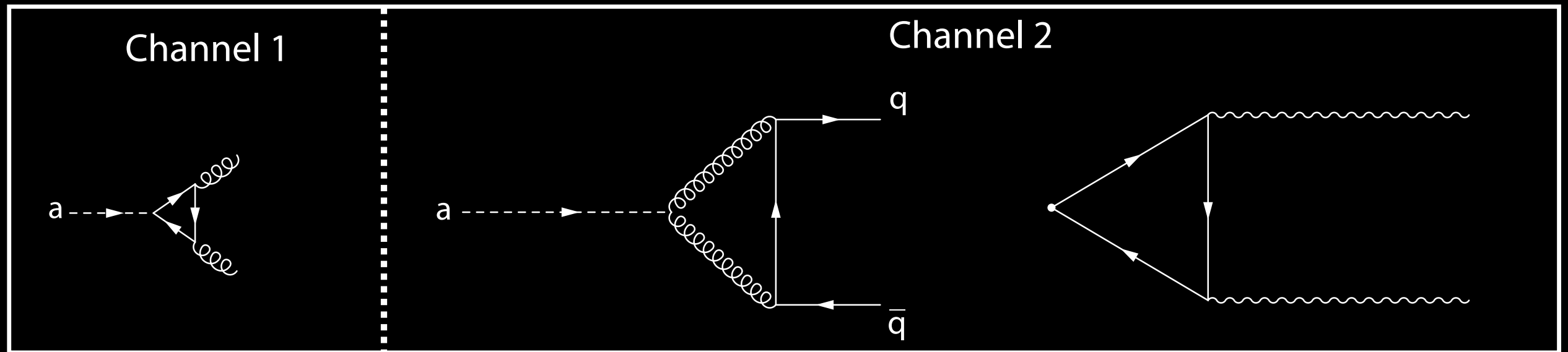


$$m_a \simeq \frac{m_\pi f_\pi}{f_a} \frac{\sqrt{r}}{1+r}$$

$$r \equiv m_u/m_d$$

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Two-photon coupling of axion



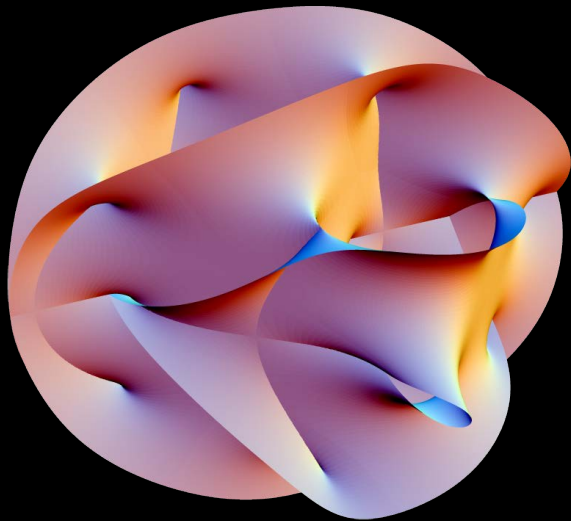
* Axions interact weakly with SM particles $\Gamma, \sigma \sim \alpha^2$

* Axions have a two-photon coupling

$$g_{a\gamma\gamma} = -\frac{3\alpha}{8\pi f_a} \xi$$

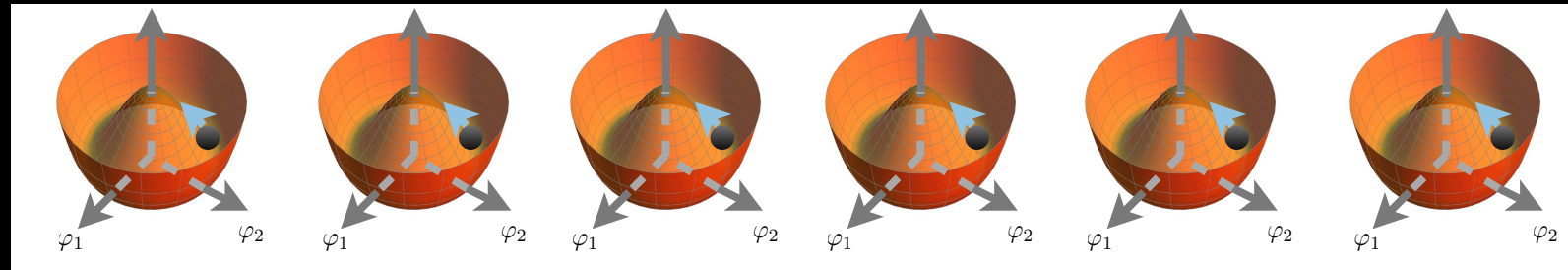
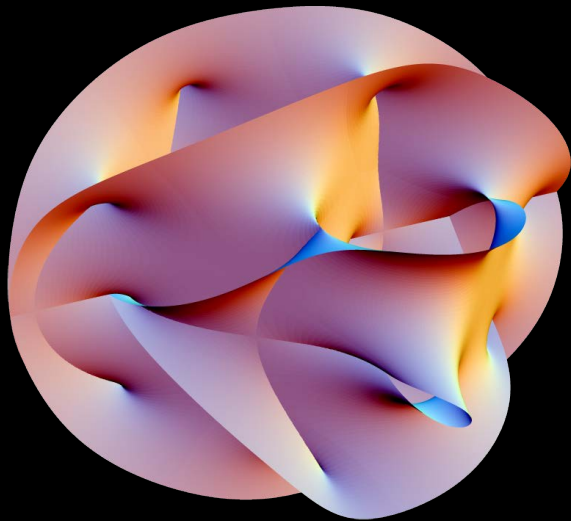
ULTRA-LIGHT AXIONS (ULAS) IN STRING THEORY

✧ In string theory, extra dimensions compactified: Calabi-Yau manifolds



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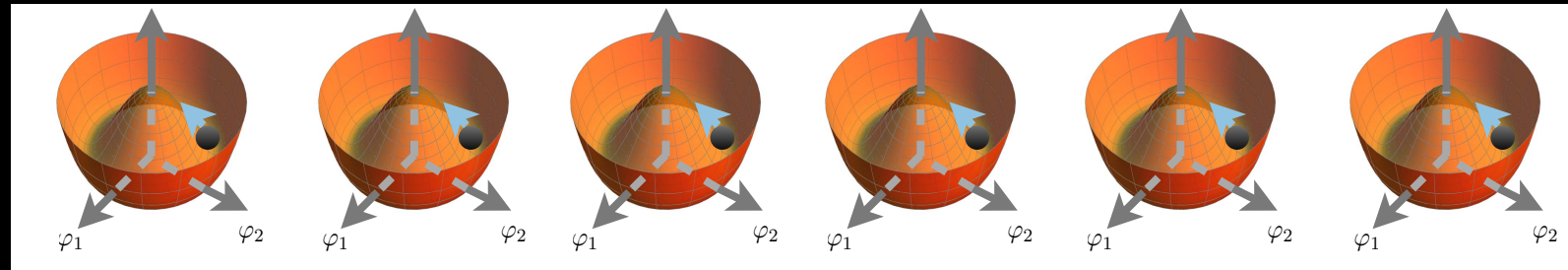
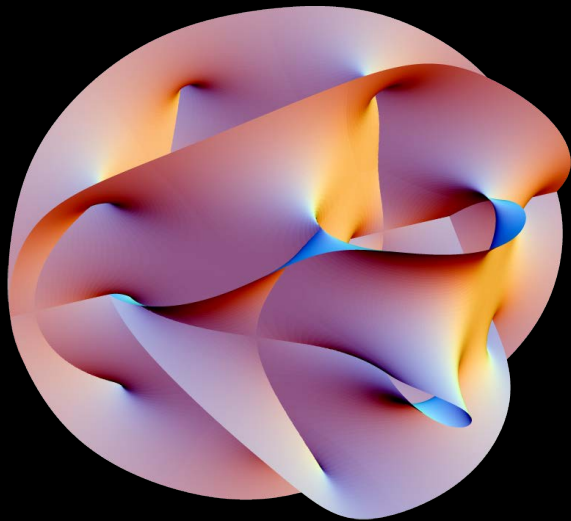


+....

*Hundreds of scalars
with approx shift symmetry*

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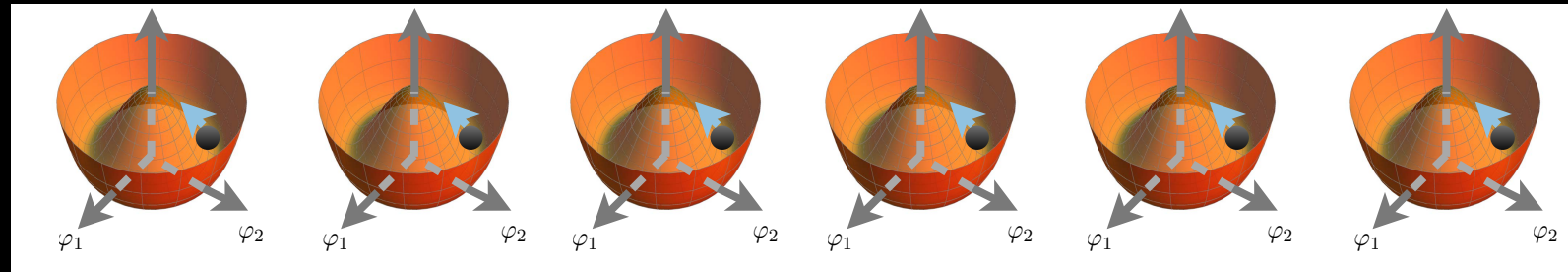
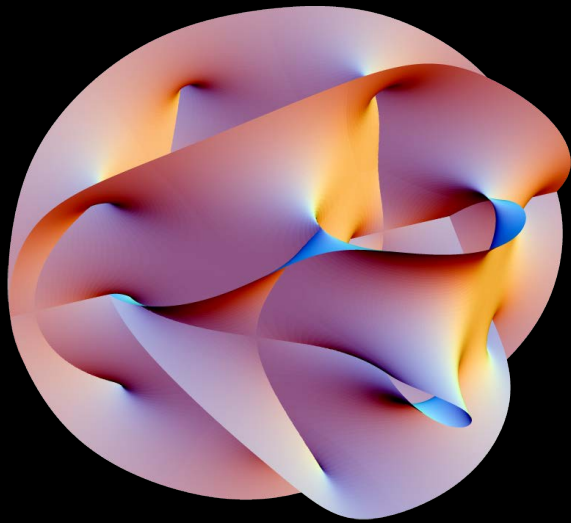
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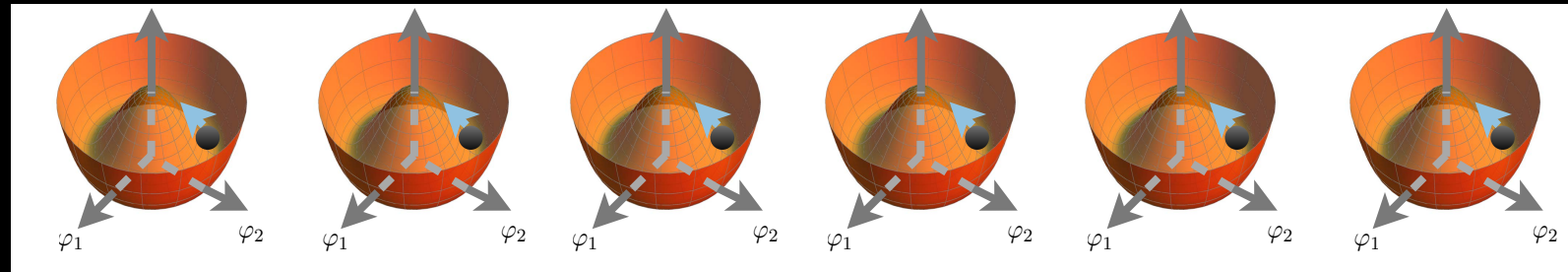
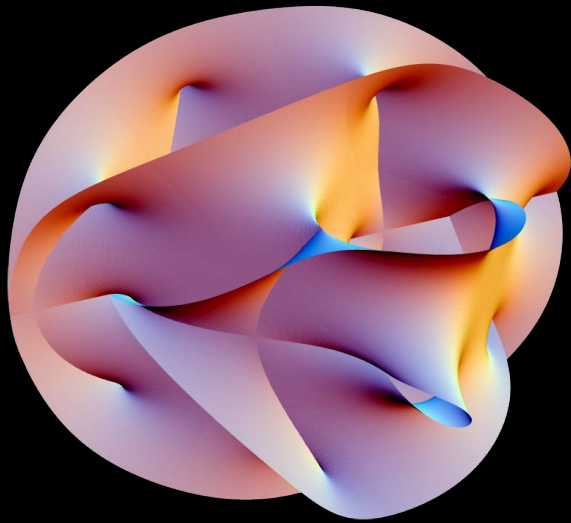
Many axions

- * Mass acquired non-perturbatively (instantons, D-Branes)

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

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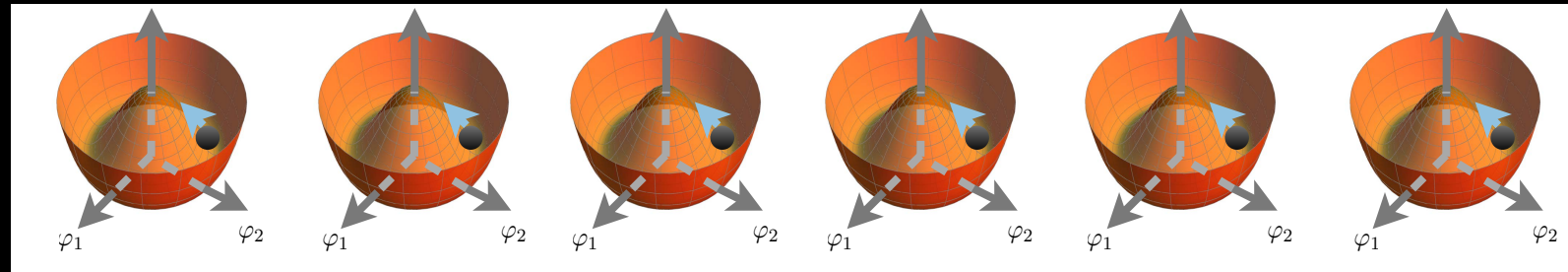
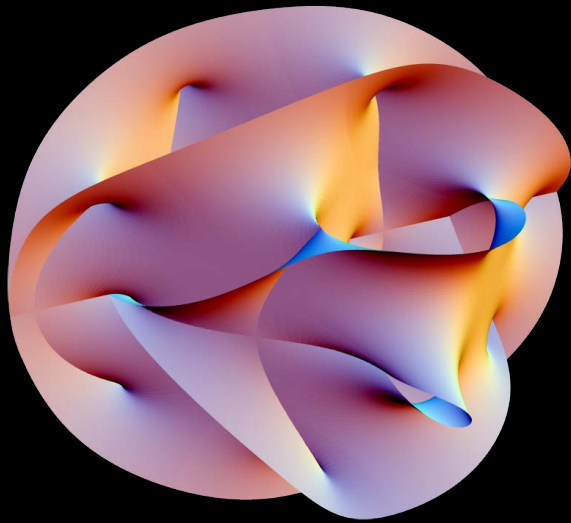
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**Scale of new
ultra-violet physics**

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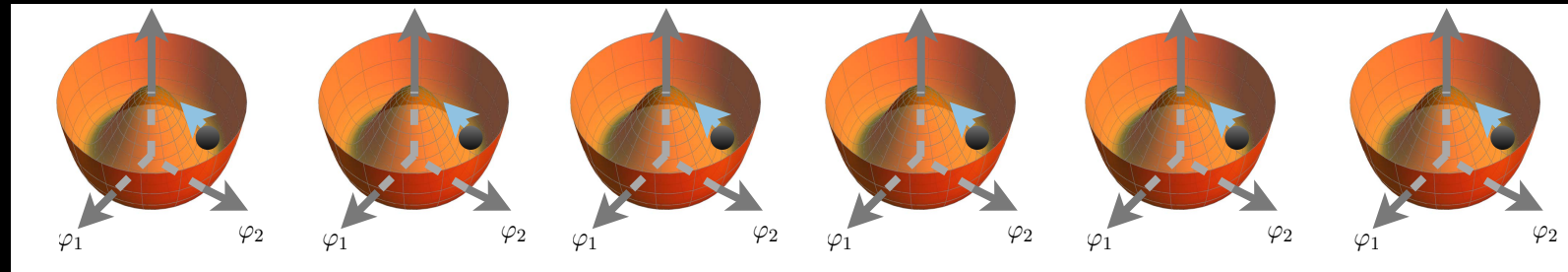
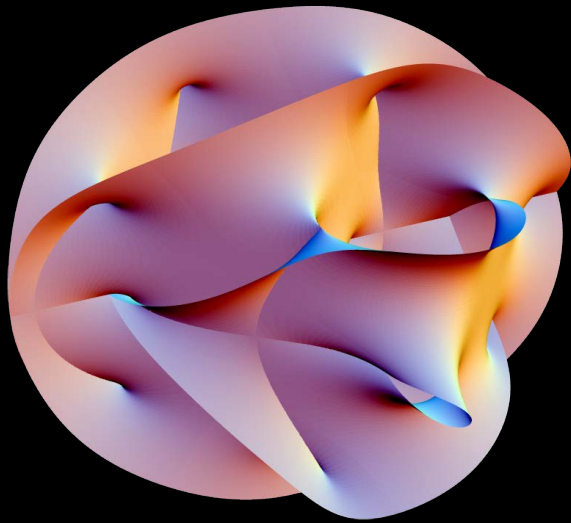
**Scale of extra dimensions
in Planck units**

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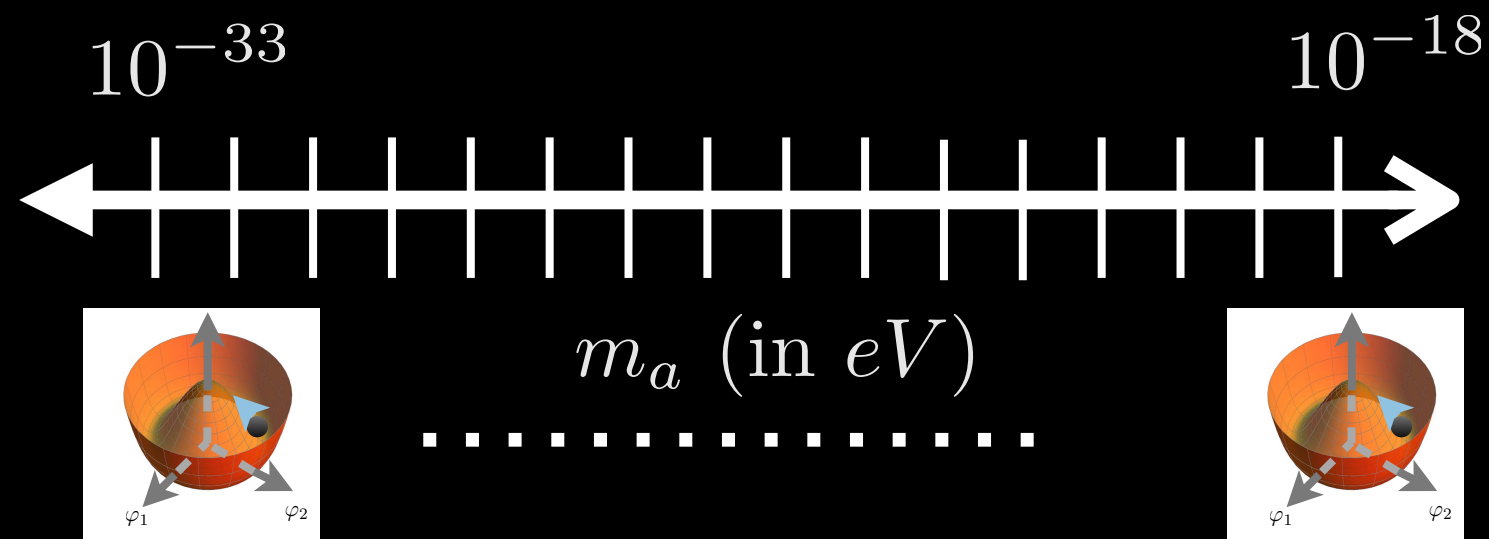
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Axiverse! Arvanitaki+ 2009

Witten and Svrcek (2006), Acharya et al. (2010), Cicoli (2012)



ULTRA-LIGHT AXIONS

✱ Interactions with standard model are very small!

$$g_{a\gamma\gamma} \propto m_a$$

✱ Inaccessible to terrestrial experimentation

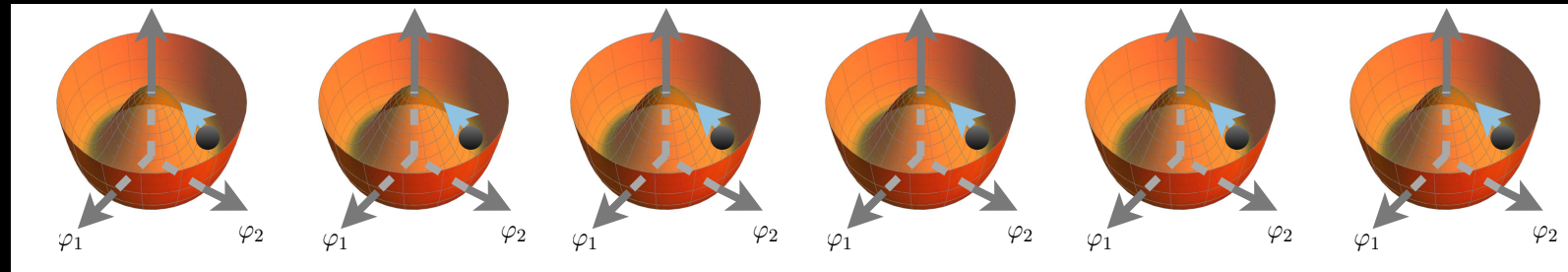
Ultra-light axions still gravitate!

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✧ Bosons moving in extra dimensions are axions in 4D!

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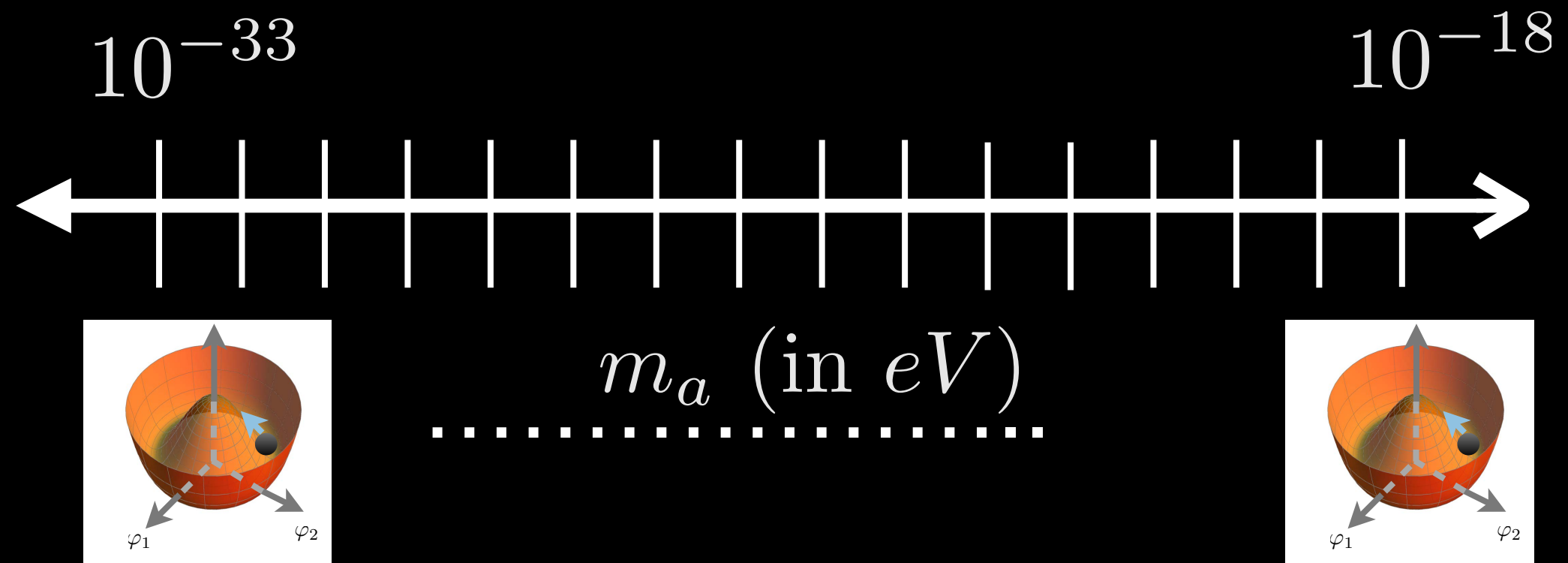
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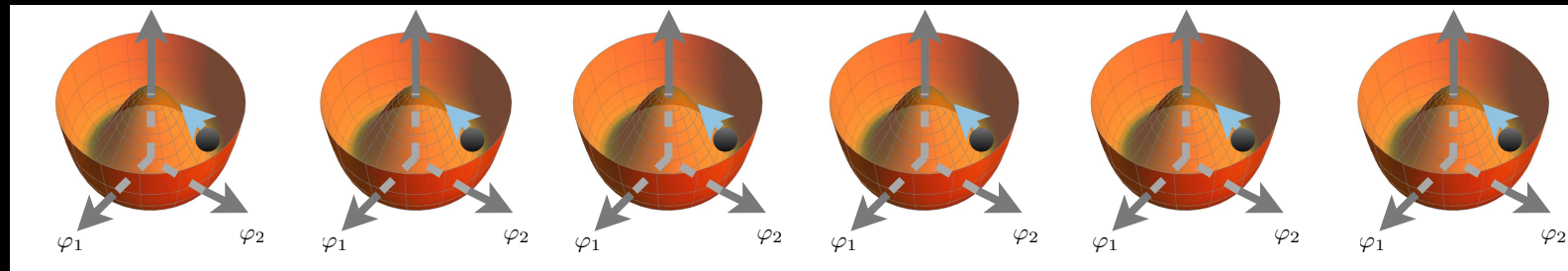


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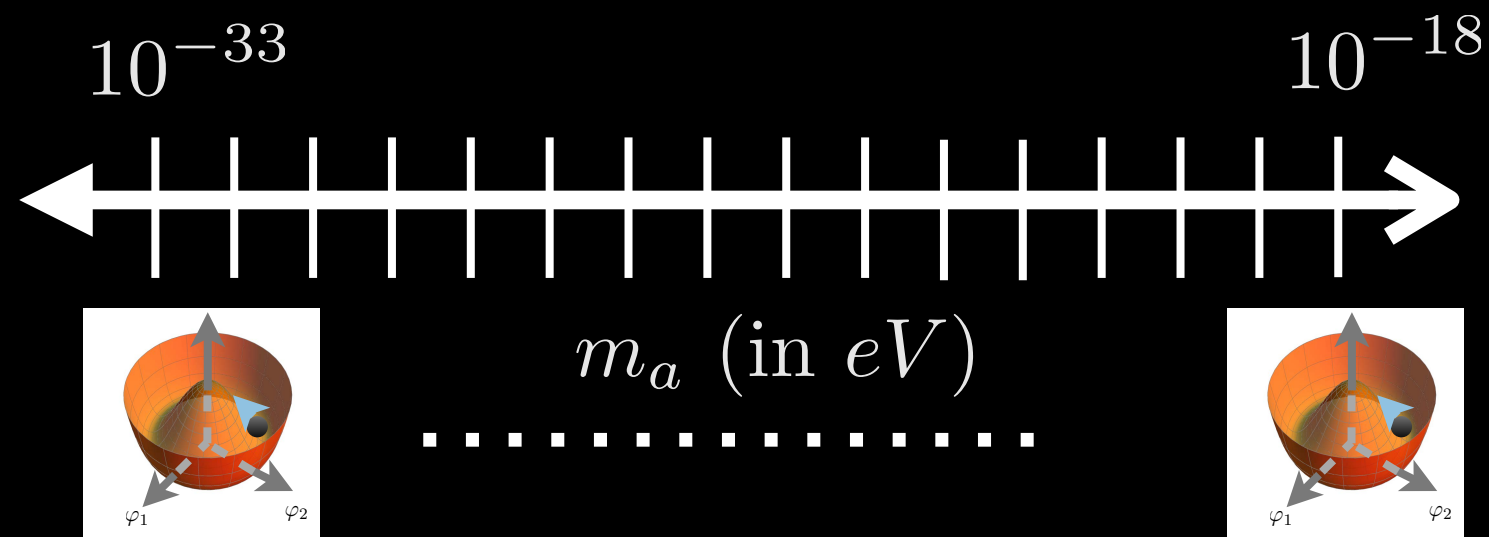
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✧ In string theory, extra dimensions compactified: Calabi-Yau manifolds



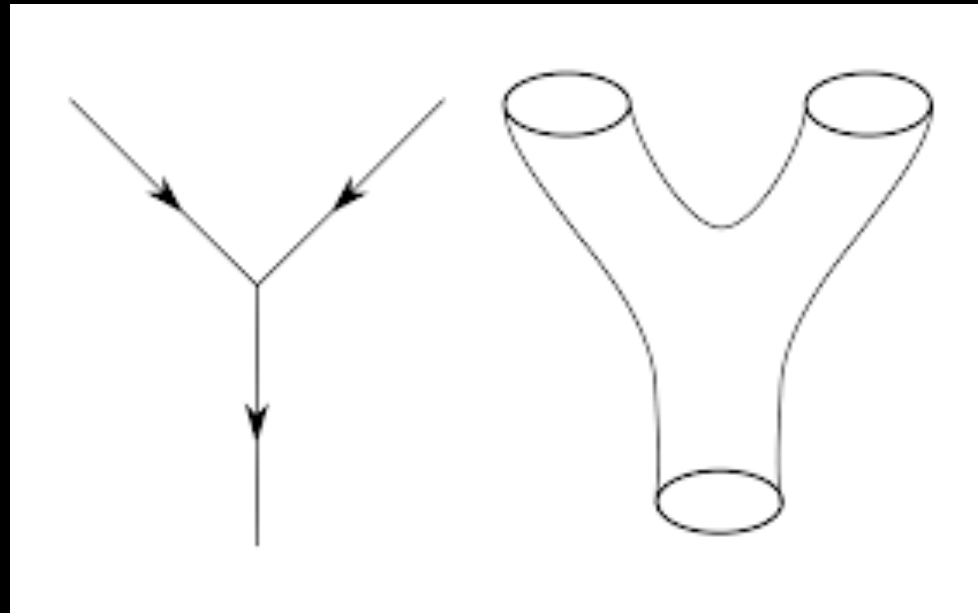
Axiverse! Arvanitaki+ 2009

Witten and Svrcek (2006), Acharya et al. (2010), Cicoli (2012)



STRING THEORY

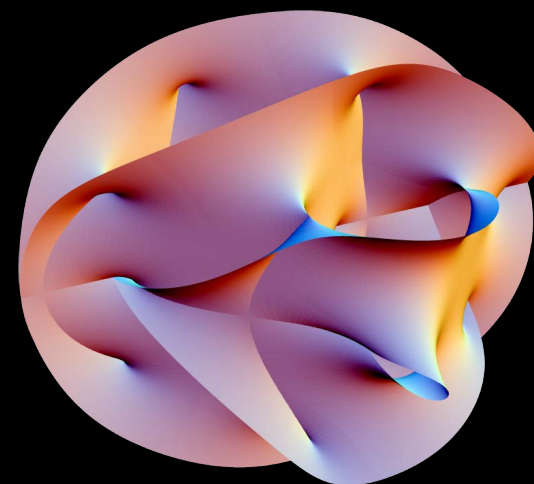
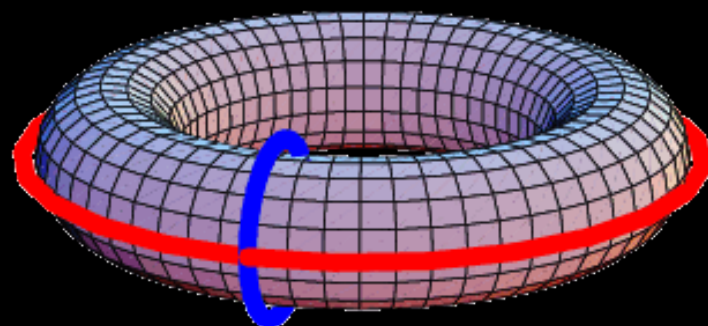
- * One framework that solves SM problems is string theory



Replace point particles with extended objects

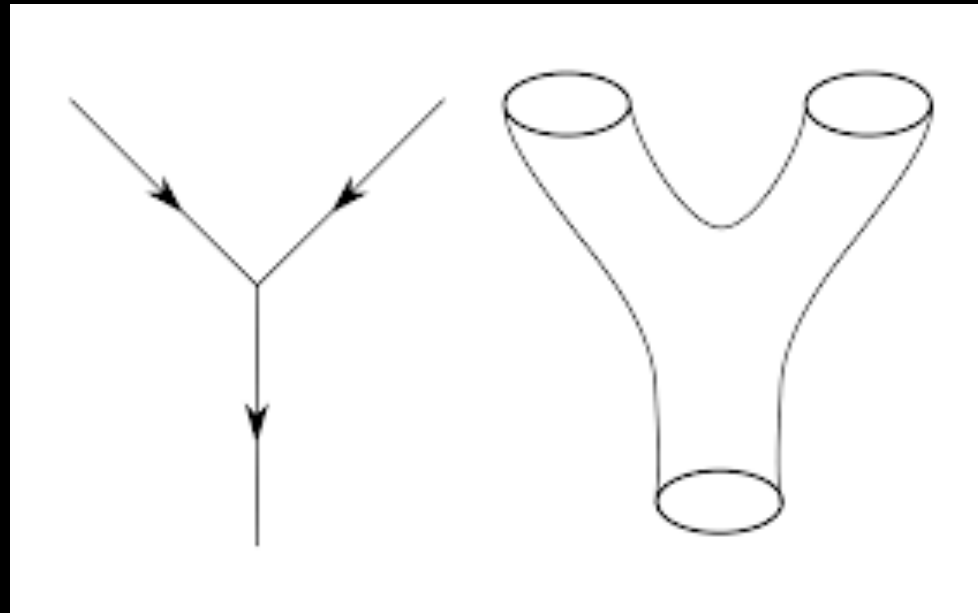
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Must be curled up/compactified



STRING THEORY

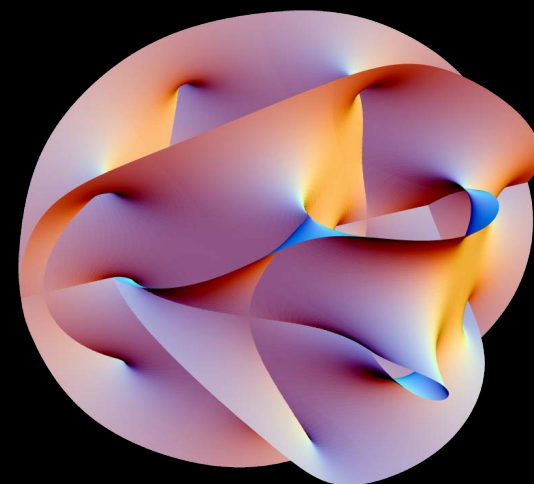
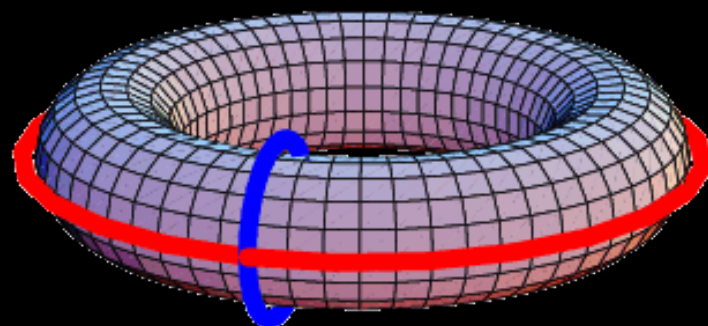
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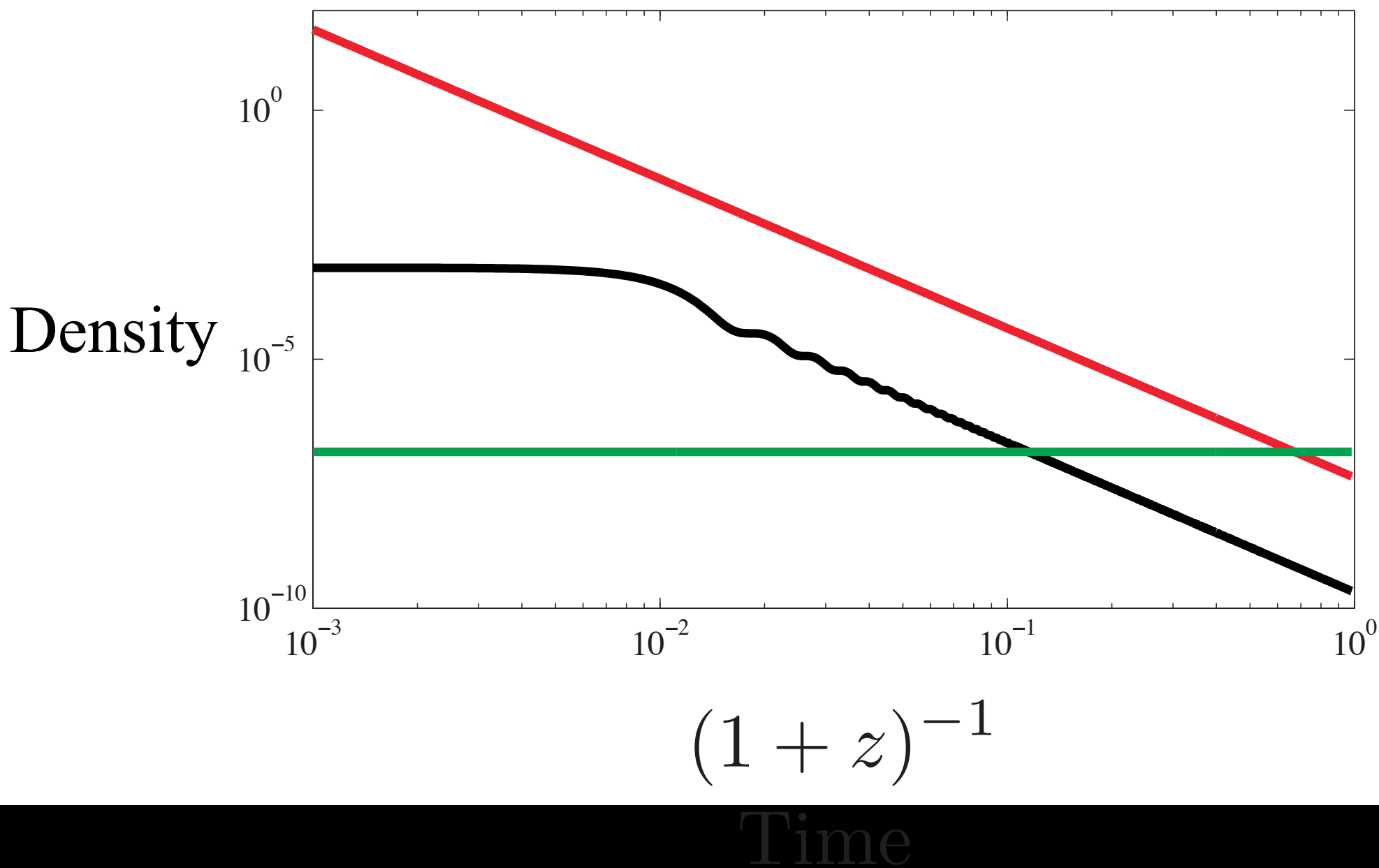
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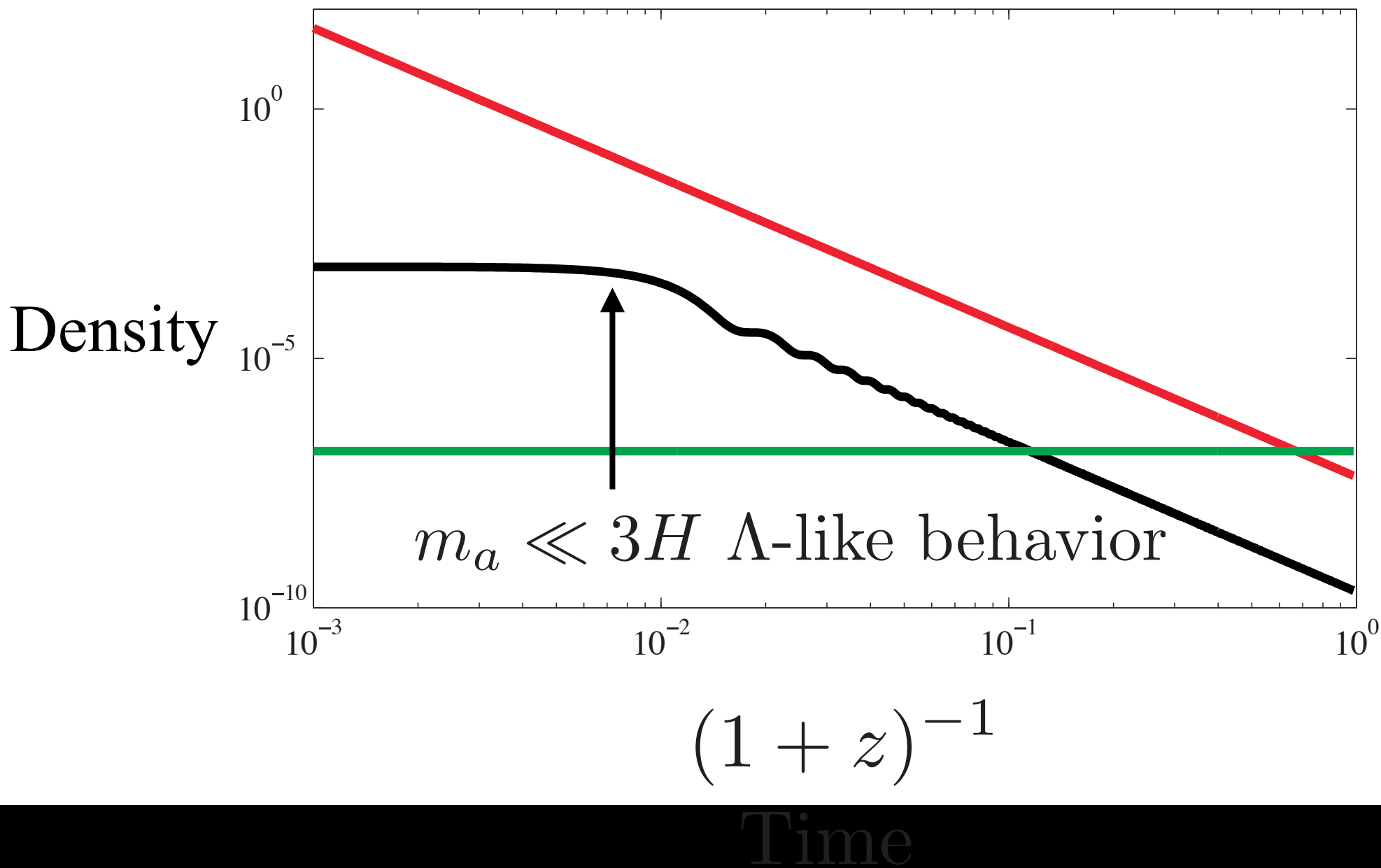
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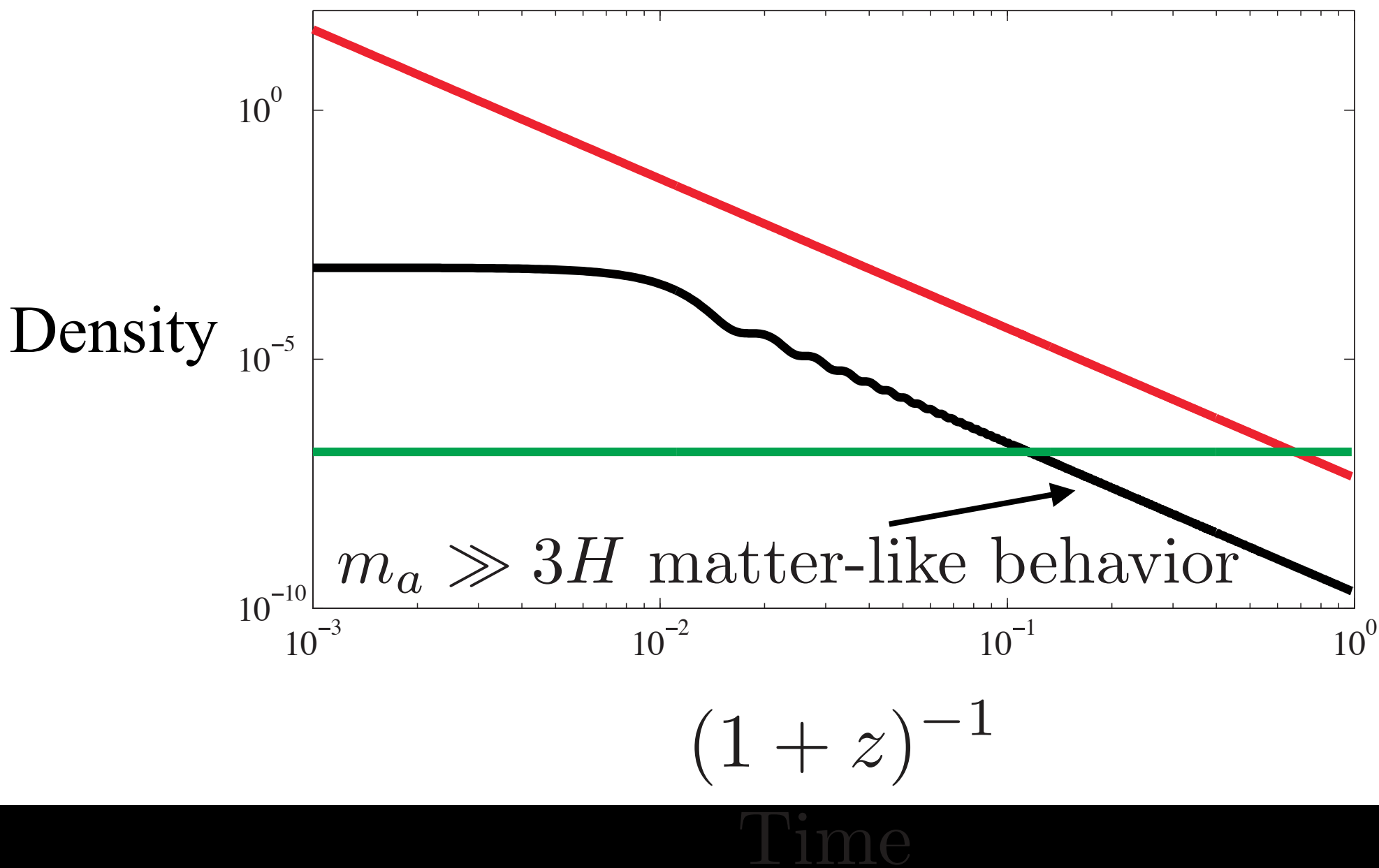
COSMOLOGY OF ULTRA-LIGHT AXIONS: DARK MATTER AND DARK ENERGY CANDIDATES



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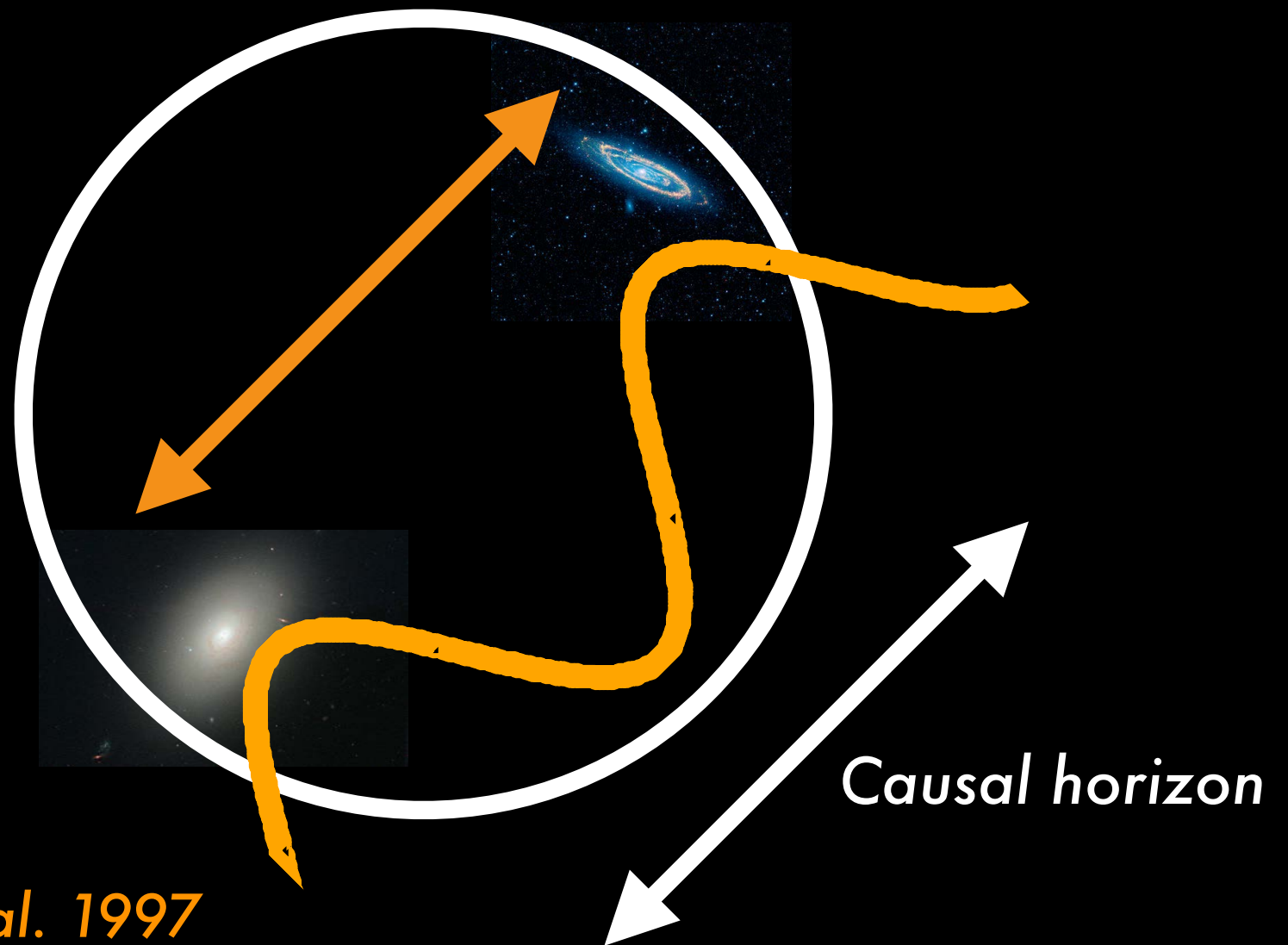
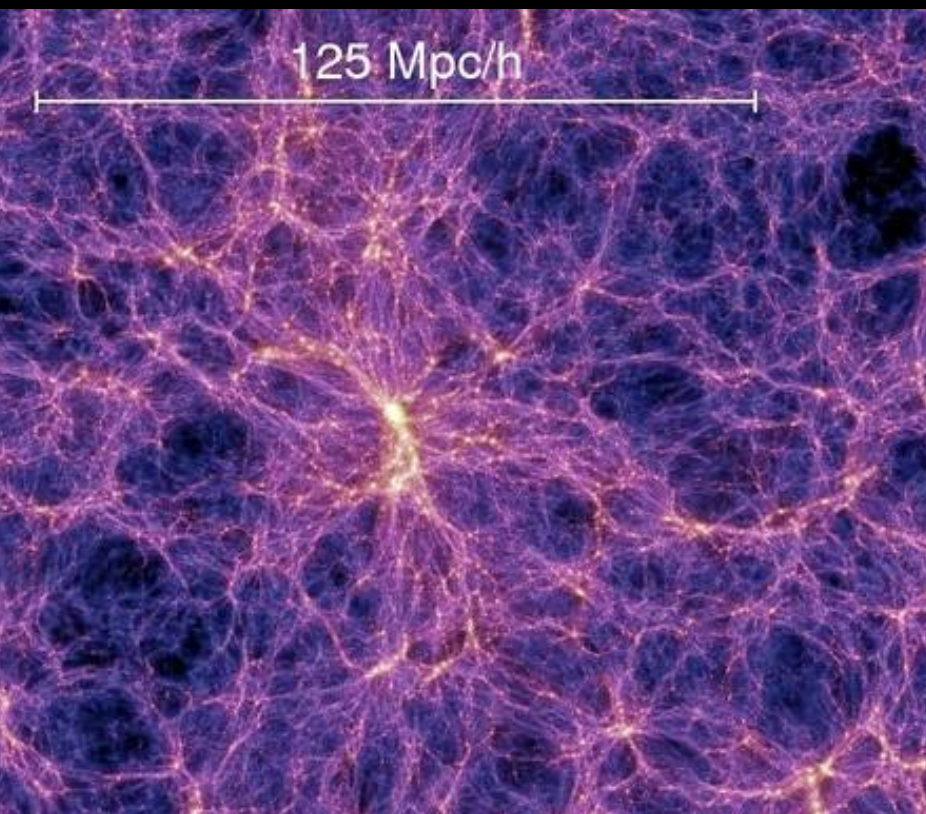


COSMOLOGY OF ULTRA-LIGHT AXIONS: DARK MATTER AND DARK ENERGY CANDIDATES



COSMOLOGY OF ULTRA-LIGHT AXIONS: DARK MATTER AND DARK ENERGY CANDIDATES

*Scale corresponding to
typical galaxy separation today*



Frieman et al 1995, Coble et al. 1997

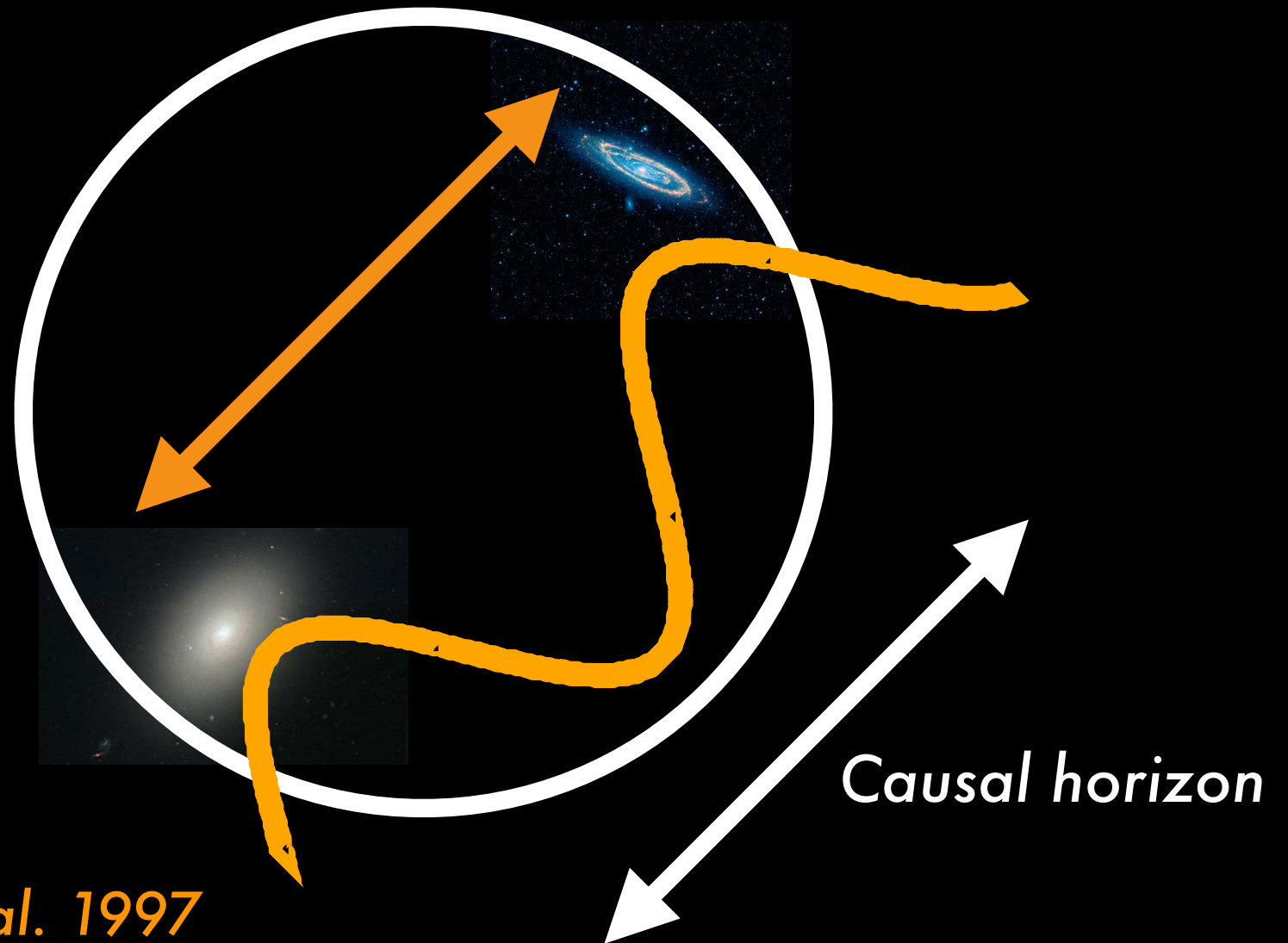
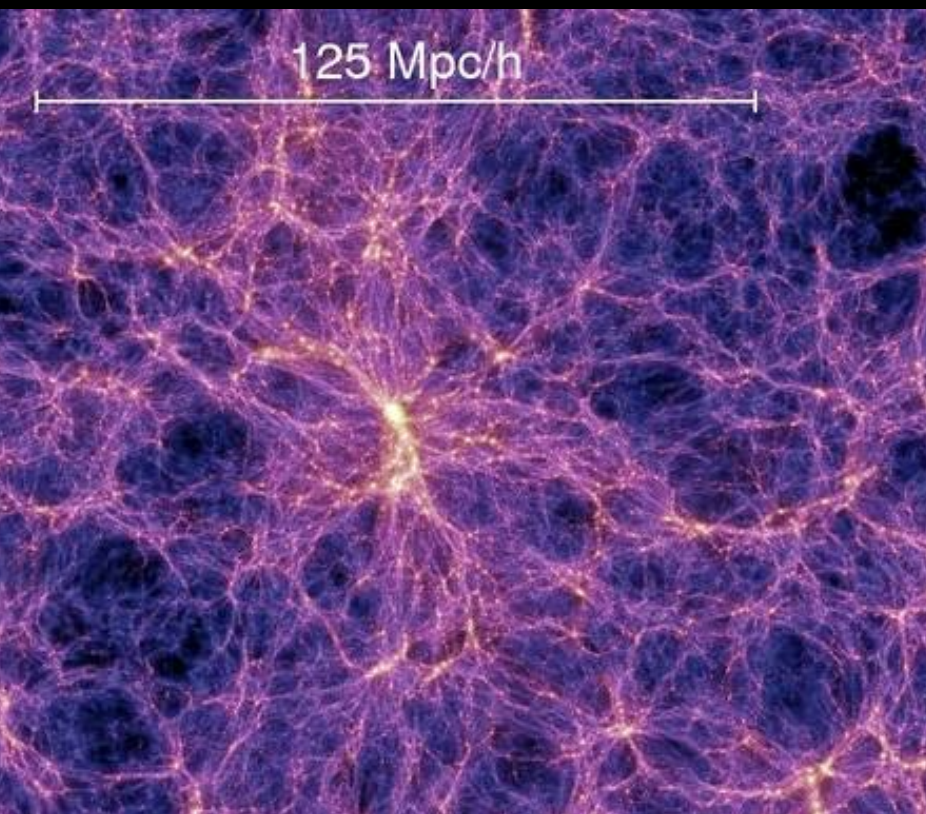
ULA as dark energy with specific $w(z)$

$$m_a \lesssim 10^{-27} \text{ eV}$$

ULA matter behavior starts too late for struct. formation

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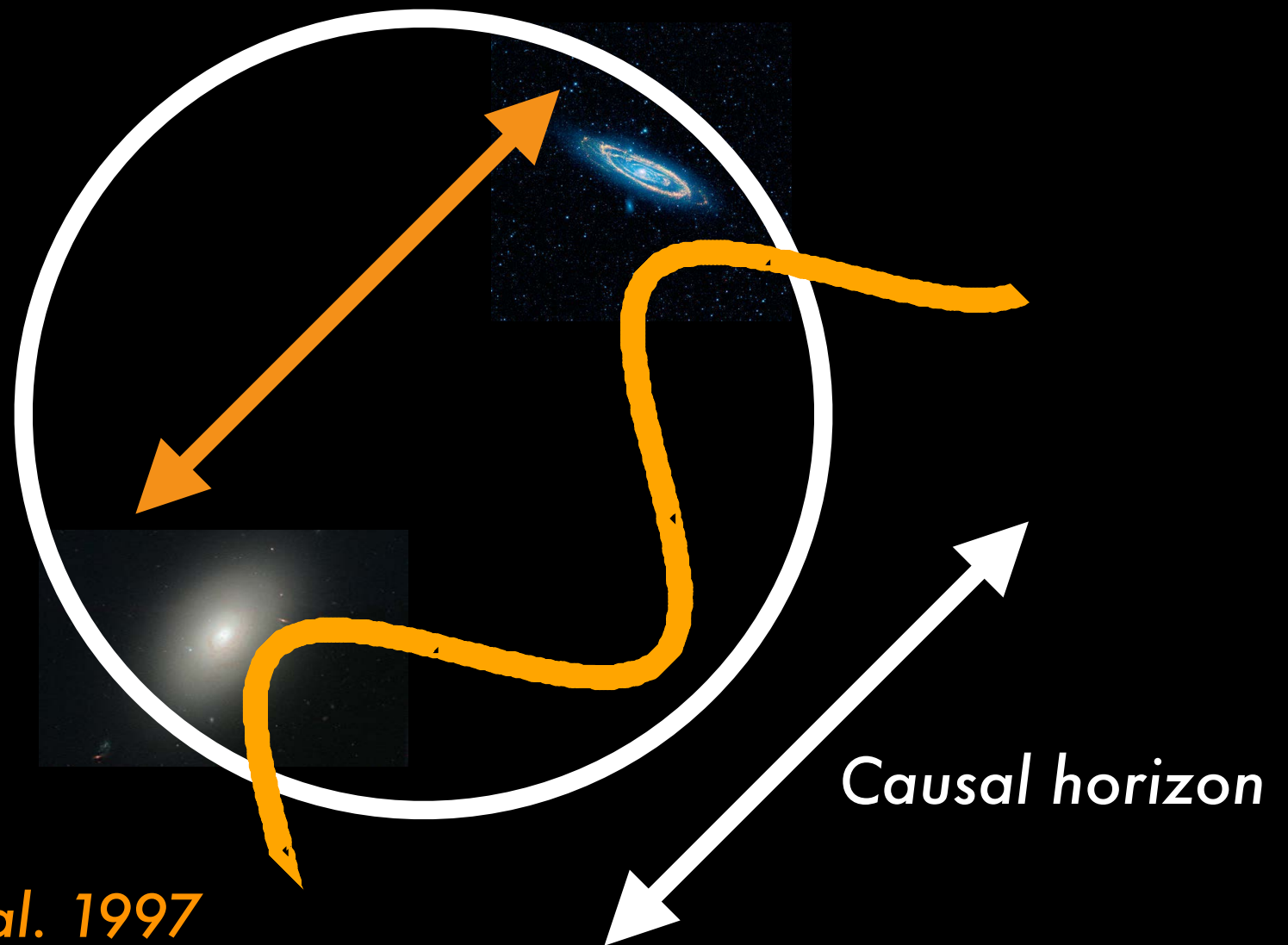
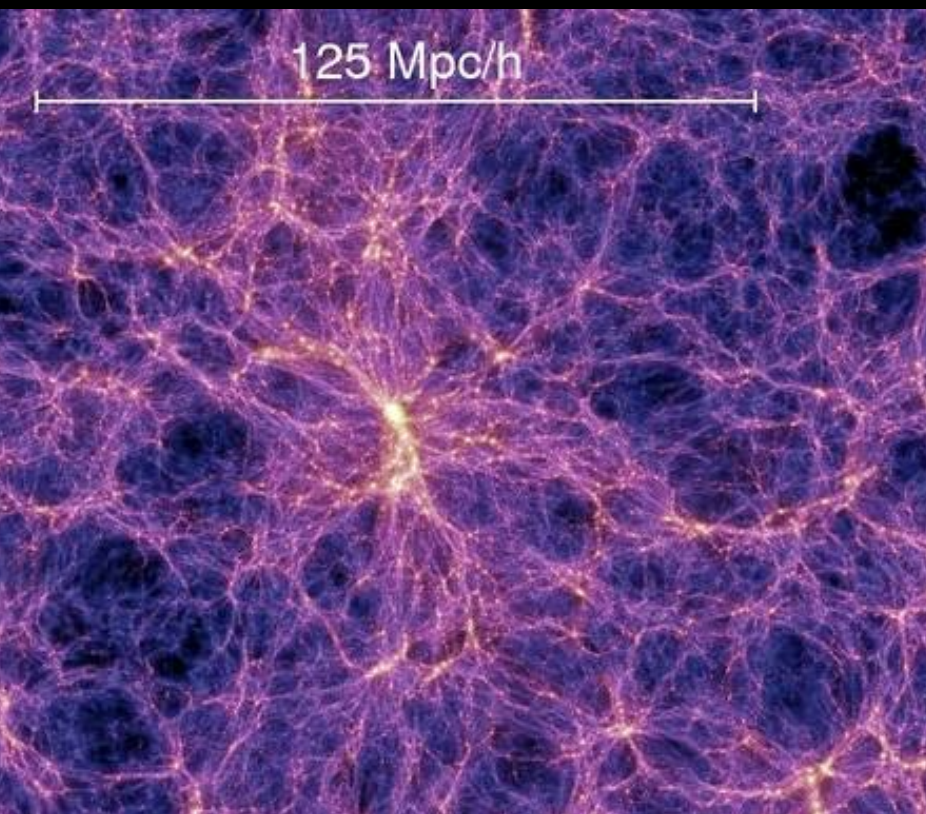
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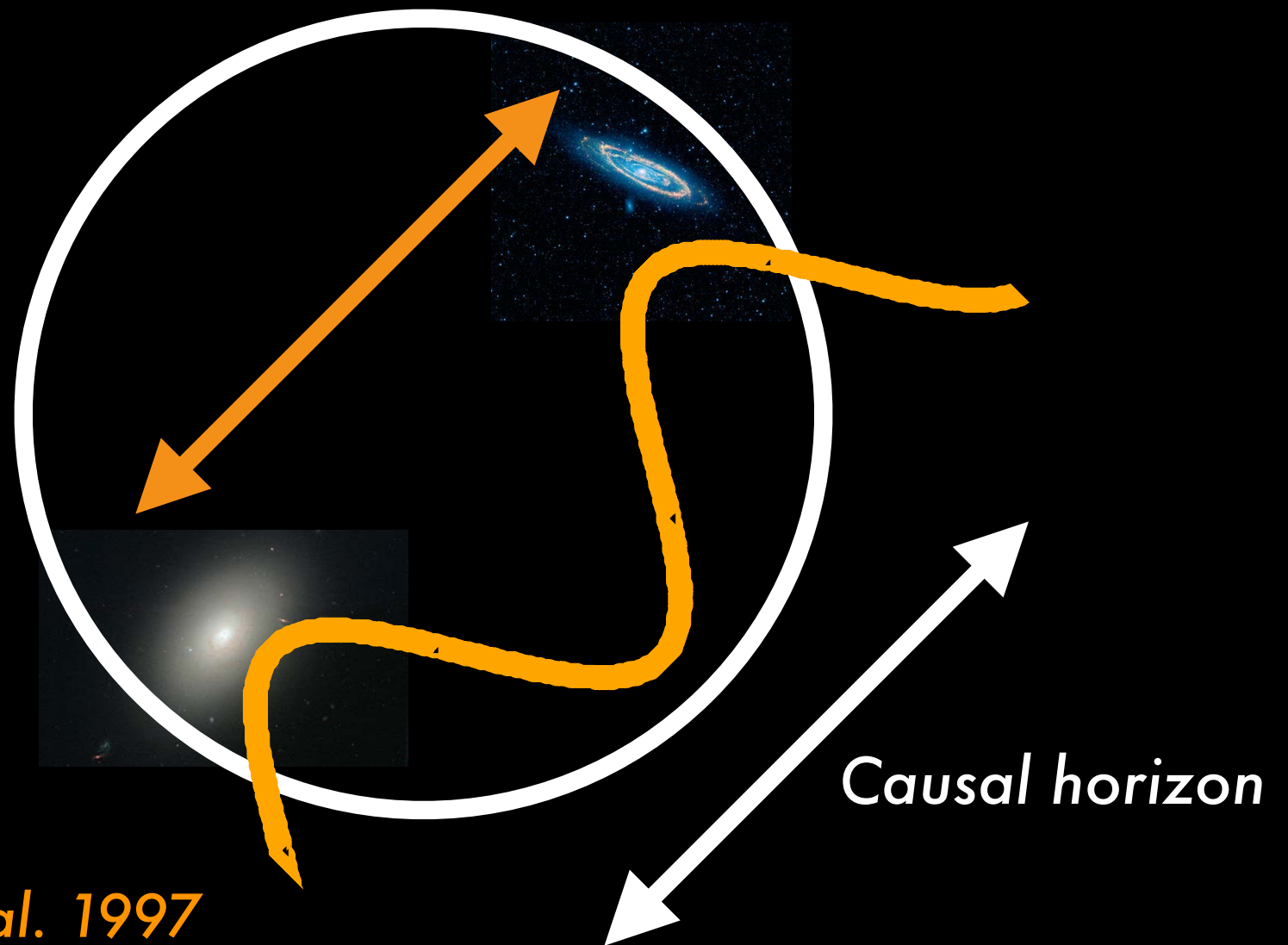
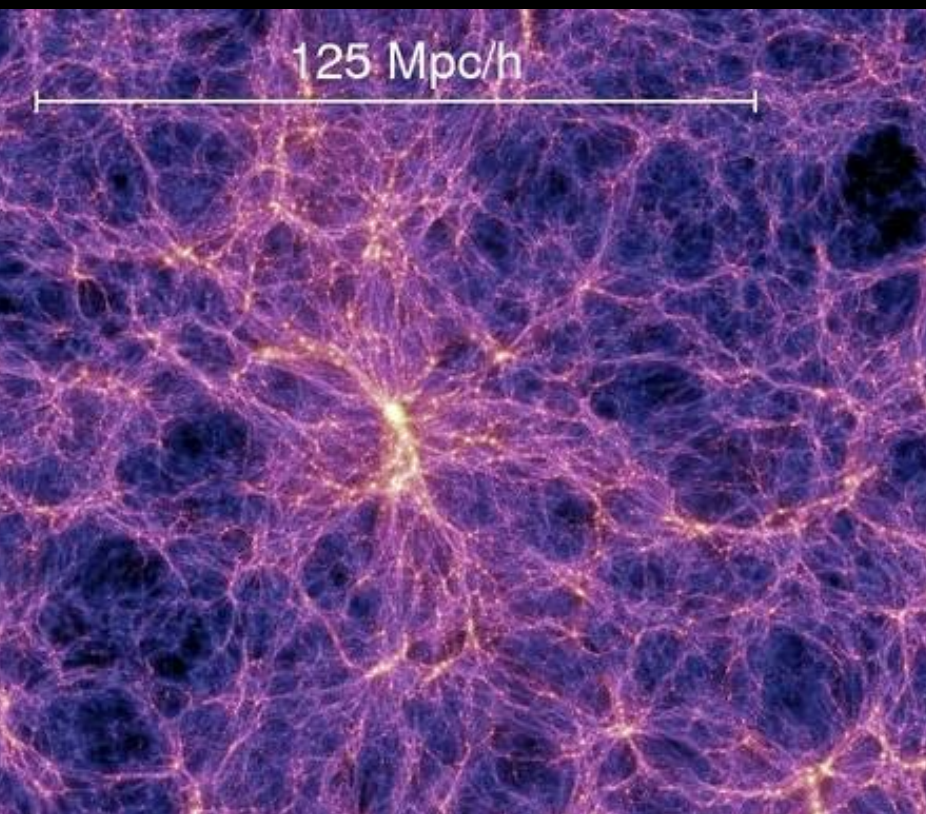
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Corresponds to time of matter/radiation equality, when

$$\rho_m = \rho_\gamma + \rho_\nu$$

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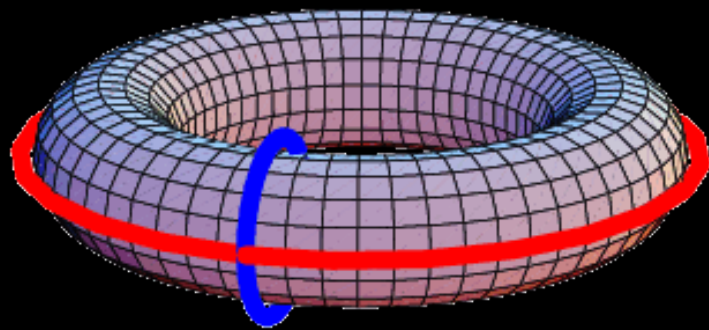
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Simple relic density constraints:

$$10^{-33} \text{ eV} < m_a < 10^{-18} \text{ eV}$$

Light axions and string theory

- * String theory has extra dimensions: *compactify (6)!*
- * Form fields and gauge fields: 'Axion' is KK zero-mode of form field



$$\mathcal{L} \propto \frac{a G \tilde{G}}{f_a}$$

ULAs: gravitational constraints

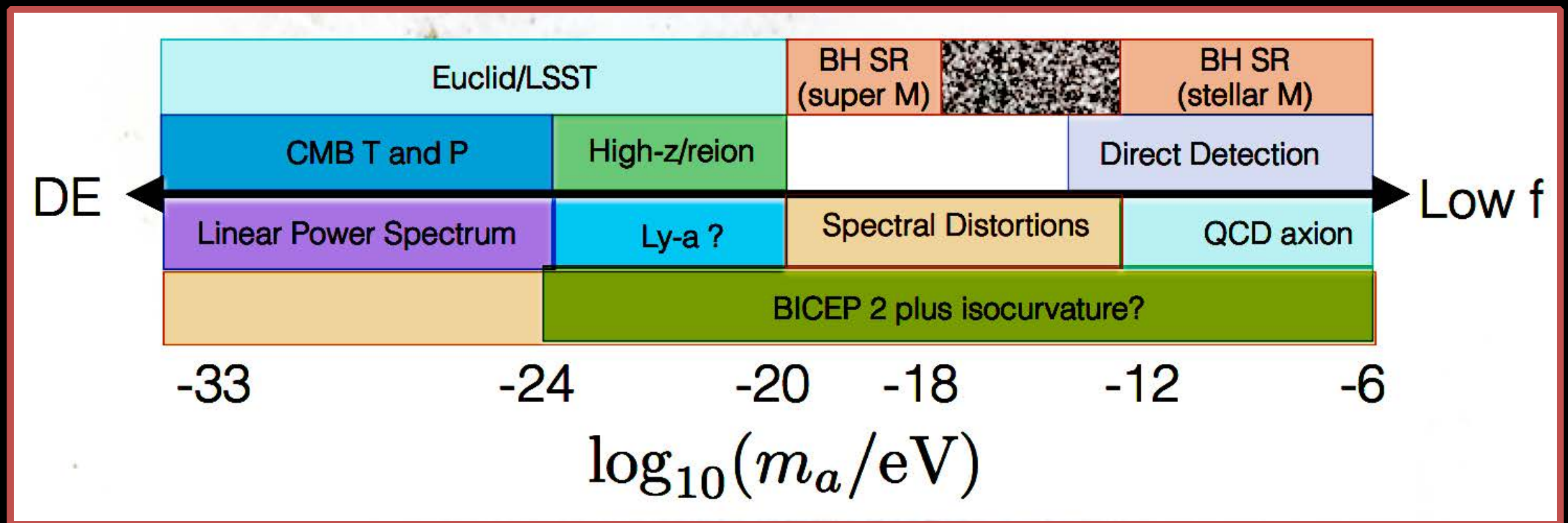


figure adapted from DJEM 2014

$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

Flat logarithmic mass distribution:
Very low axion masses natural!

ULAs: gravitational constraints

Independent of axion SM couplings: uncertainties astrophysical!

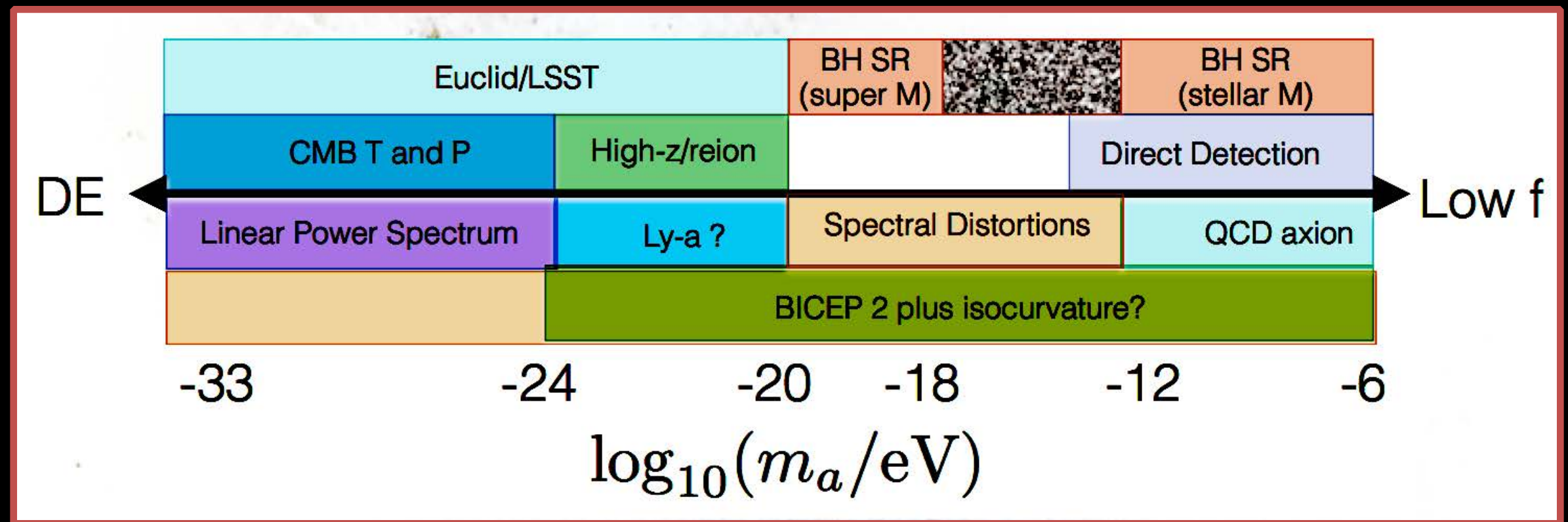


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Forecast: uncertain scales

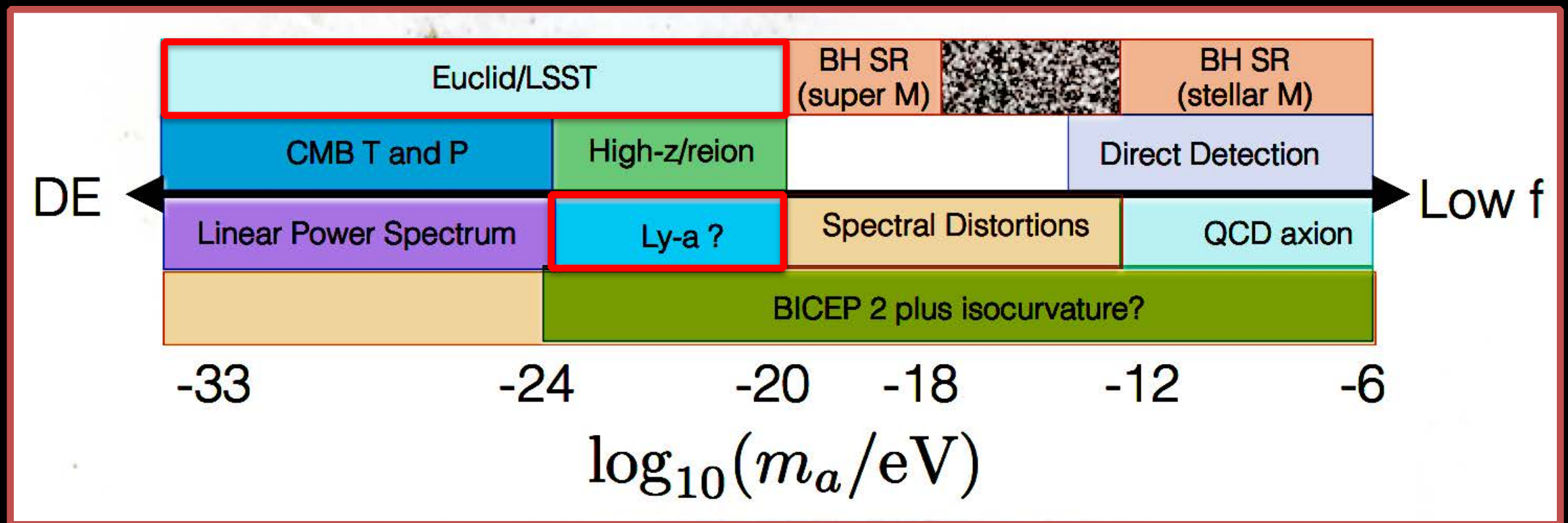


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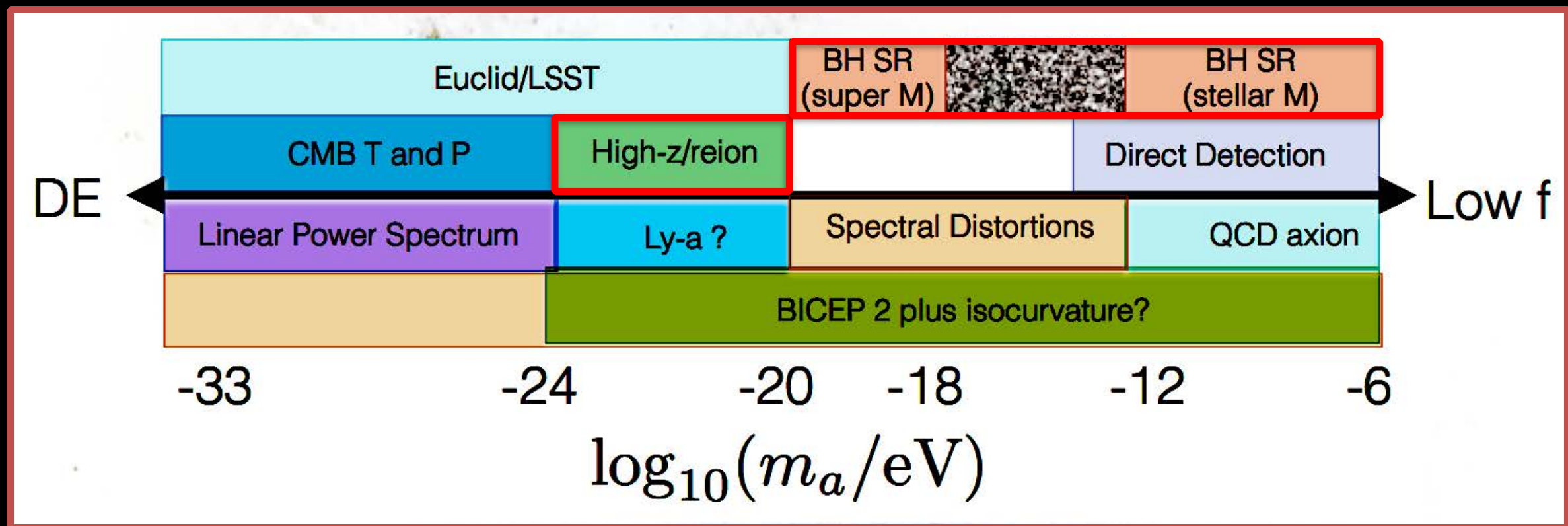


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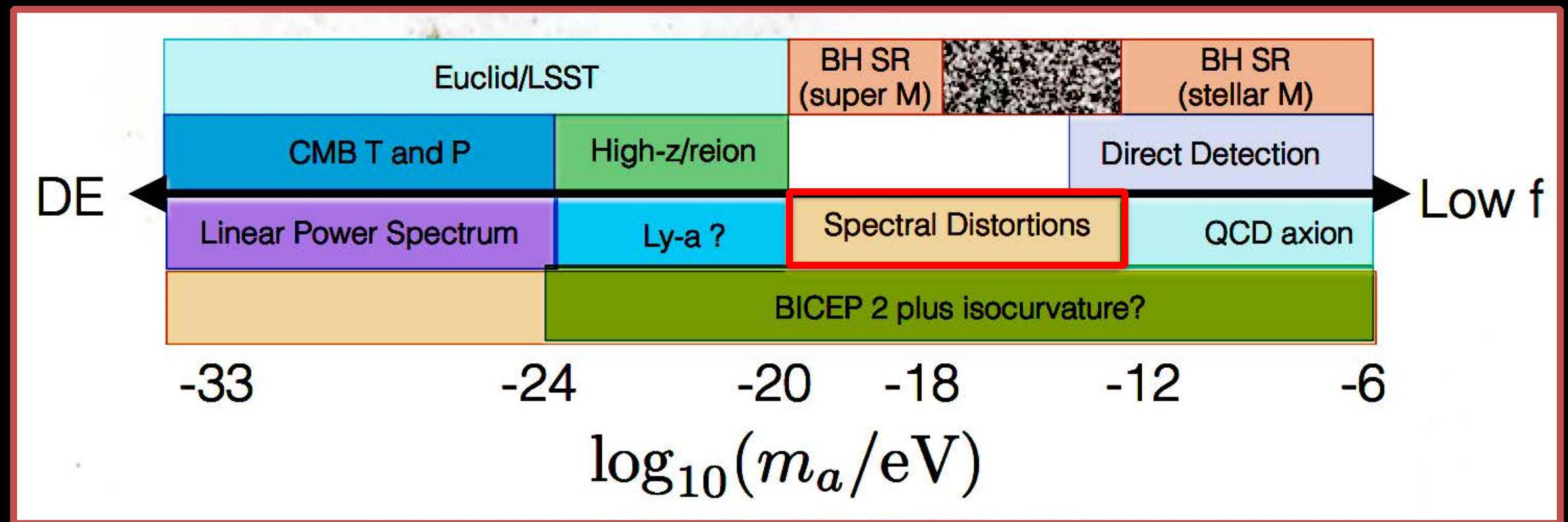


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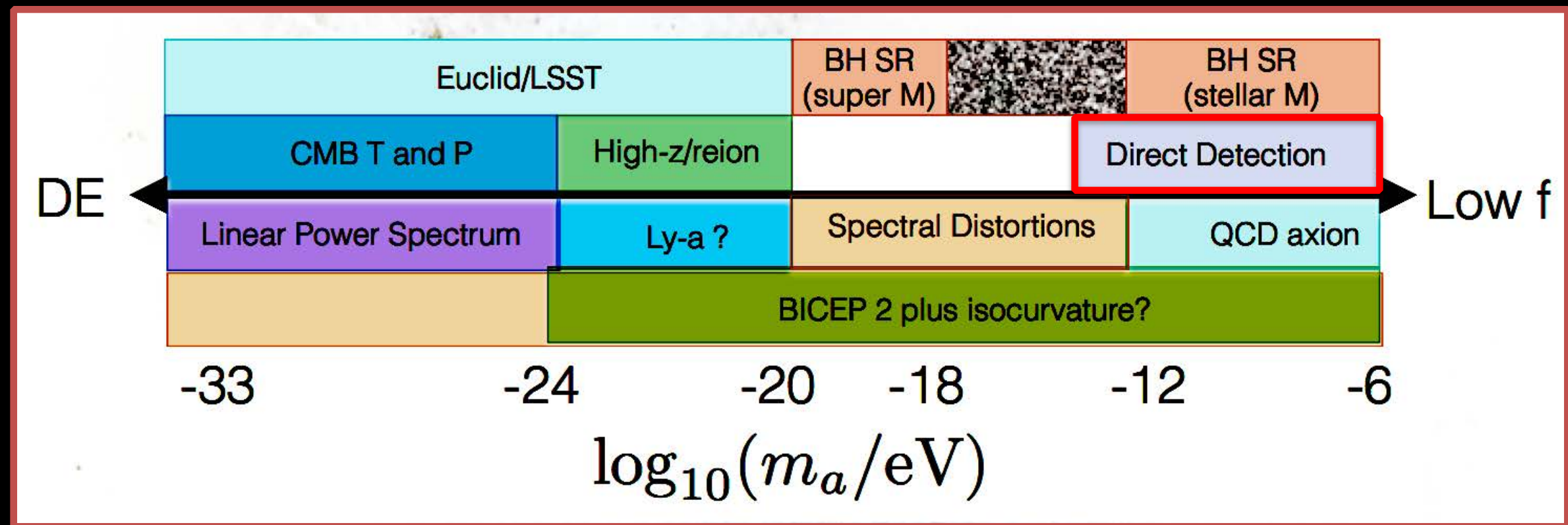


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DUST!

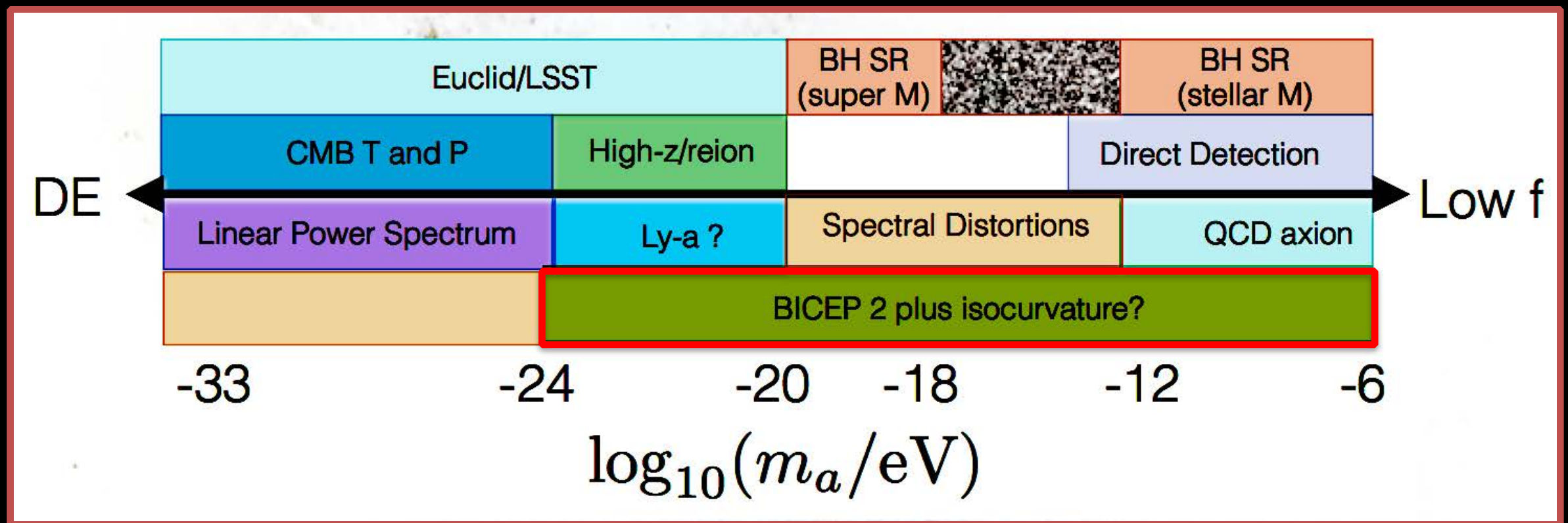


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Rough forecast

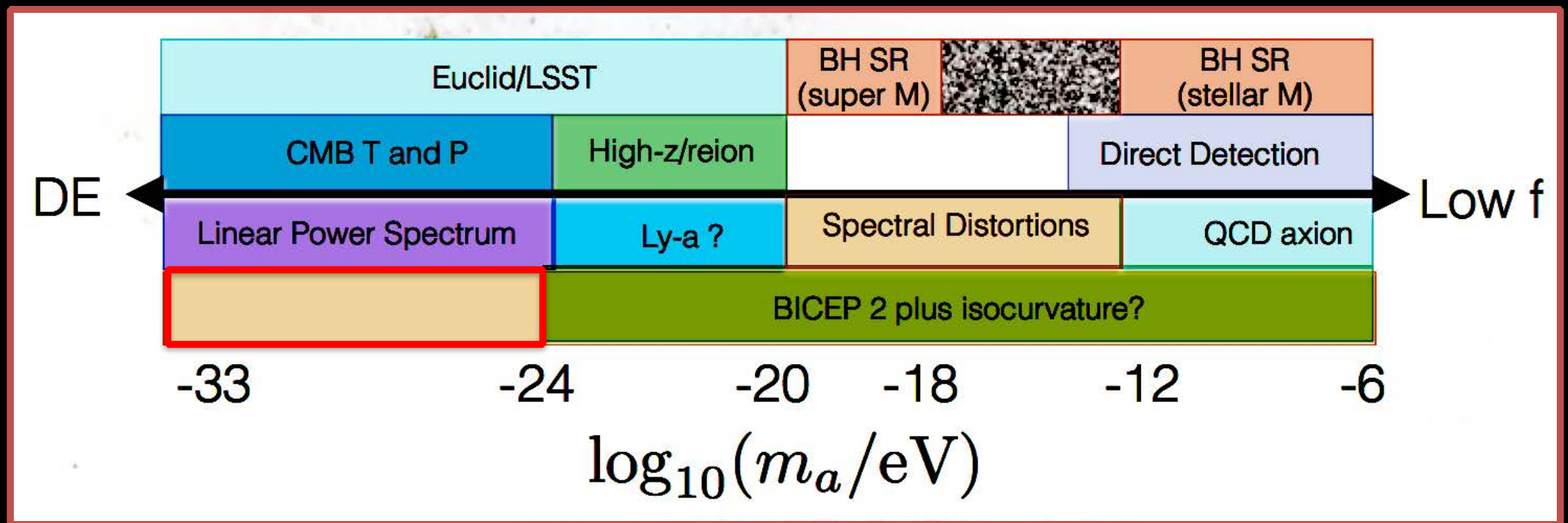


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IRONCLAD: this work

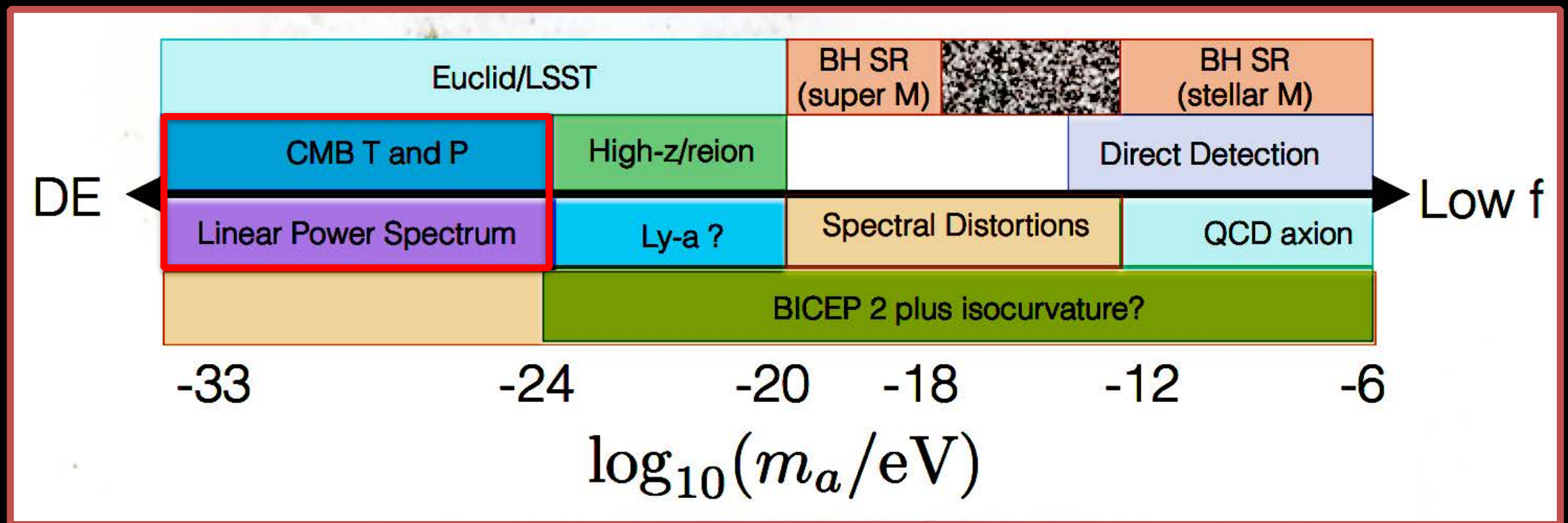


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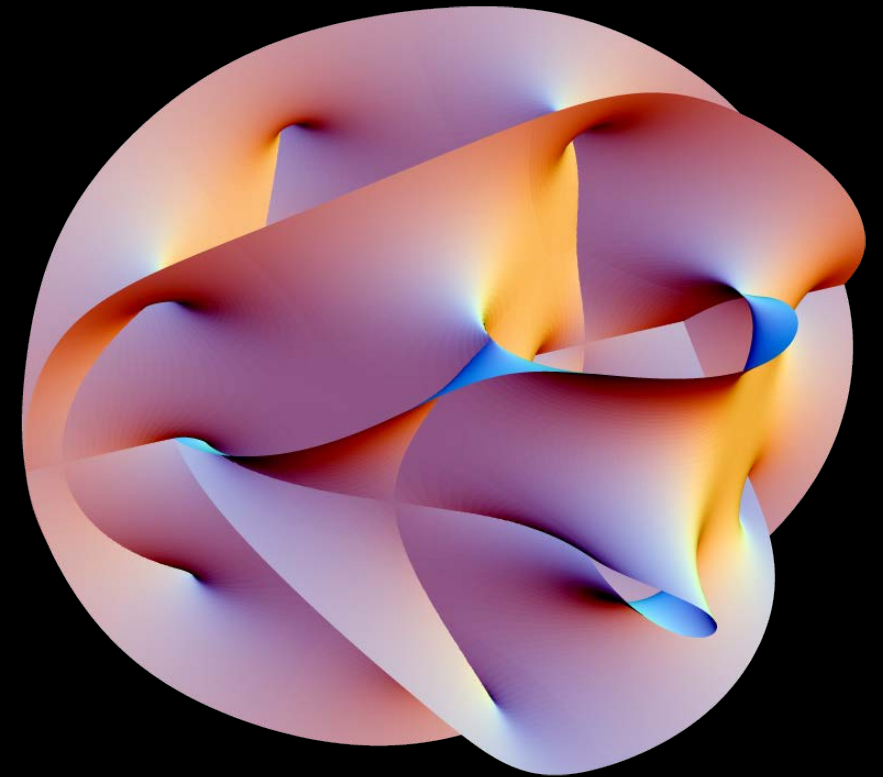
THE AXIVERSE: ULTRA-LIGHT AXIONS (ULAS)

- * Calabi-Yau manifolds

Many 2-cycles \longrightarrow Many axions

Hundreds!

- * Mass from non-perturbative physics
(instantons, D-branes)



$$m_a^2 = \frac{\mu^4}{f_a^2} e^{-\text{Volume}}$$

$$f_a \propto \frac{M_{\text{pl}}}{\text{Volume}}$$

$$\mathcal{L} \propto g_{a\gamma\gamma} \vec{E}_{\text{gauge}} \cdot \vec{B}_{\text{gauge}}$$
$$g_{a\gamma\gamma} \propto \frac{1}{f_a}$$

Also Witten and Svrcek (2006), Acharya et al. (2010), Cicoli (2012)

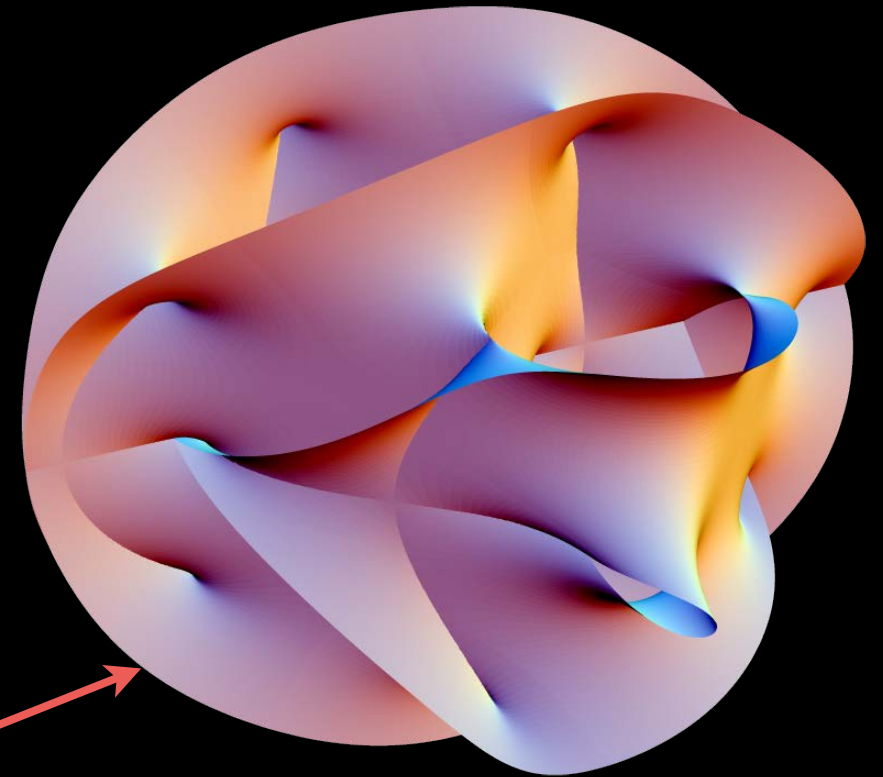
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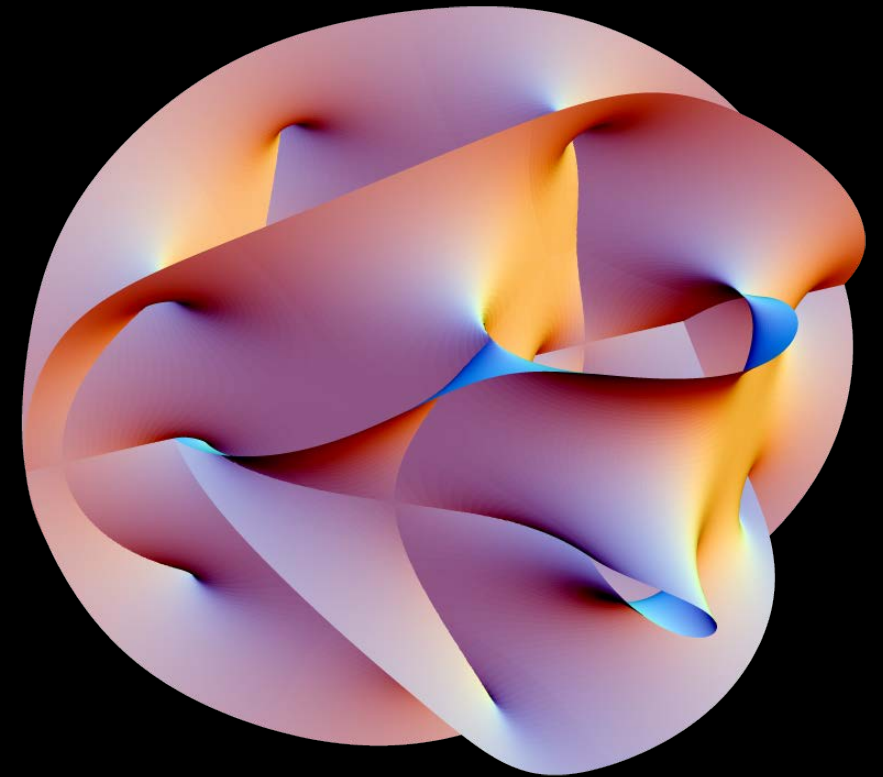
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New UV scale: not QCD scale

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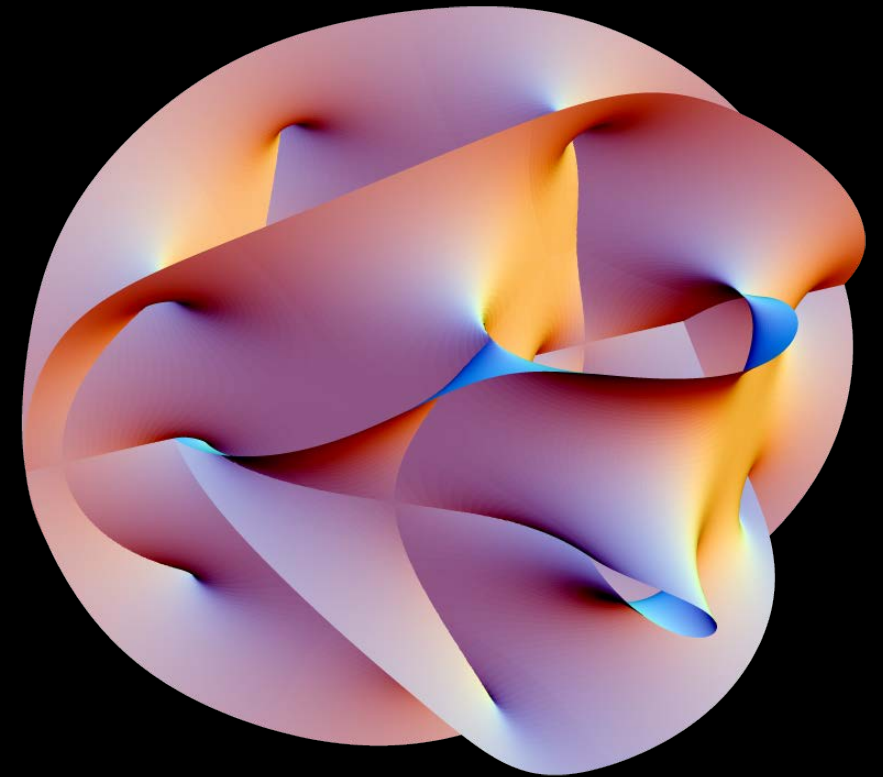
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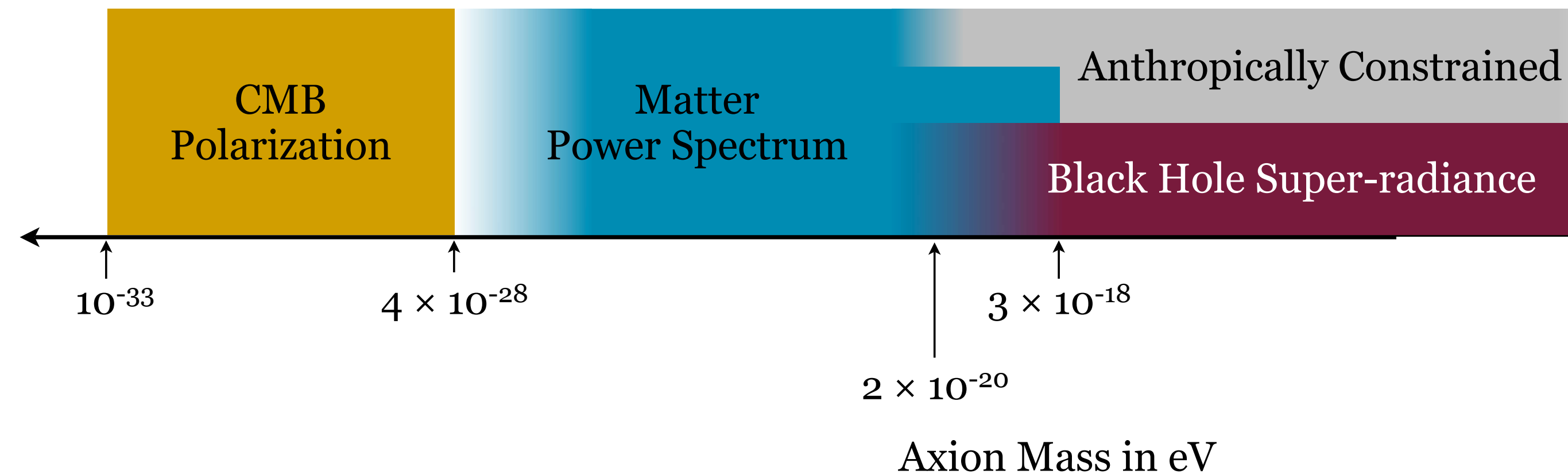
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Scalars with approximate shift symmetry \longrightarrow "Axion"

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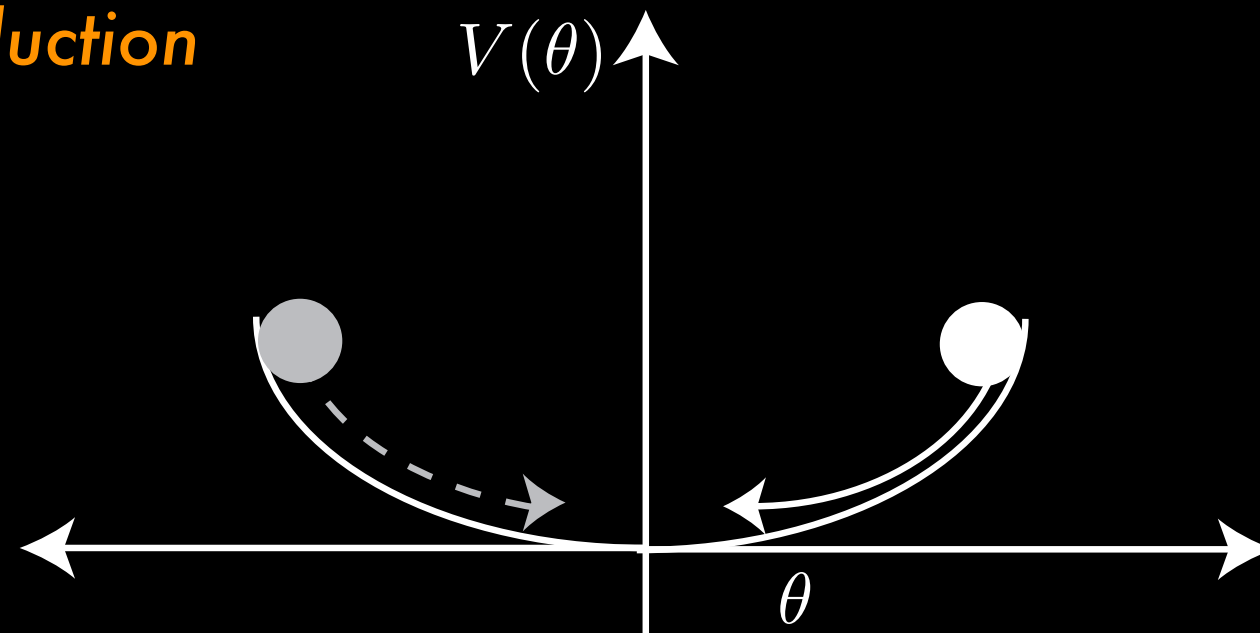


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COSMOLOGICAL AXION EVOLUTION

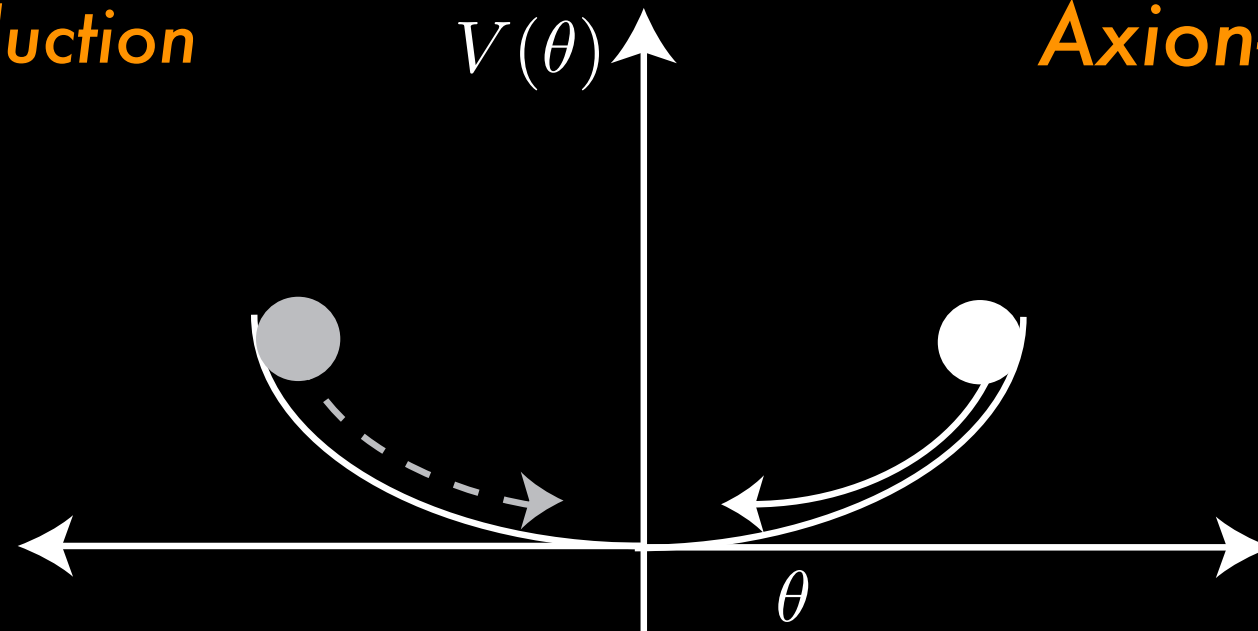
Misalignment production



COSMOLOGICAL AXION EVOLUTION

Misalignment production

Axion-driven acceleration

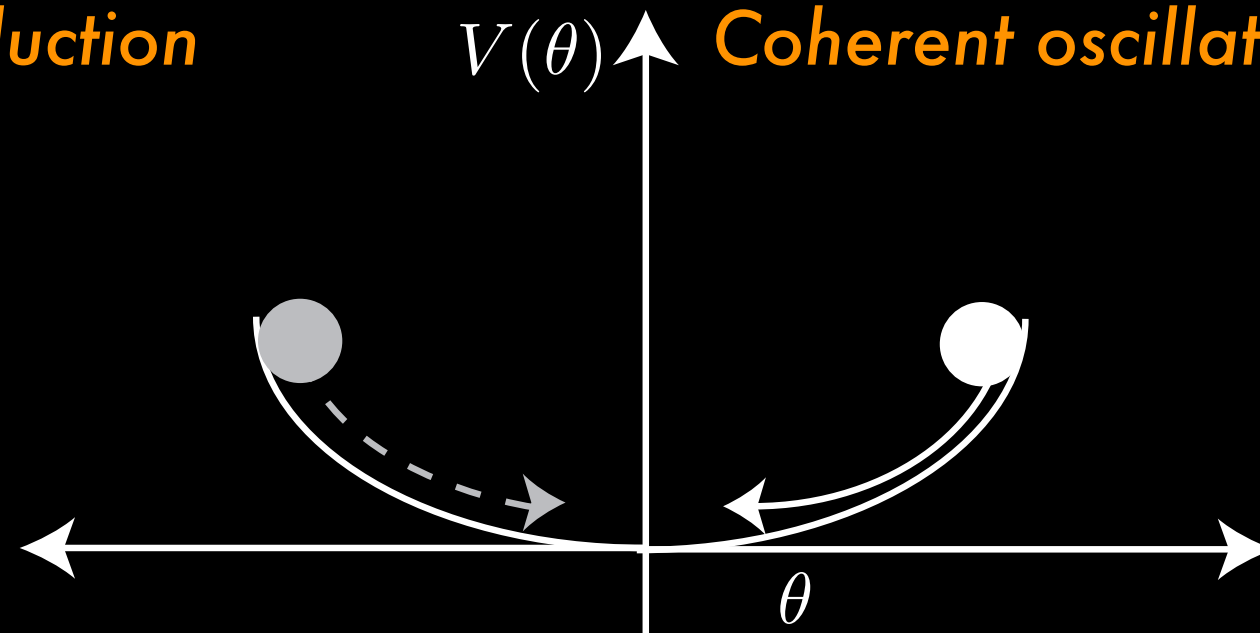


$$m \ll 3H \rightarrow n_a \propto \text{const}, w_a \equiv \frac{P_a}{\rho_a}, w_a \simeq -1$$

$$m \gg 3H \rightarrow n_a \propto a^{-3}, \langle w_a \rangle_{T=2\pi/m_a} = 0$$

COSMOLOGICAL AXION EVOLUTION

Misalignment production



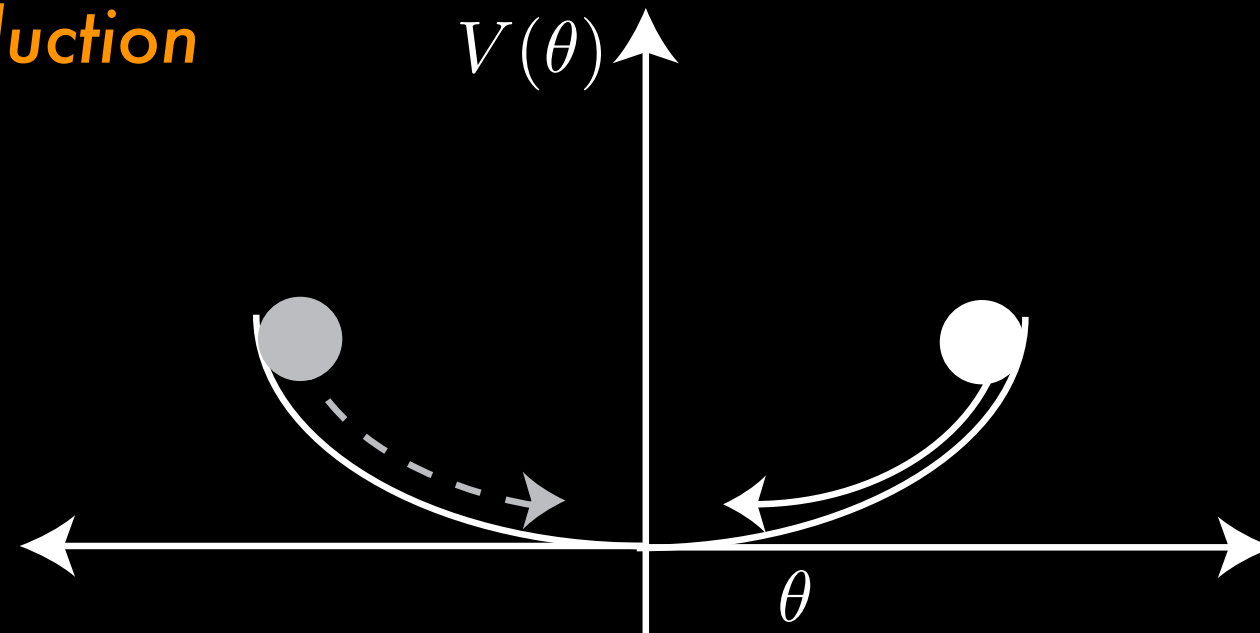
Coherent oscillation, Axions act like CDM

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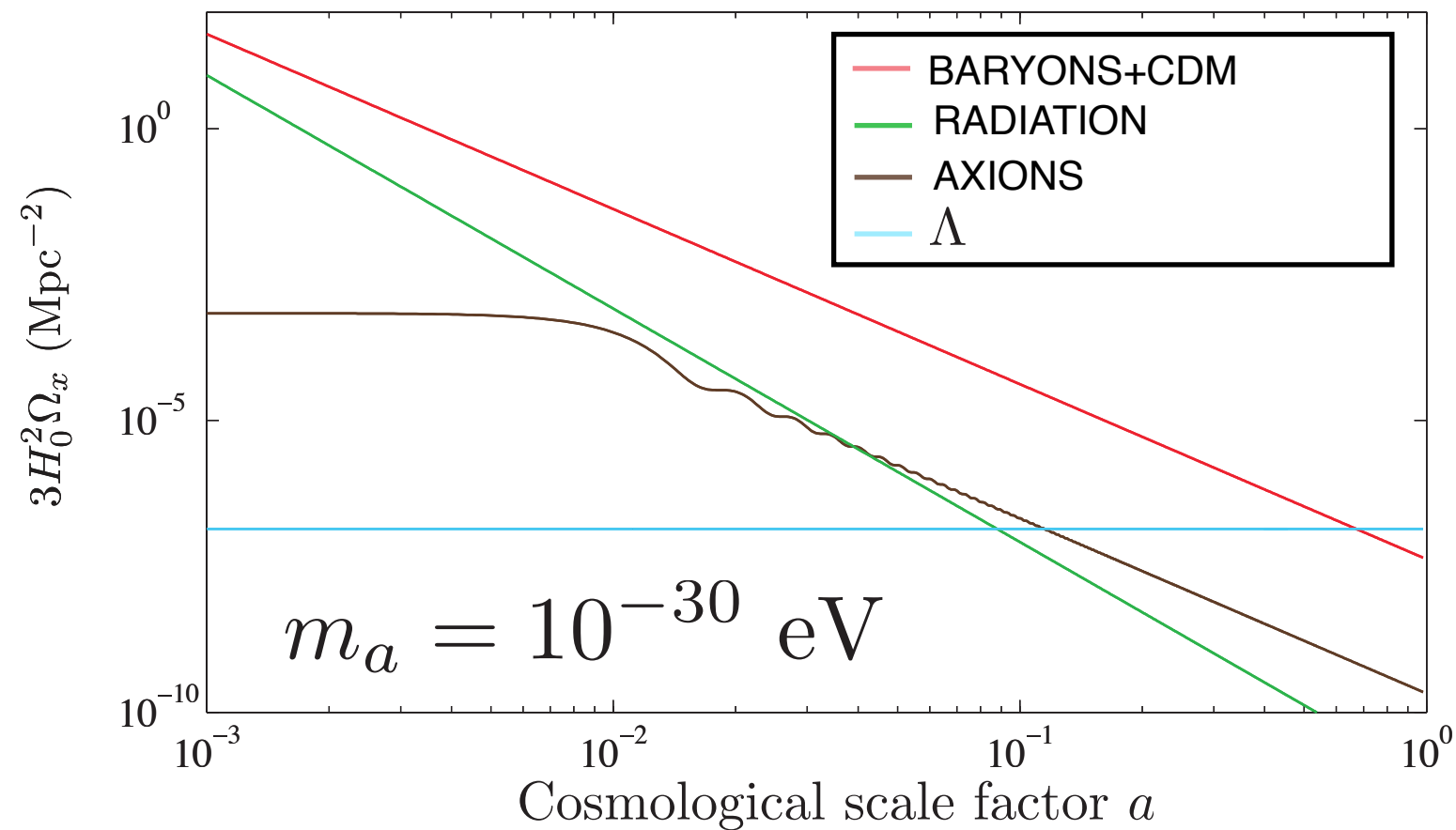


For QCD axion, we have a CDM candidate!

$$\Omega_{\text{mis}} h^2 = 0.236 \langle \theta_i^2 f(\theta_i) \rangle \left(\frac{m_a}{6.2 \mu\text{eV}} \right)^{-7/6}$$

COSMOLOGICAL AXION EVOLUTION

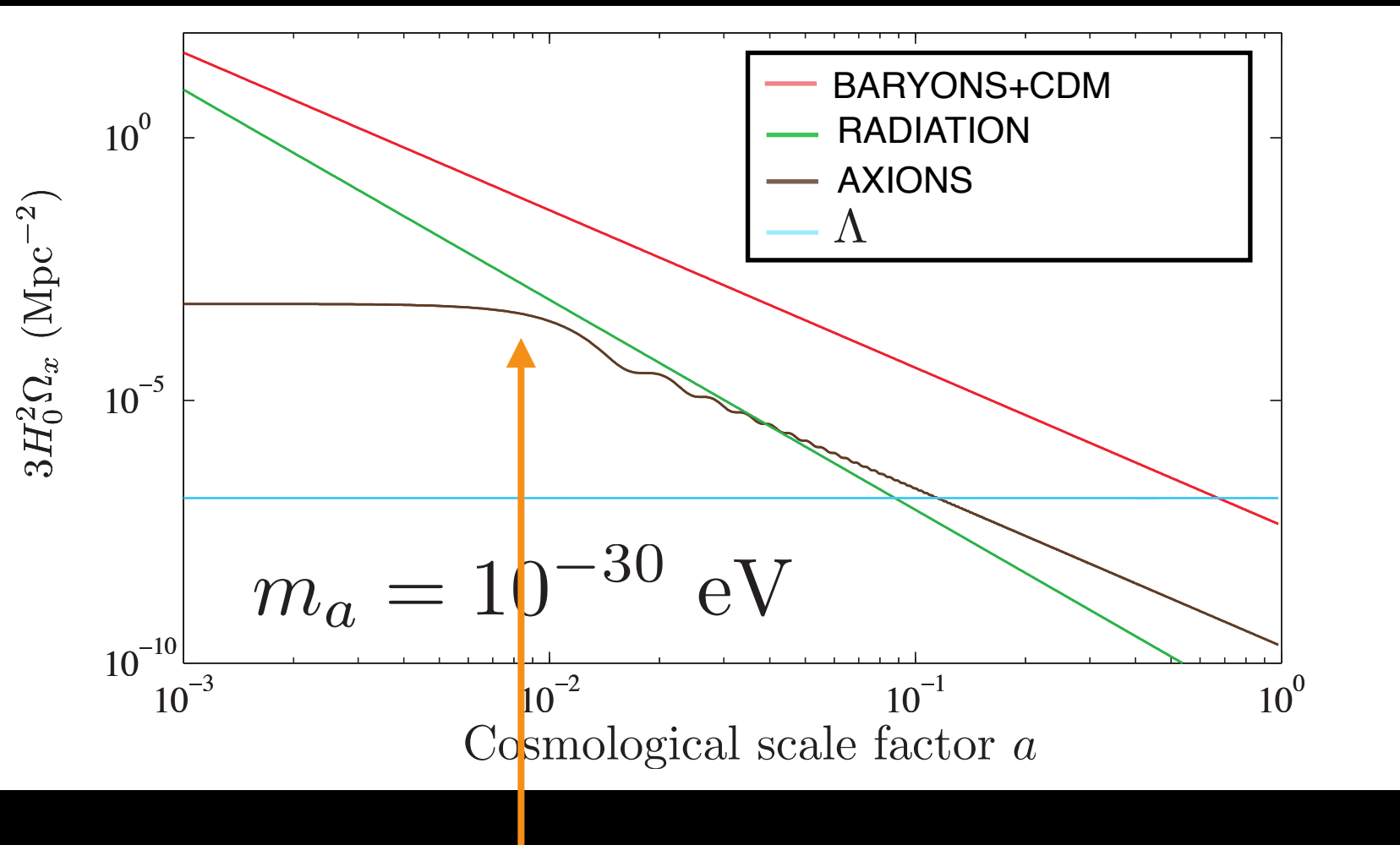
Different parameter space for non-QCD axion (Frieman et al 1995, Coble et al. 2007)



$$10^{-33} \text{ eV} < m_a < 10^{-18} \text{ eV}$$

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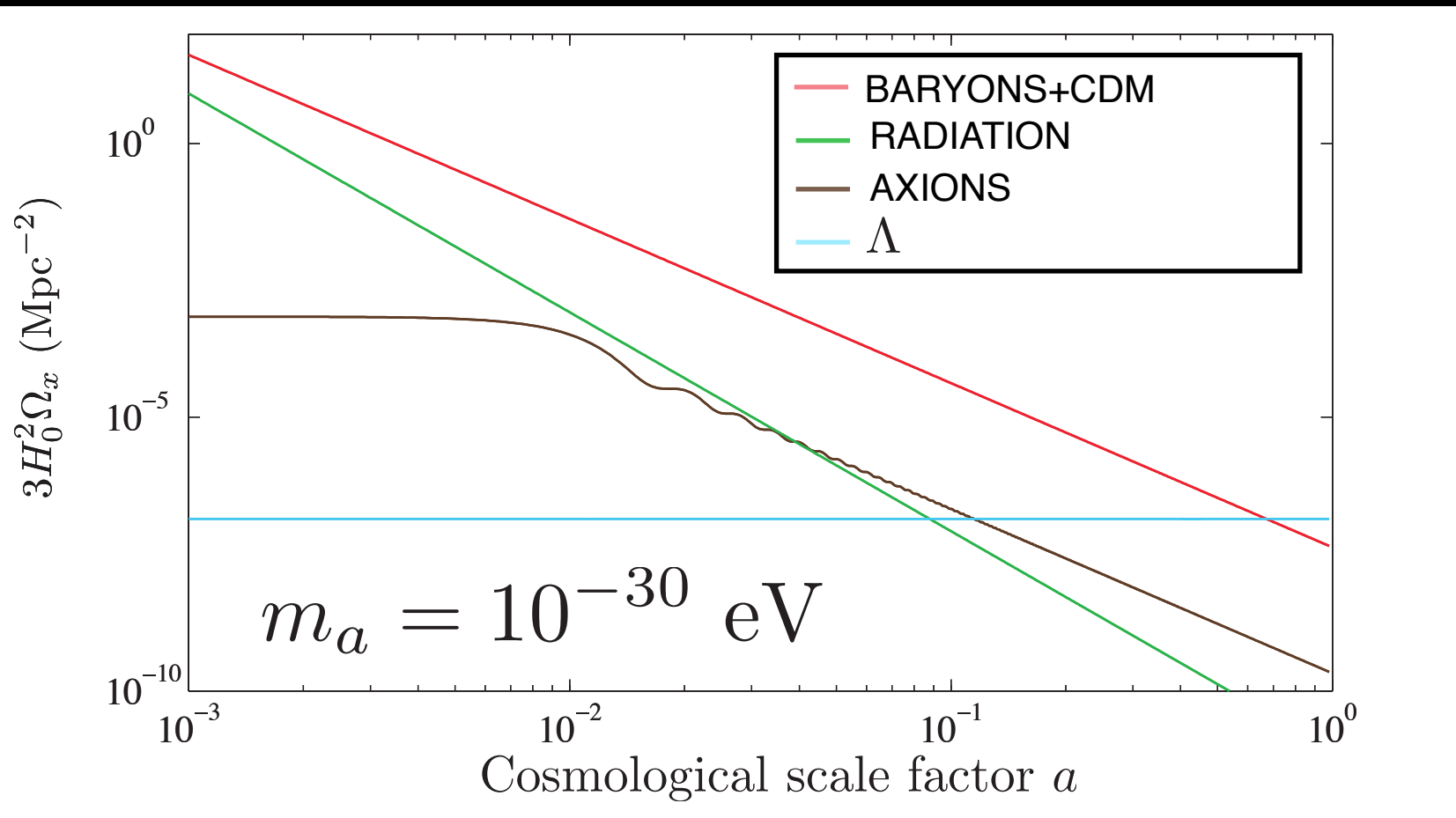


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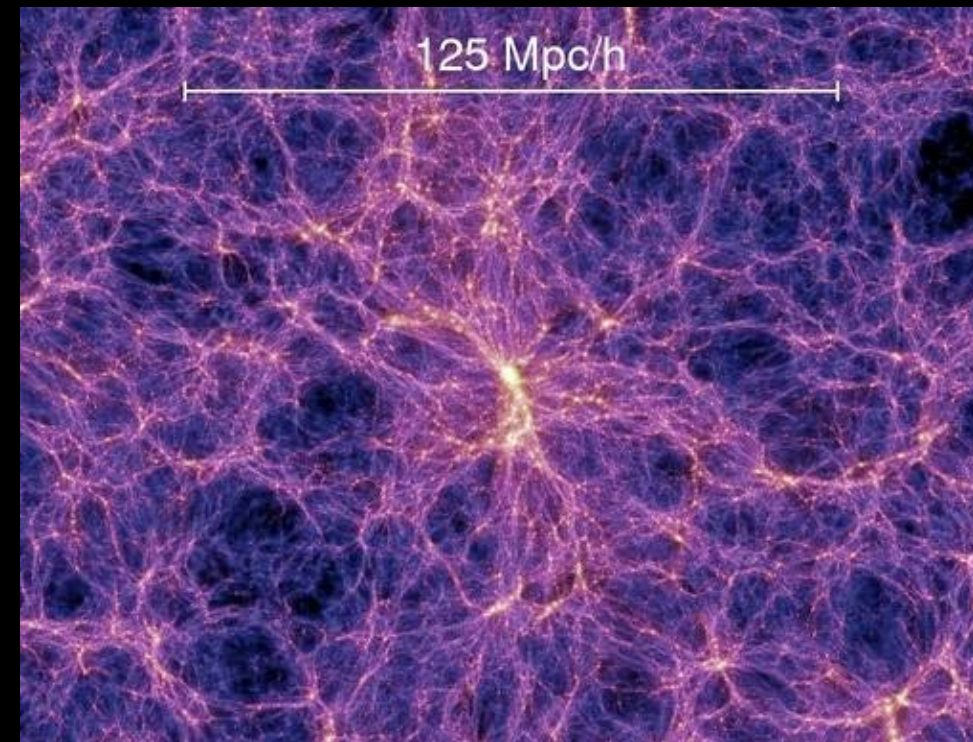
$$a \equiv a_{\text{osc}} \quad m_a = 3H(a)$$

COSMOLOGICAL AXION EVOLUTION

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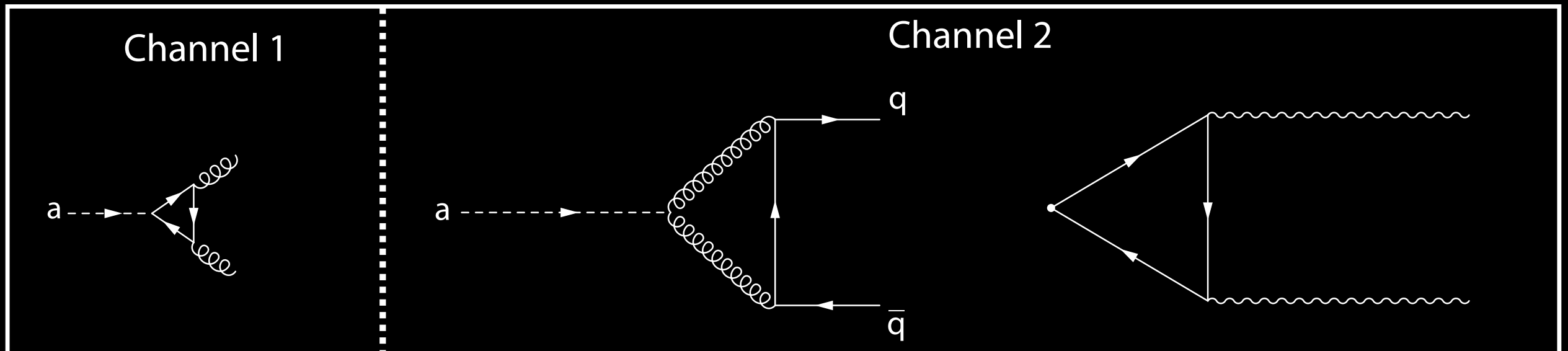
'DM' axions $a_{\text{osc}} < a_{\text{eq}}$ *Oscillation starts in time for struct. formation*

$$m_a > 10^{-27} \text{ eV}$$

DE axions $a_{\text{osc}} > a_{\text{eq}}$ *Oscillation starts too late for struct. formation*

$$m_a < 10^{-27} \text{ eV}$$

Two-photon coupling of axion



- * Axions interact weakly with SM particles $\Gamma, \sigma \sim \alpha^2$
- * Axions have a two-photon coupling

$$g_{a\gamma\gamma} = -\frac{3\alpha}{8\pi f_a} \xi$$

$$\mathcal{L} \propto g_{a\gamma\gamma} \vec{E} \cdot \vec{B}$$

- * Very little freedom once f_a specified

Axion Experiments/ Constraints

HOW TO LOOK FOR A QCD AXION



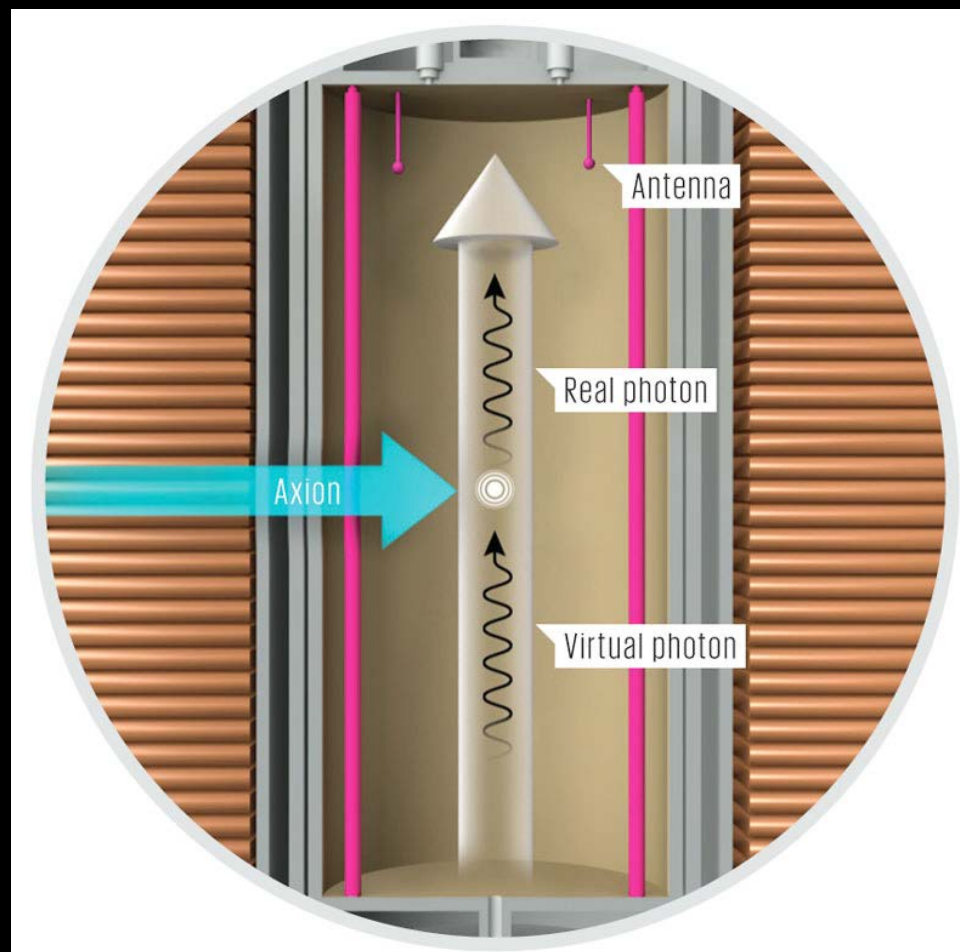
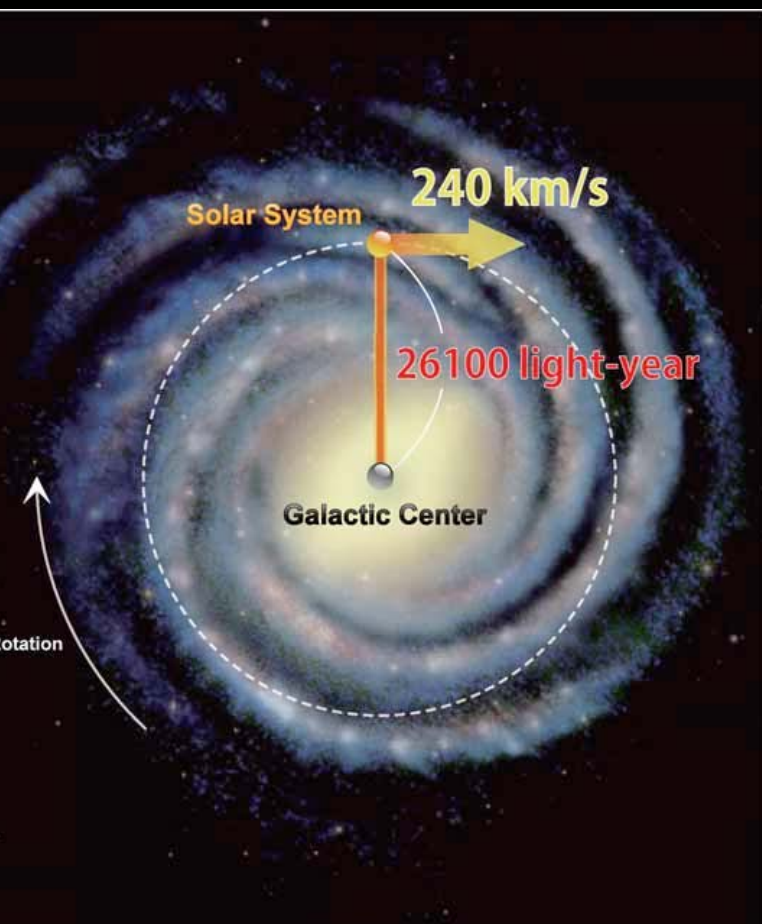
P. Sikivie 1983

***ADMX**: Use the DM axions the universe gives you

$$\mathcal{L} \propto g_{a\gamma\gamma} a \vec{E} \cdot \vec{B} \quad g_{a\gamma\gamma} \propto 1/f_a$$

$$E_\gamma = m_a c^2$$

Excite cavity TEM modes



HOW TO LOOK FOR A QCD AXION



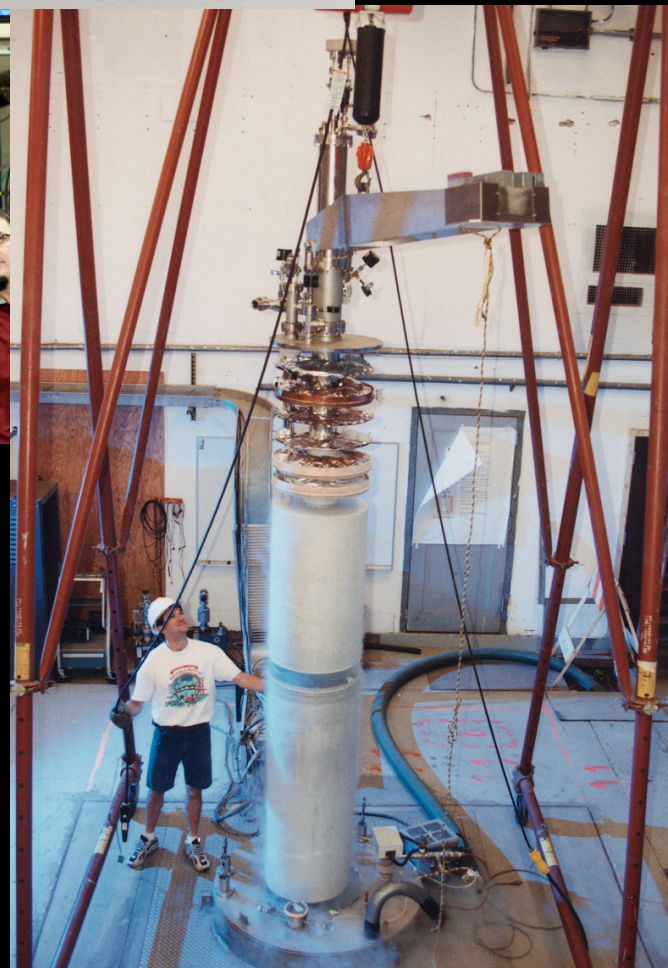
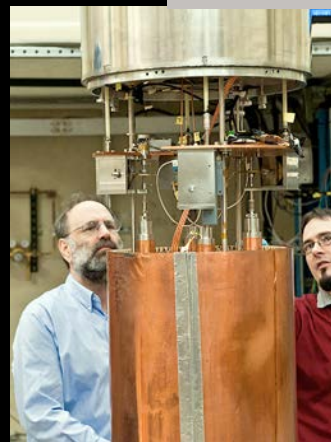
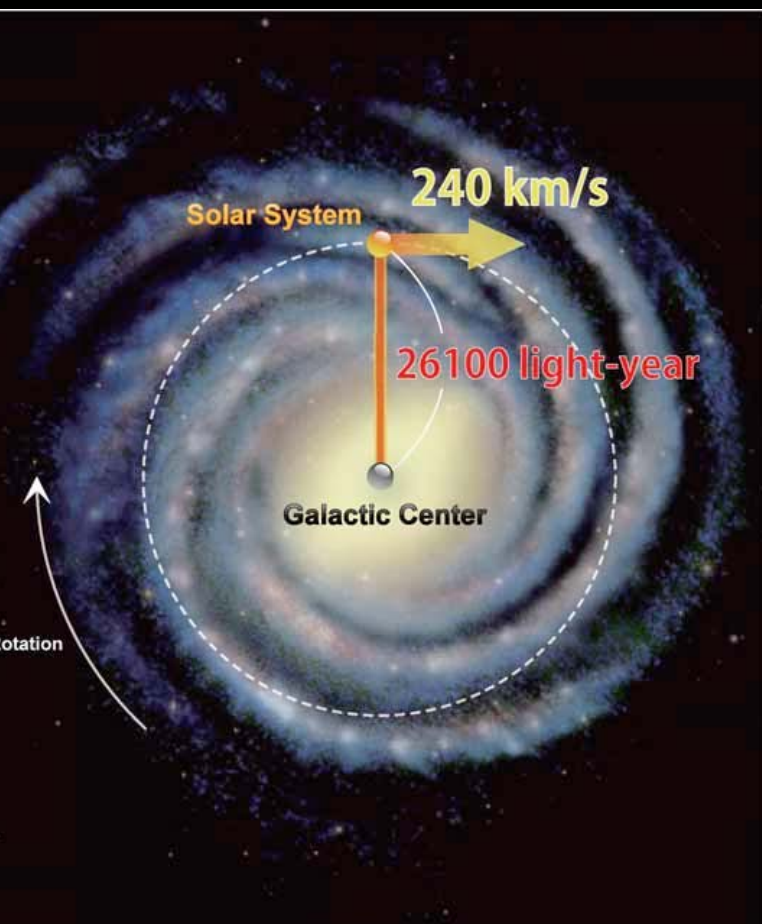
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L. Rosenberg and G. Rybka +....



HOW TO LOOK FOR AXIONS

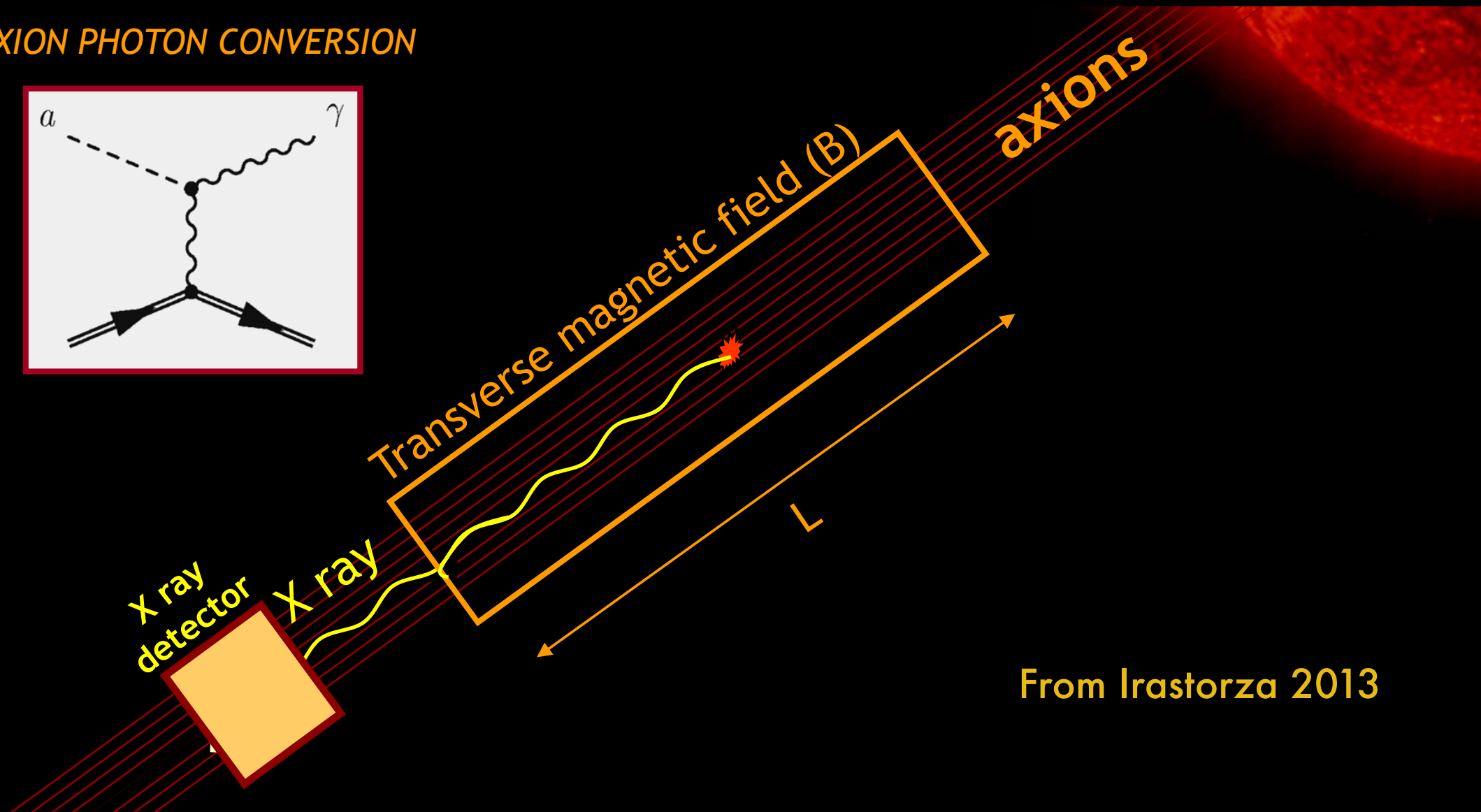
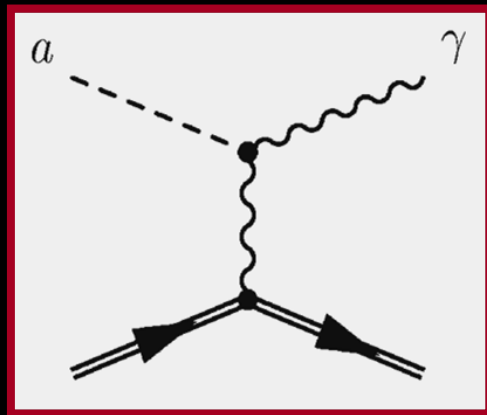
✳ By construction, axions interact with photons $g_{a\gamma\gamma} = -\frac{3\alpha\xi}{2\pi f_a}$

$g_{a\gamma\gamma} \text{ (GeV}^{-1}\text{)}$

HOW TO LOOK FOR AXIONS

✴ By construction, axions interact with photons $g_{a\gamma\gamma} = -\frac{3\alpha\xi}{2\pi f_a}$

AXION PHOTON CONVERSION



From Irastorza 2013

Make them in stars—Turn them back into photons on Earth!
CAST/IAXO experiments

HOW TO LOOK FOR AXIONS

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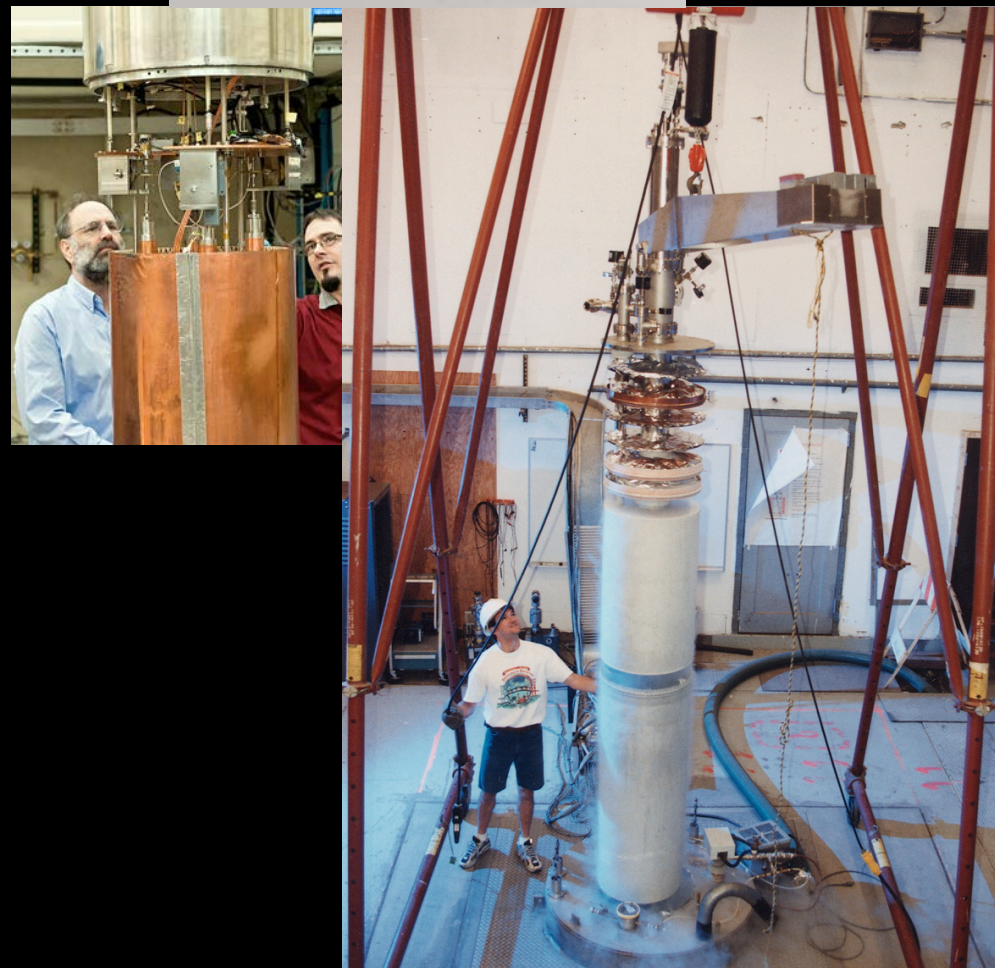
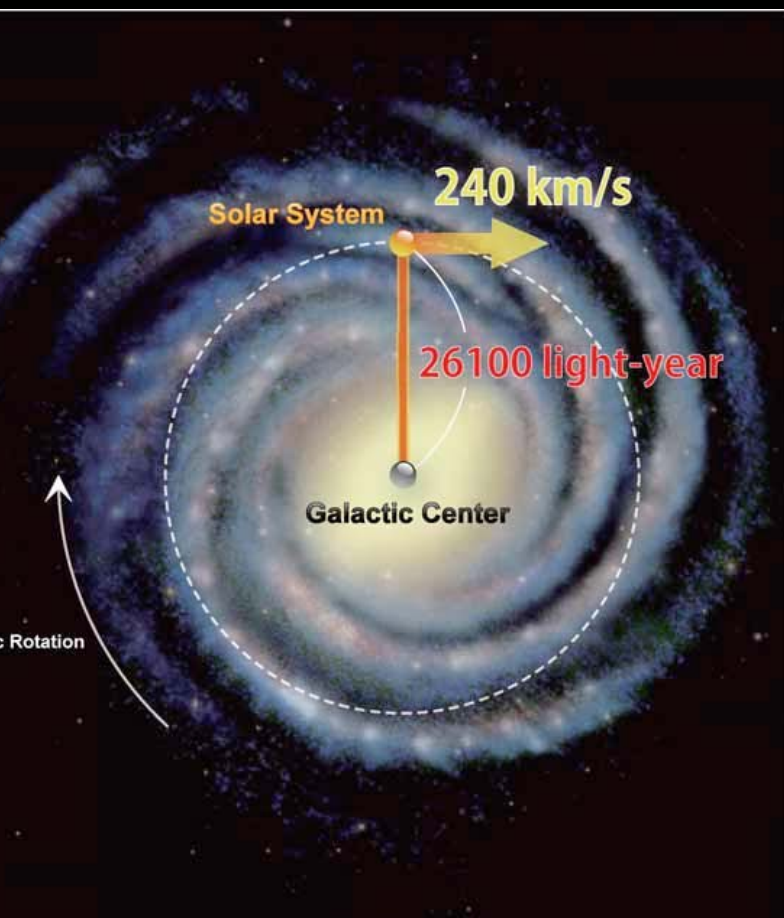
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Use the dark matter in the universe!

Pierre Sikivie



$g_{a\gamma\gamma} \text{ (GeV}^{-1}\text{)}$



HOW TO LOOK FOR A QCD AXION



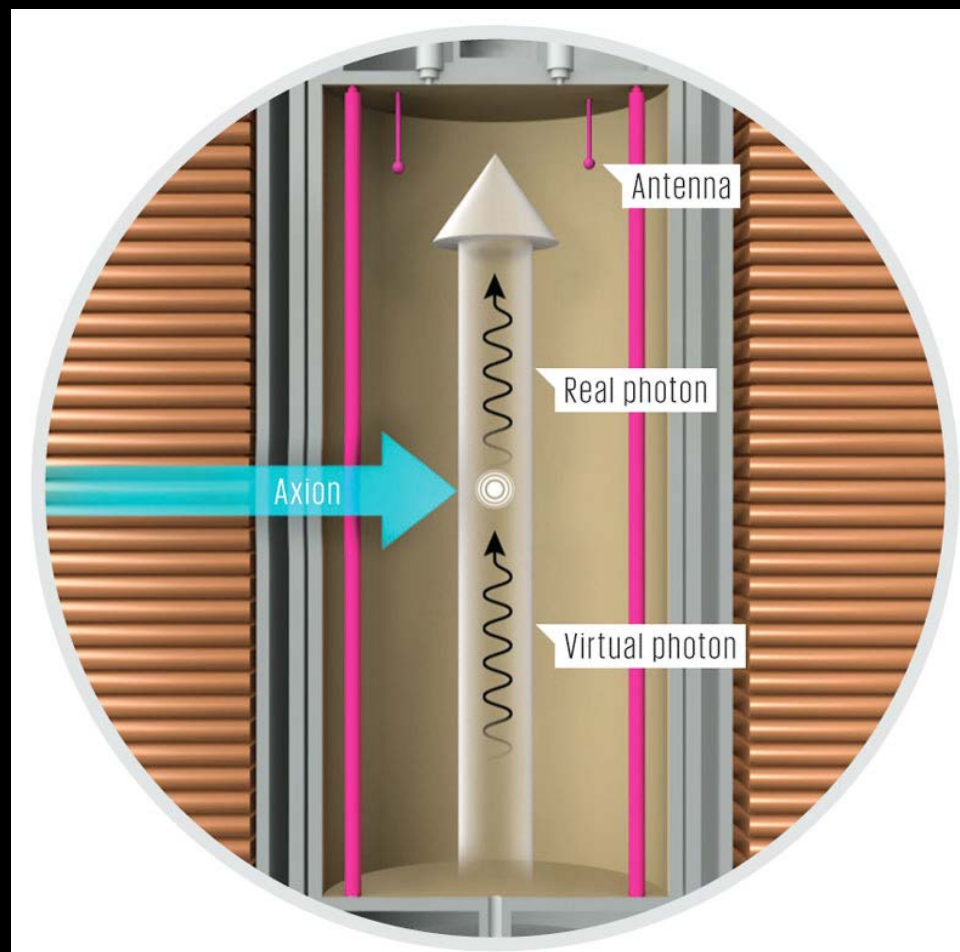
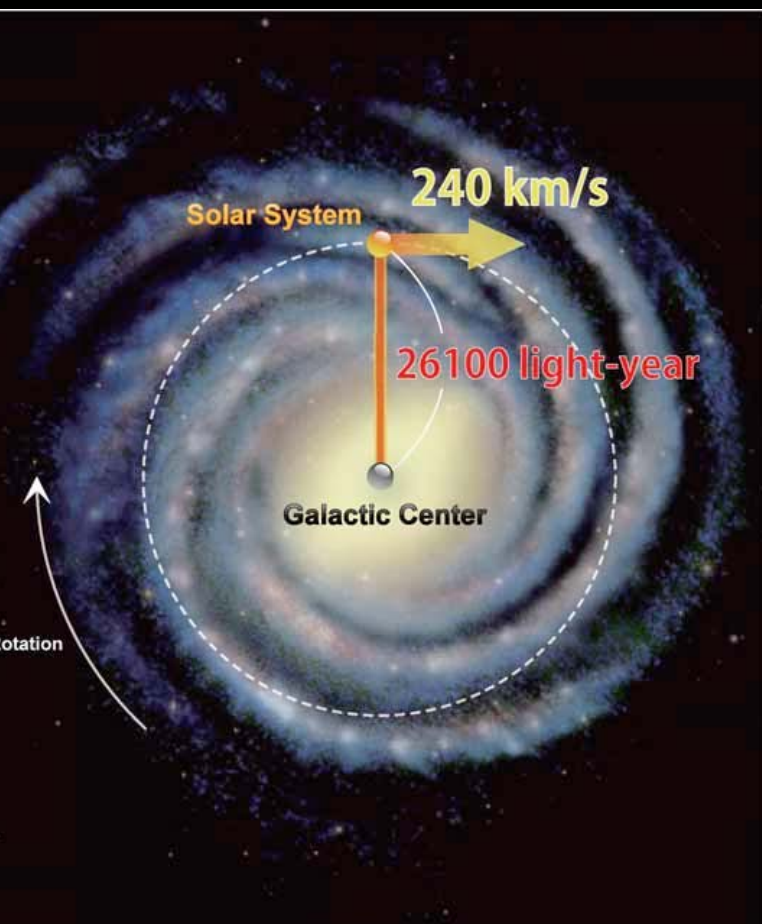
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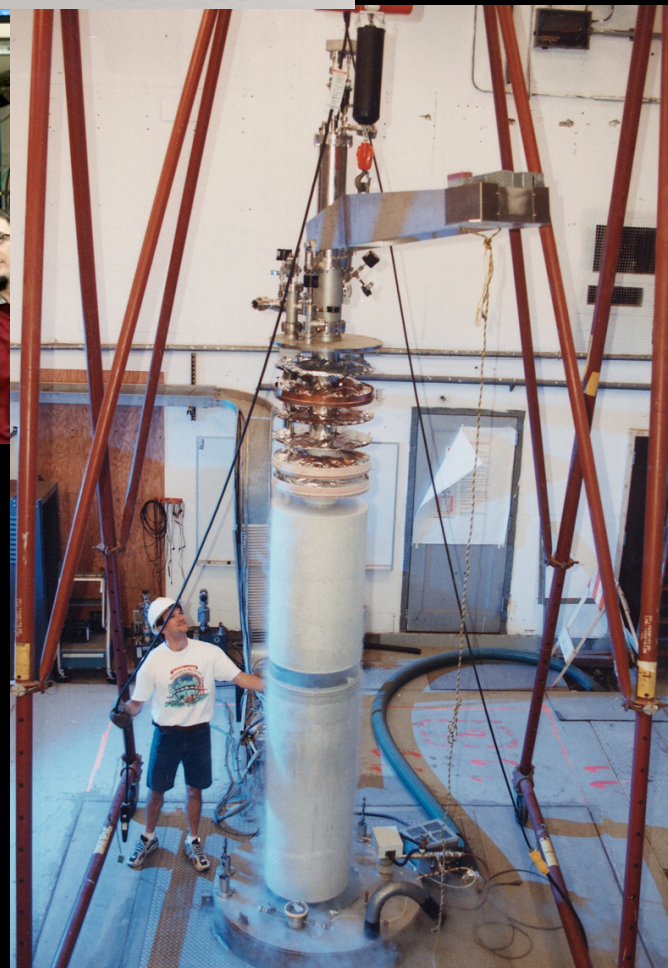
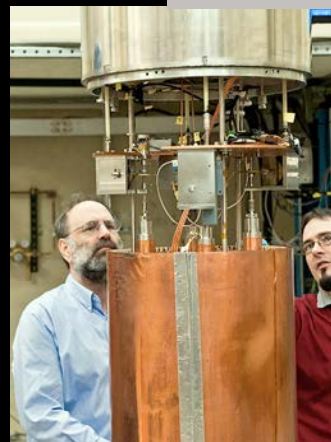
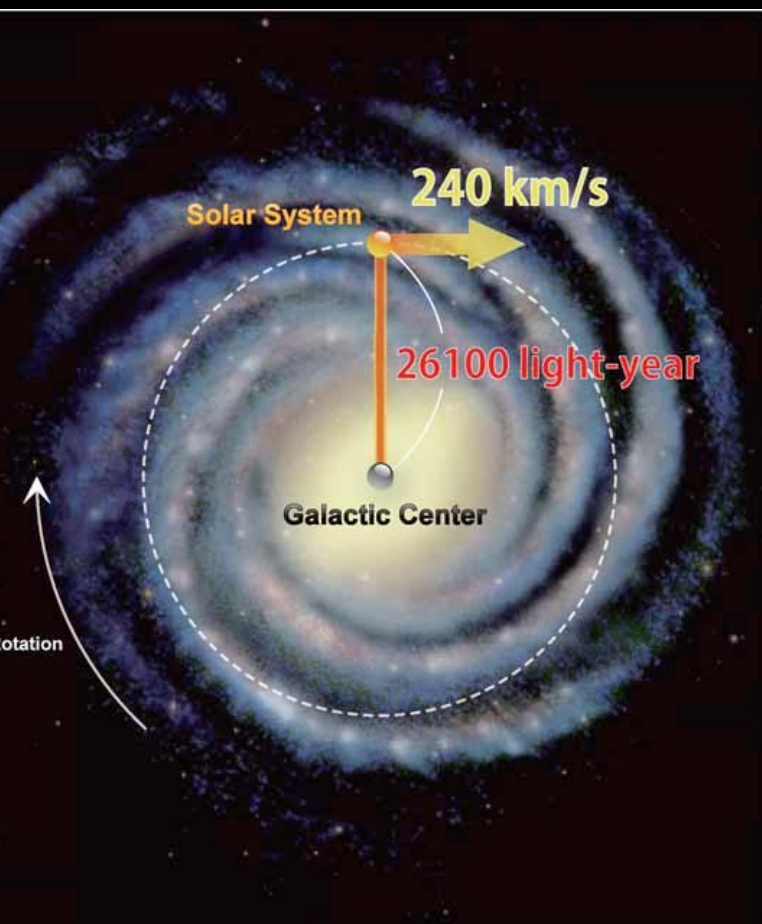
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HOW TO LOOK FOR AXIONS

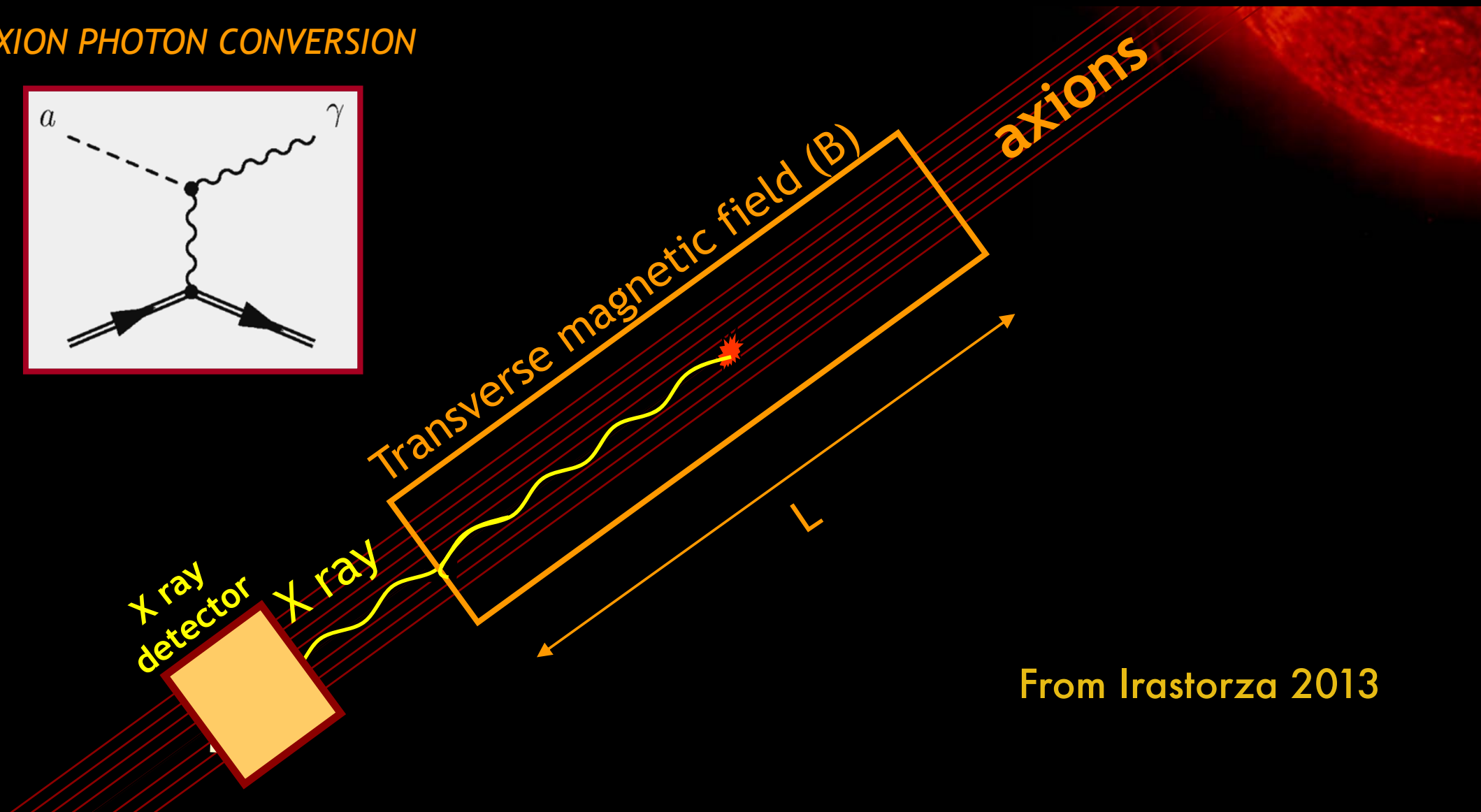
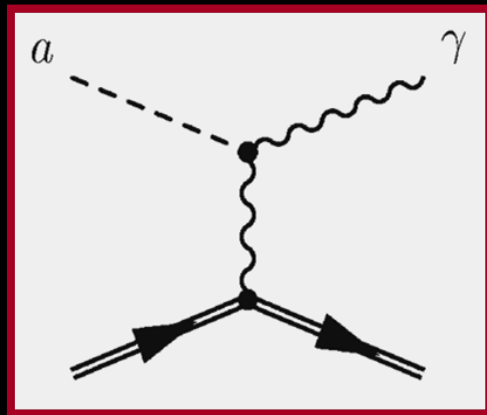
✧ By construction, axions interact with photons

$$g_{a\gamma\gamma} \text{ (GeV}^{-1}\text{)}$$

HOW TO LOOK FOR AXIONS

✴ By construction, axions interact with photons

AXION PHOTON CONVERSION



From Irastorza 2013

Make them in stars—Turn them back into photons on Earth!
CAST/IAXO experiments

HOW TO LOOK FOR AXIONS

✴ By construction, axions interact with photons



Pierre Sikivie



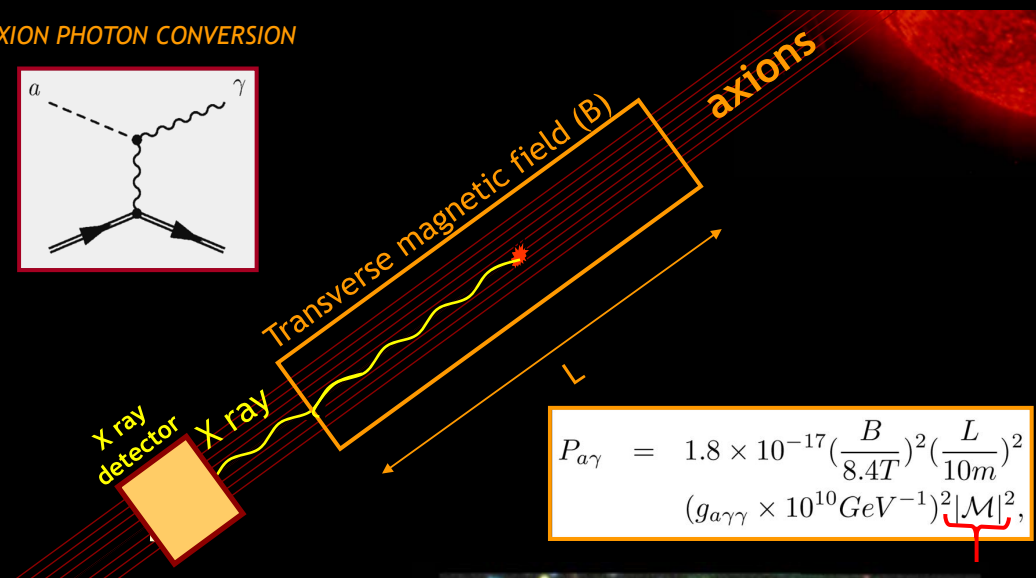
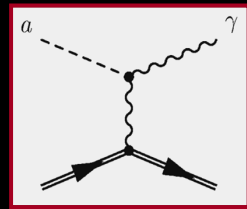
Sunset
Detectors

Sunrise
Detectors

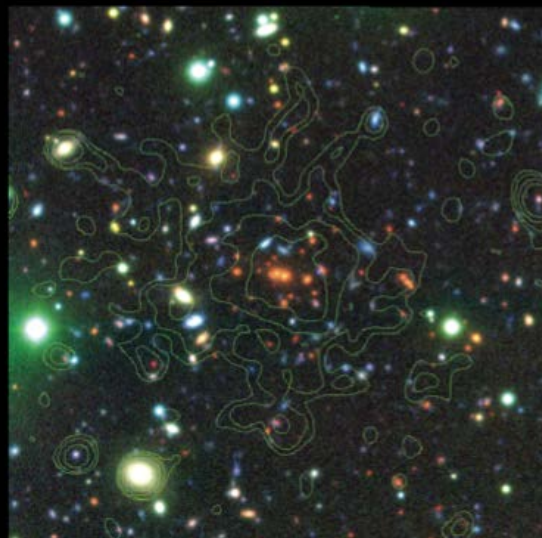
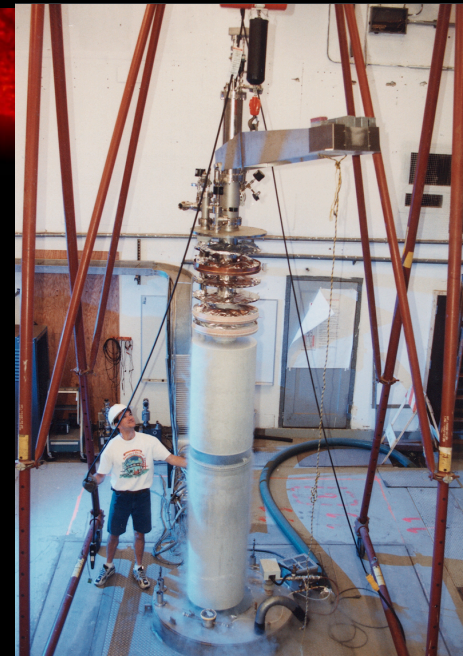
Make them in stars—Turn them back into photons on Earth!
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Limits and horizon

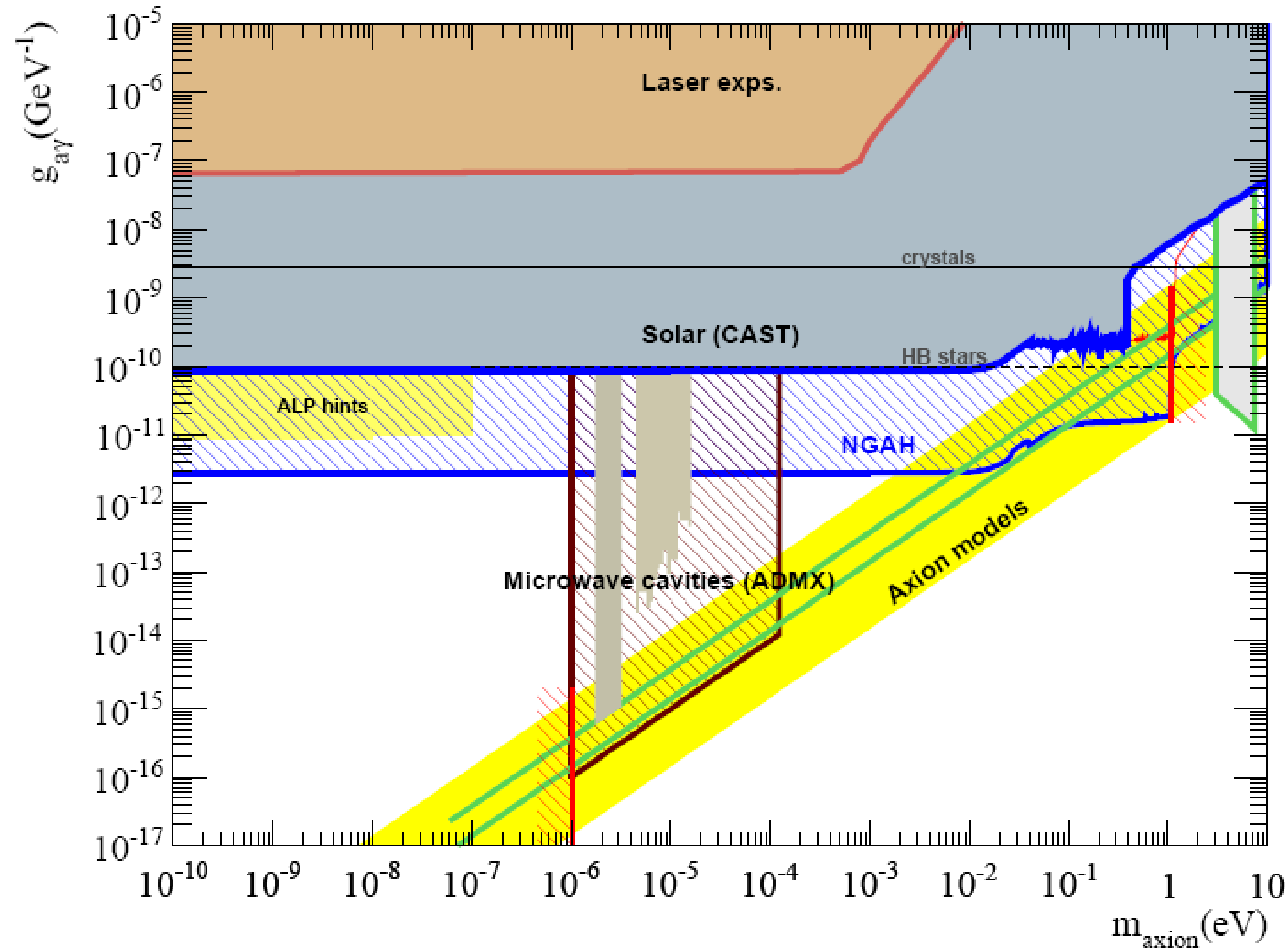
AXION PHOTON CONVERSION



$$P_{a\gamma} = 1.8 \times 10^{-17} \left(\frac{B}{8.4T} \right)^2 \left(\frac{L}{10m} \right)^2 (g_{a\gamma\gamma} \times 10^{10} GeV^{-1})^2 |\mathcal{M}|^2,$$

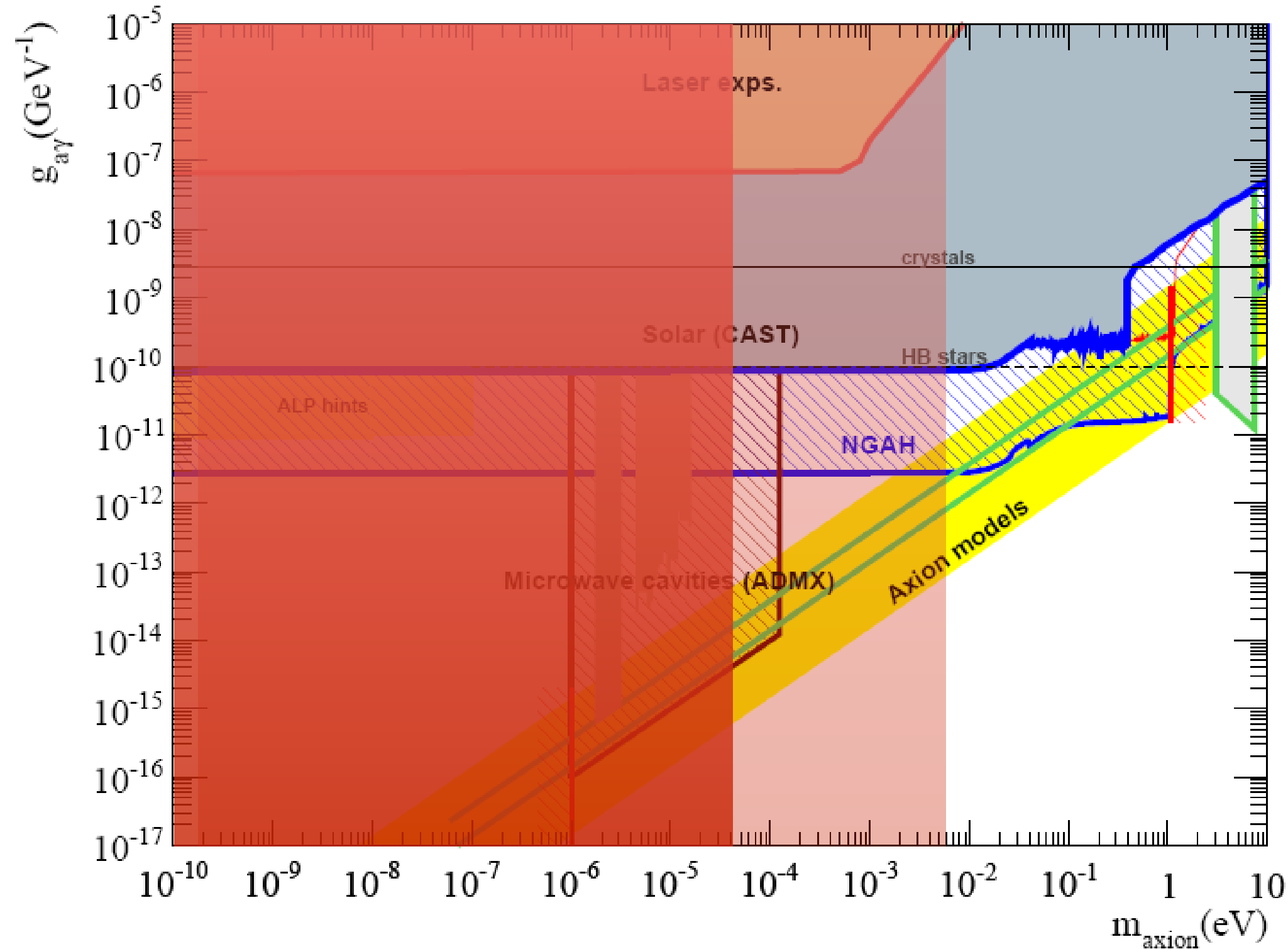


Limits and horizon

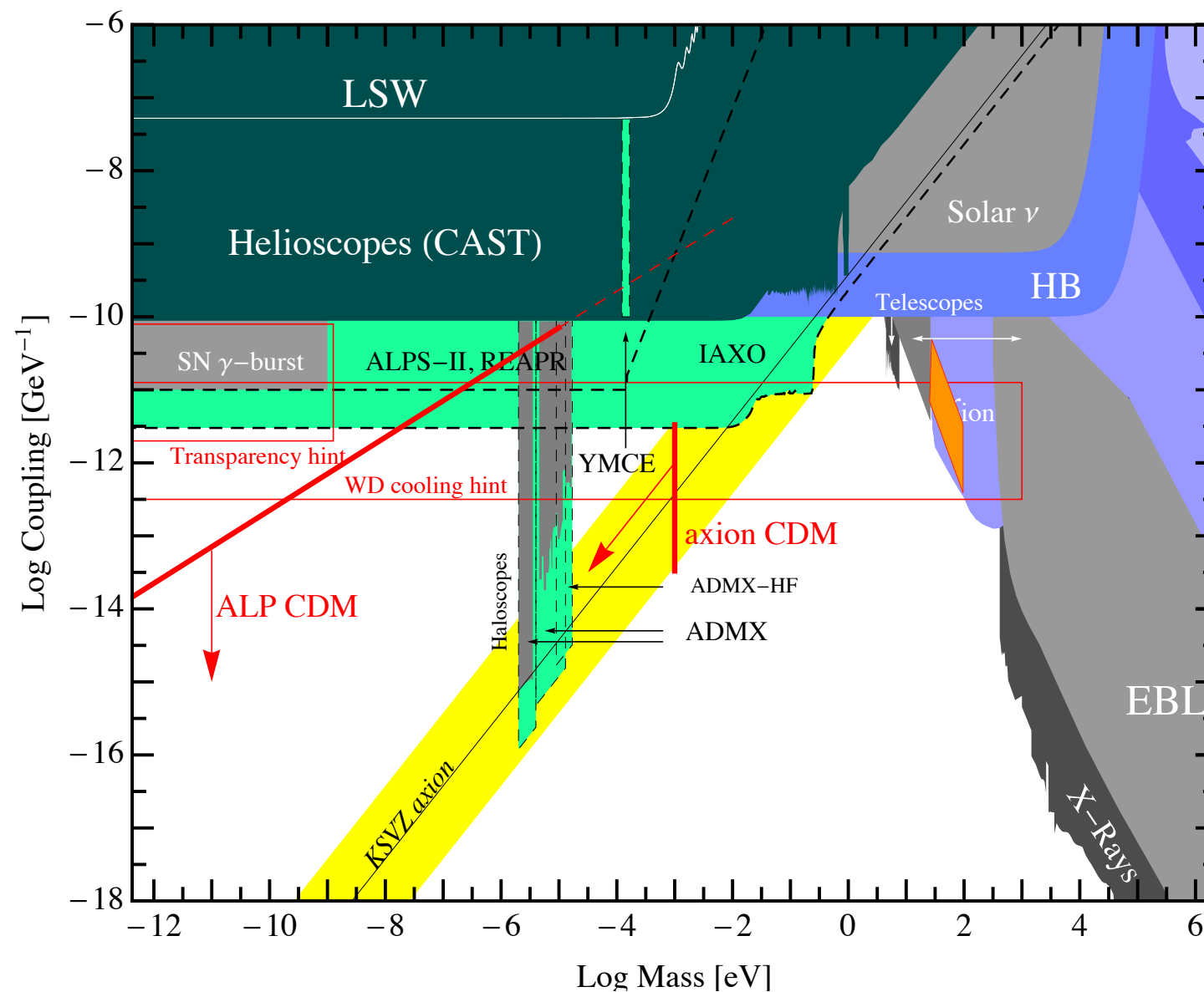


Limits and horizon

Cosmological abundance limits (more soon...)



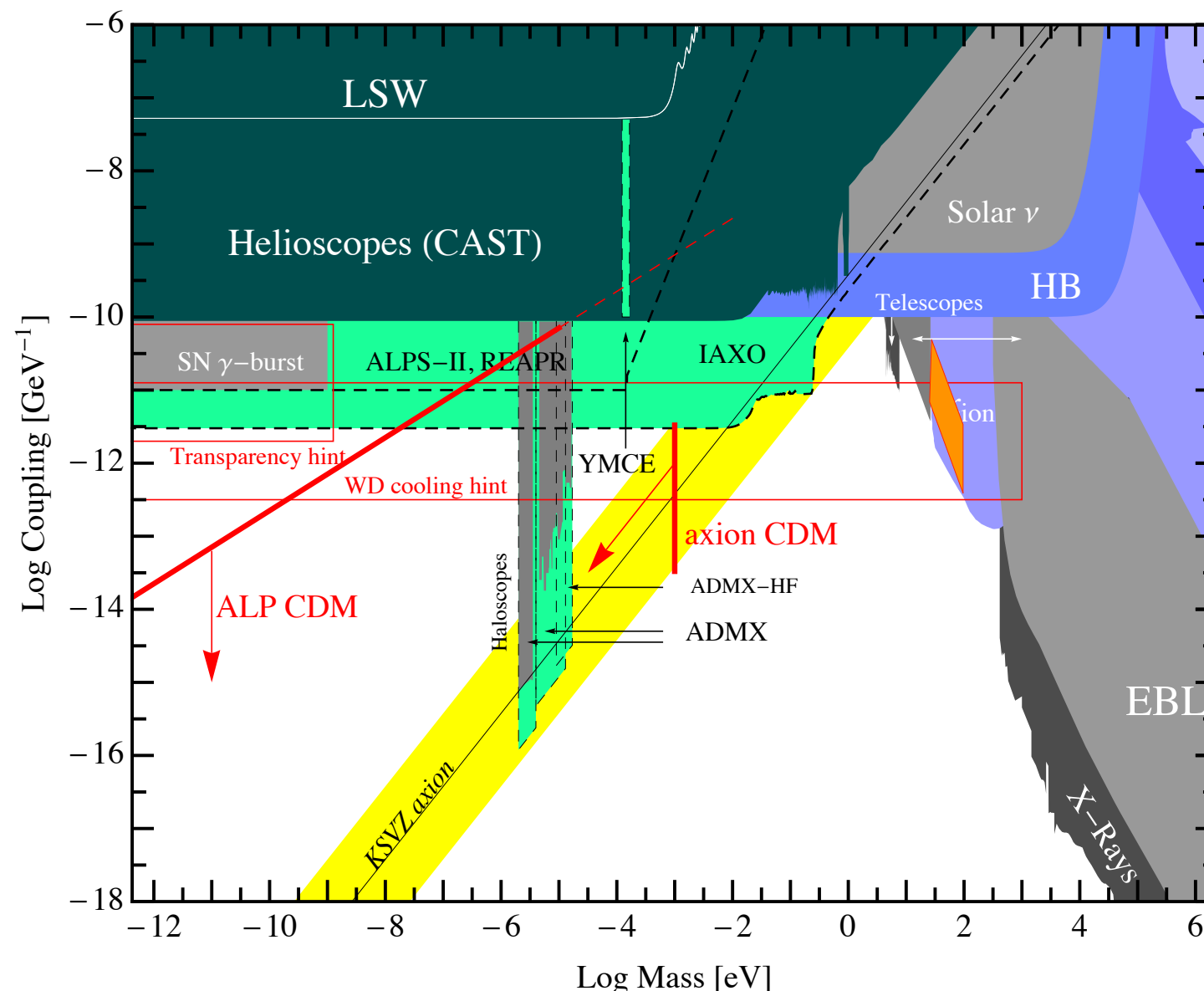
Experimental constraints ULA and axion-like particles (ALPs)



$$\mathcal{L} \propto g_{a\gamma\gamma} \vec{E} \cdot \vec{B}$$

Experimental constraints ULA and axion-like particles (ALPs)

Experimental desert: Gravitational constraints essential

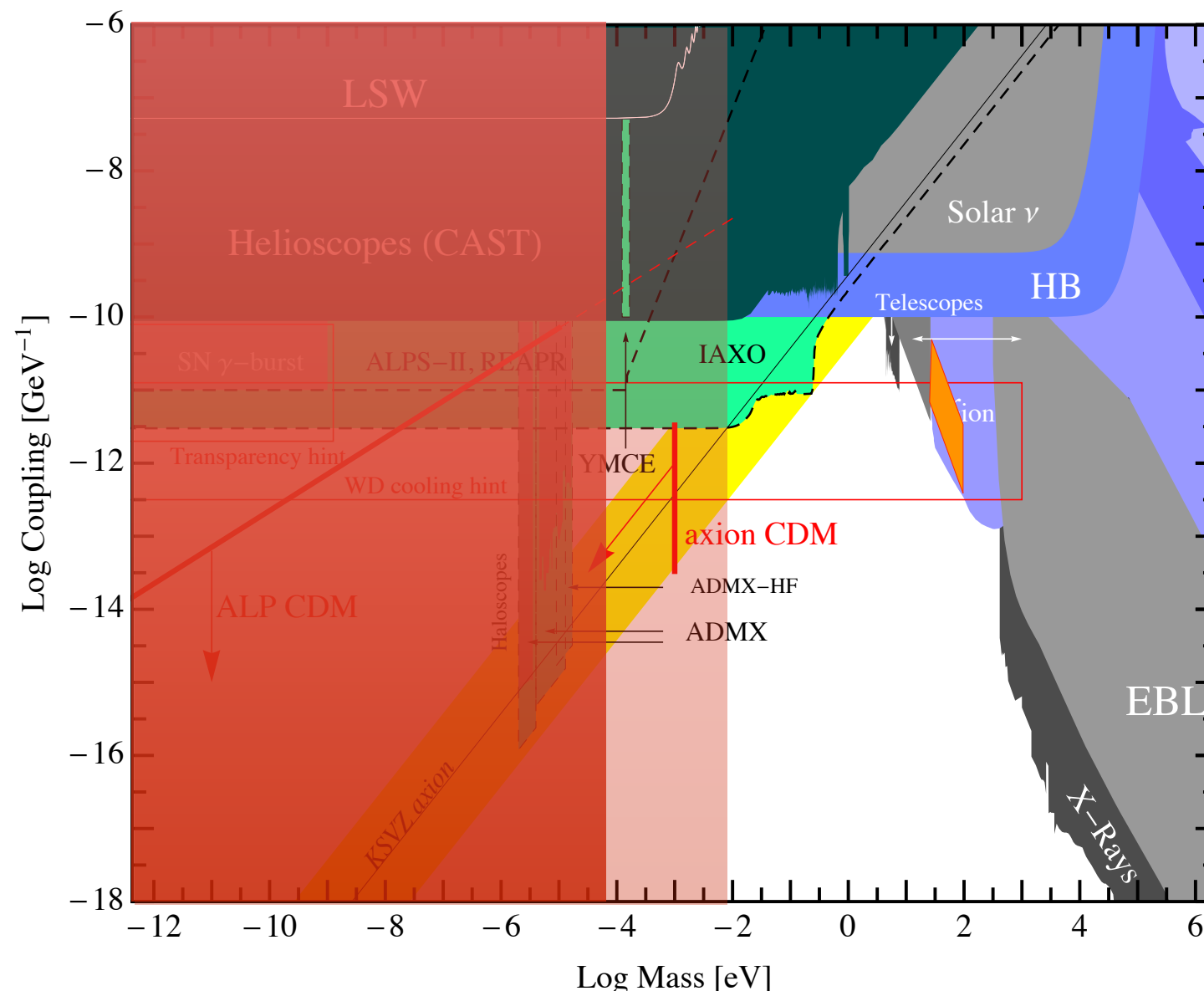


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From arXiv: 1205.2671

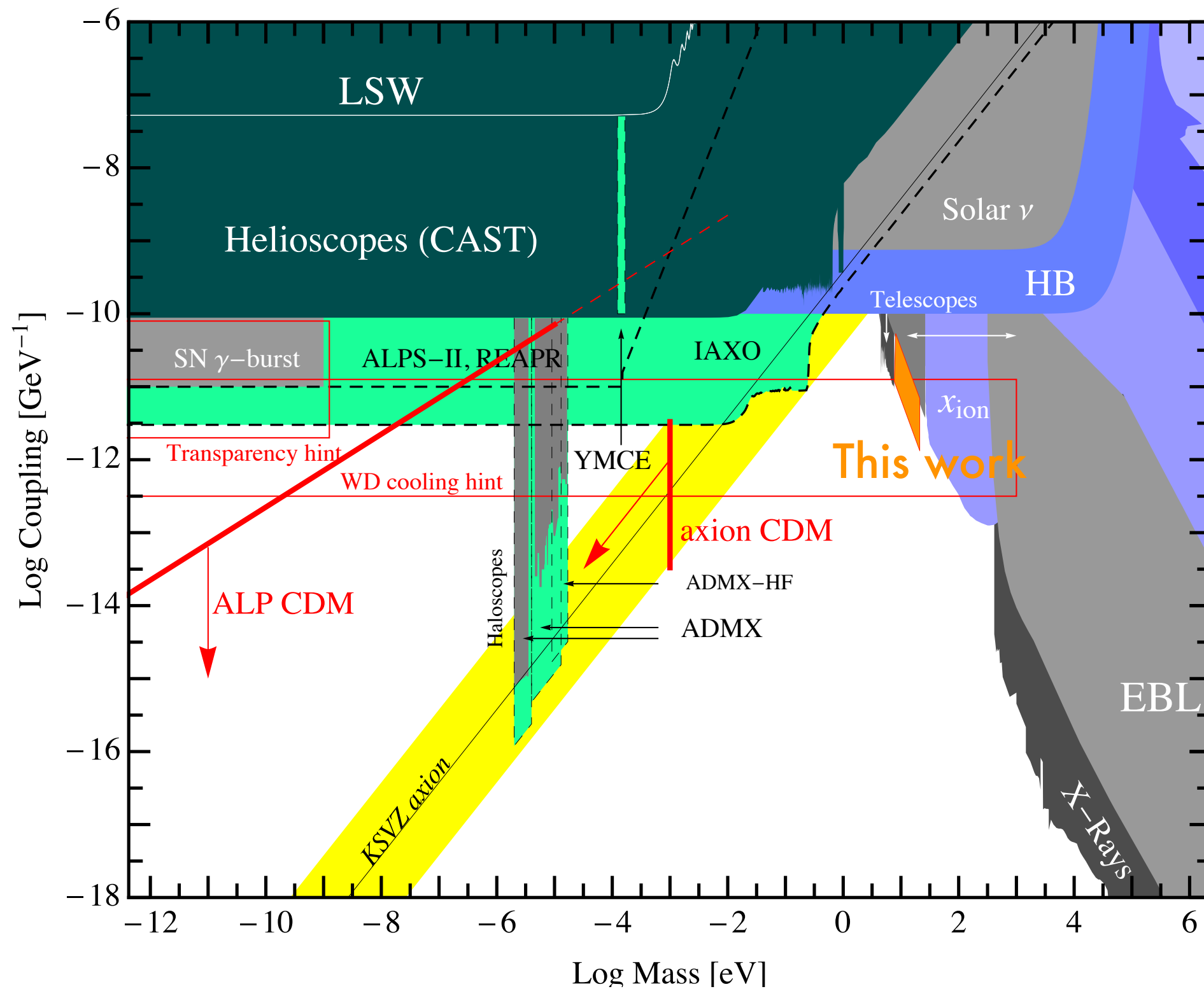
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Lay of the land

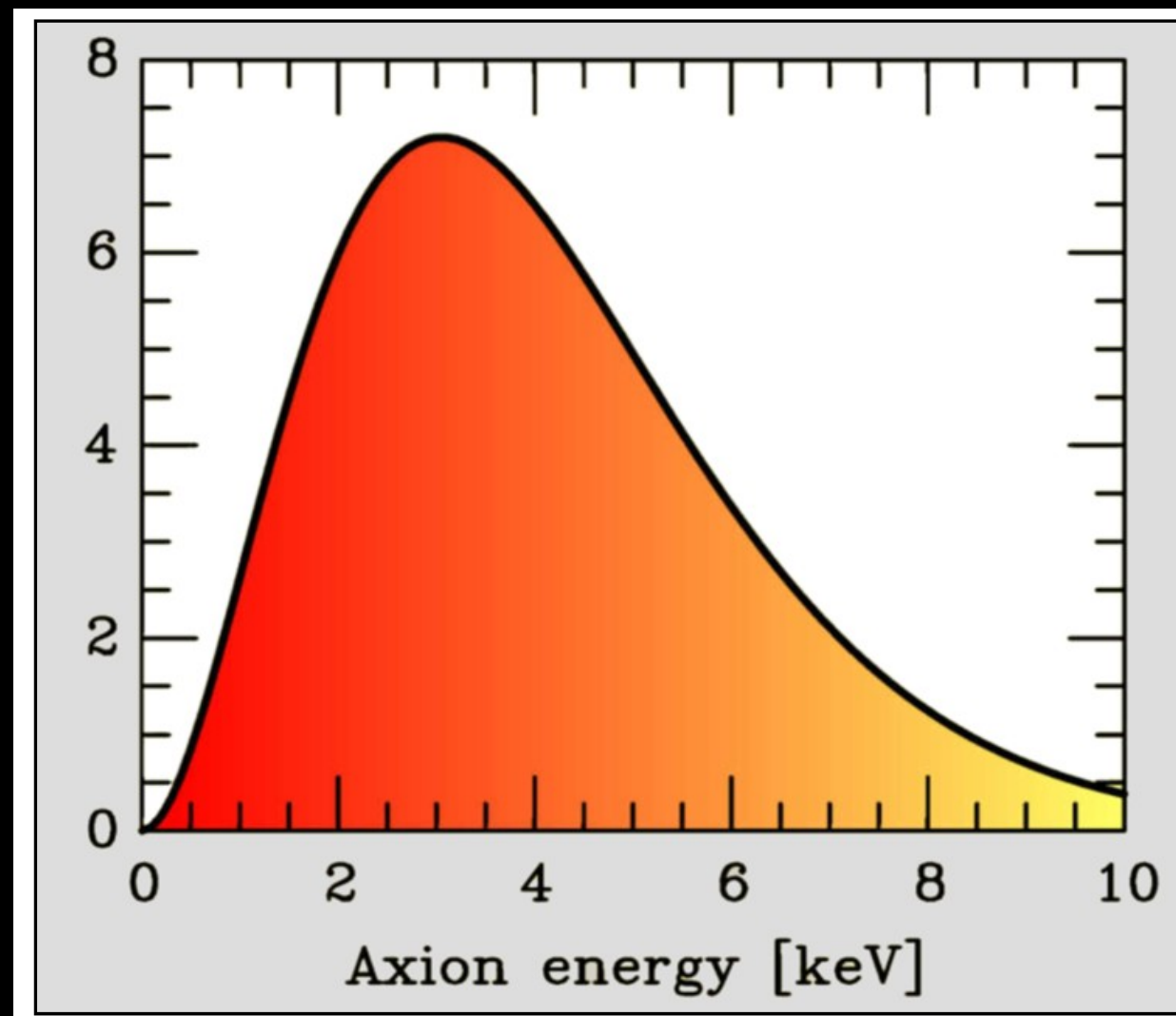


Axion helioscopes

* Resonance condition

$$qL < \pi \Rightarrow \sqrt{m_\gamma^2 - \frac{2\pi E_a}{L}} < m_a < \sqrt{m_\gamma^2 + \frac{2\pi E_a}{L}}$$

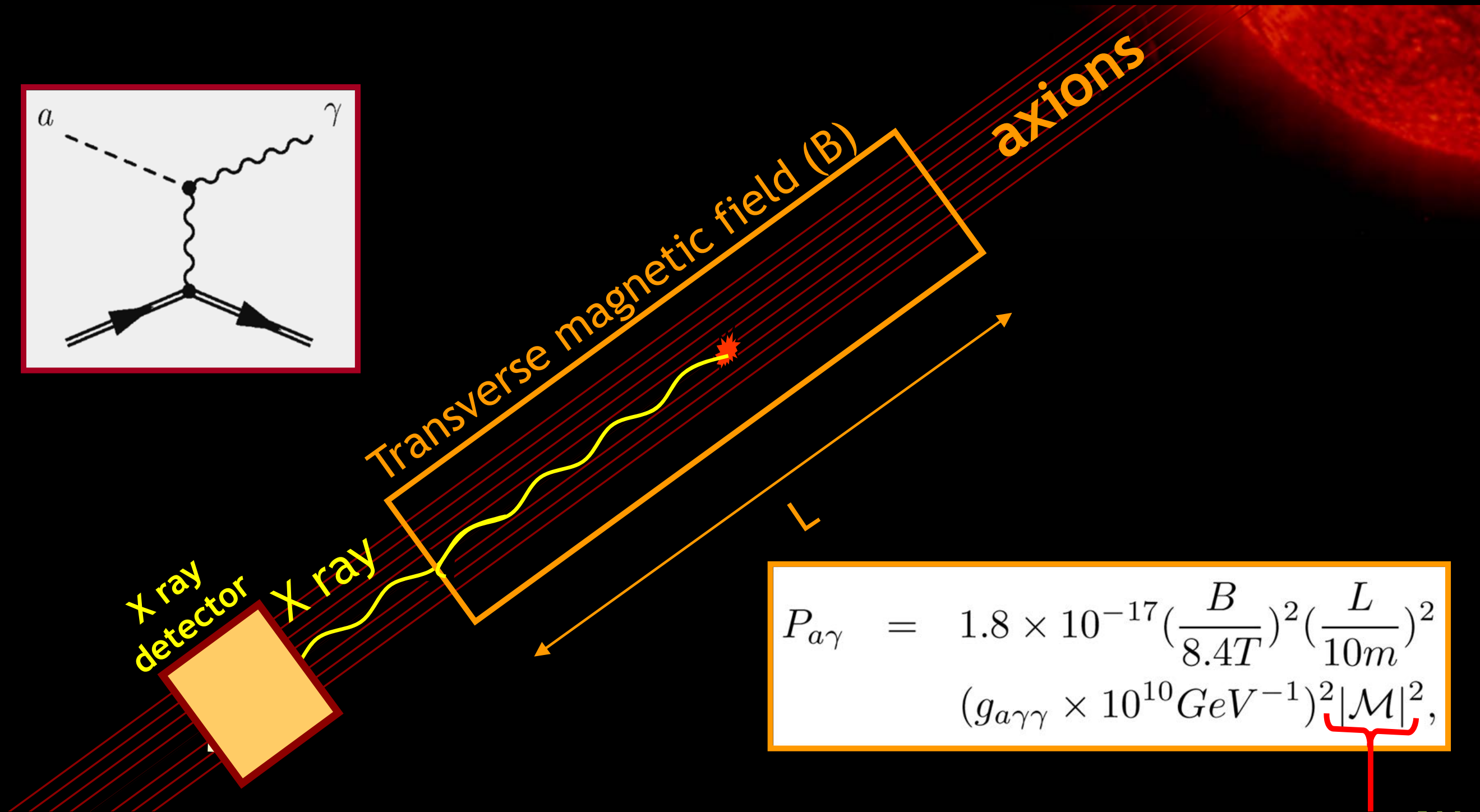
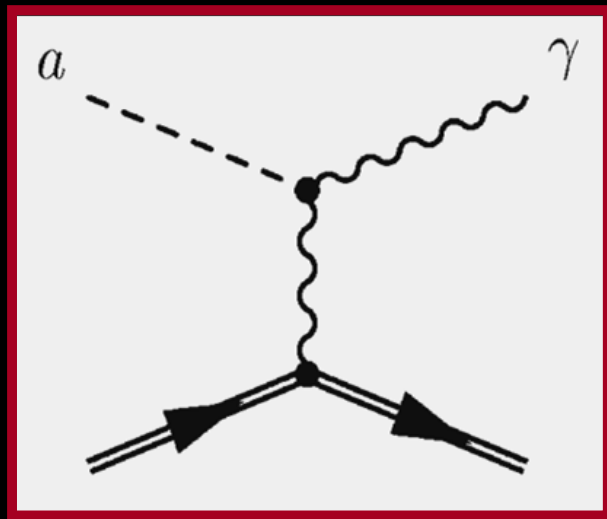
* Broad axion energy spectrum



Axion helioscopes

- * Backwards Primakoff process (Sikivie, Zioutas, and many others)

From Irastorza 2013

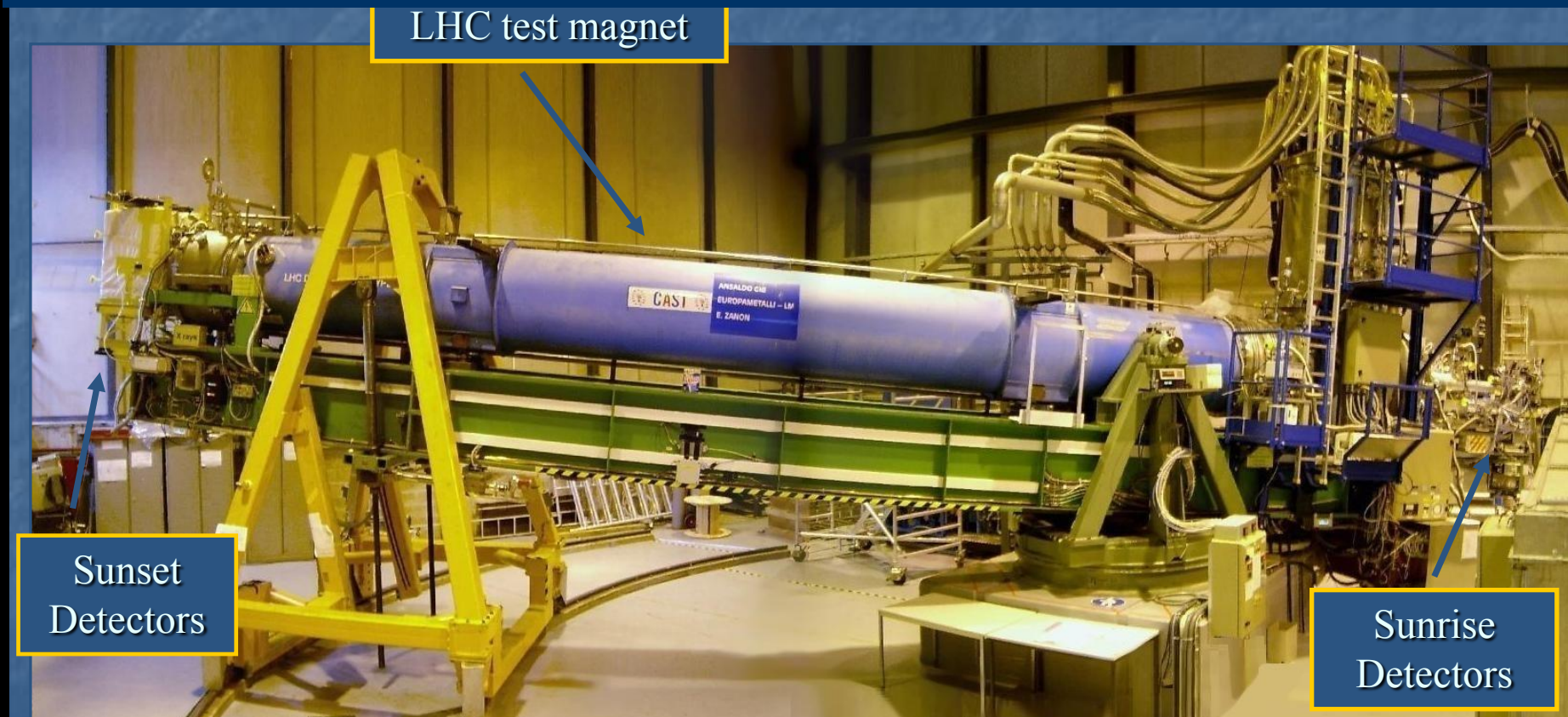


$$P_{a\gamma} = 1.8 \times 10^{-17} \left(\frac{B}{8.4T} \right)^2 \left(\frac{L}{10m} \right)^2 (g_{a\gamma\gamma} \times 10^{10} \text{GeV}^{-1})^2 |\mathcal{M}|^2,$$

CAST/IAXO

* CAST

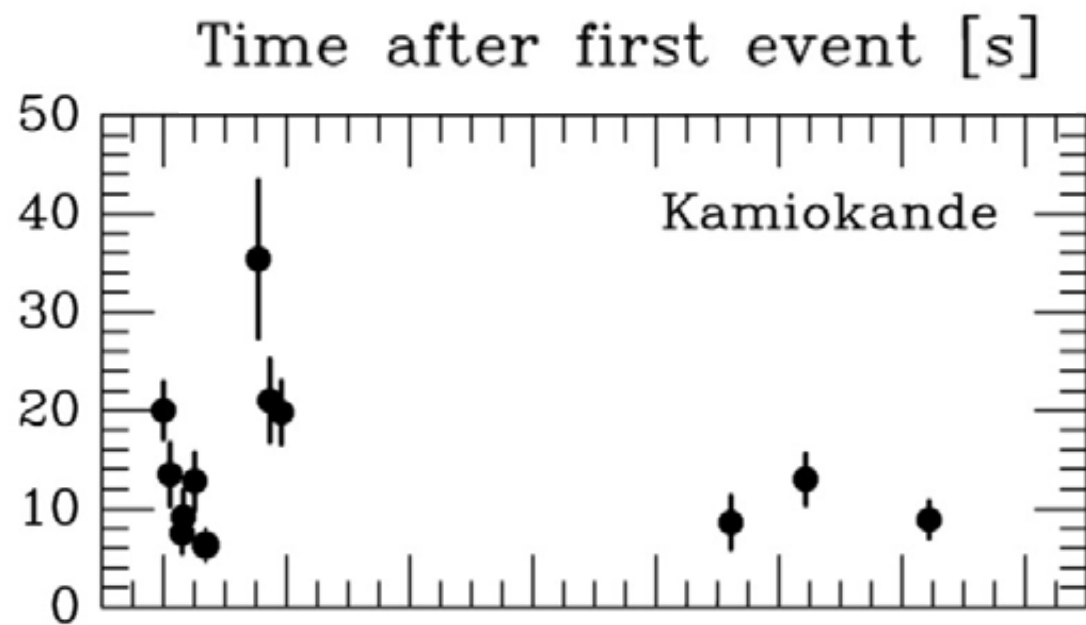
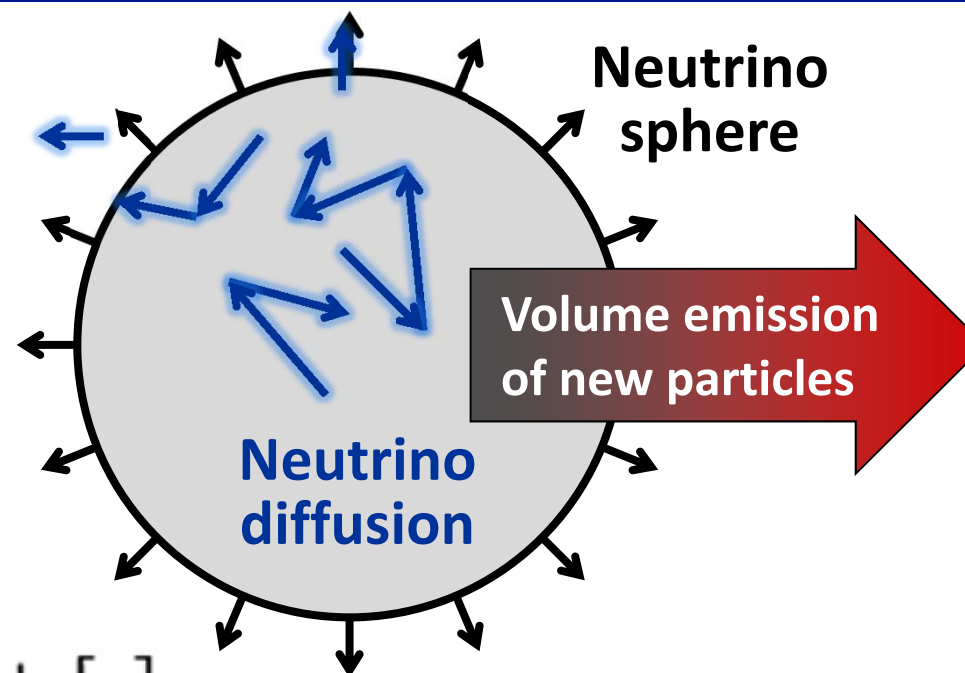
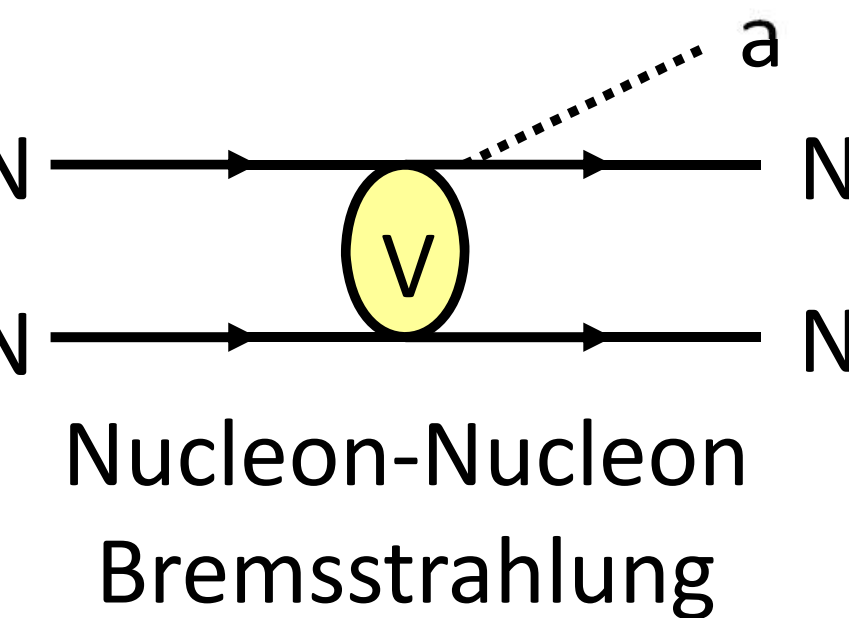
➤ LHC test magnet ($B=9$ T, $L=9.26$ m)



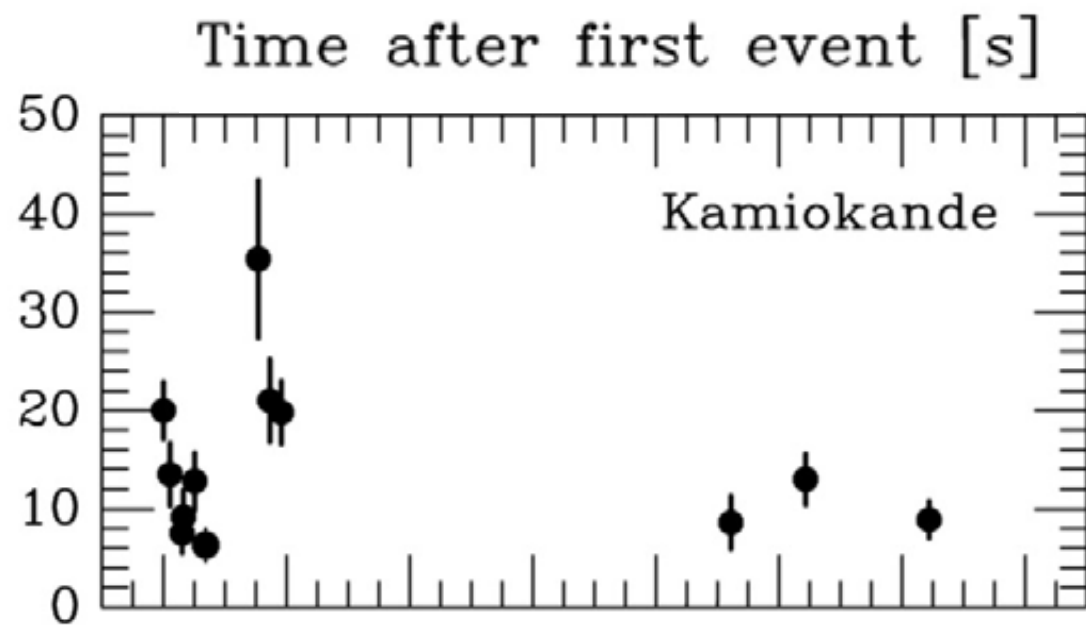
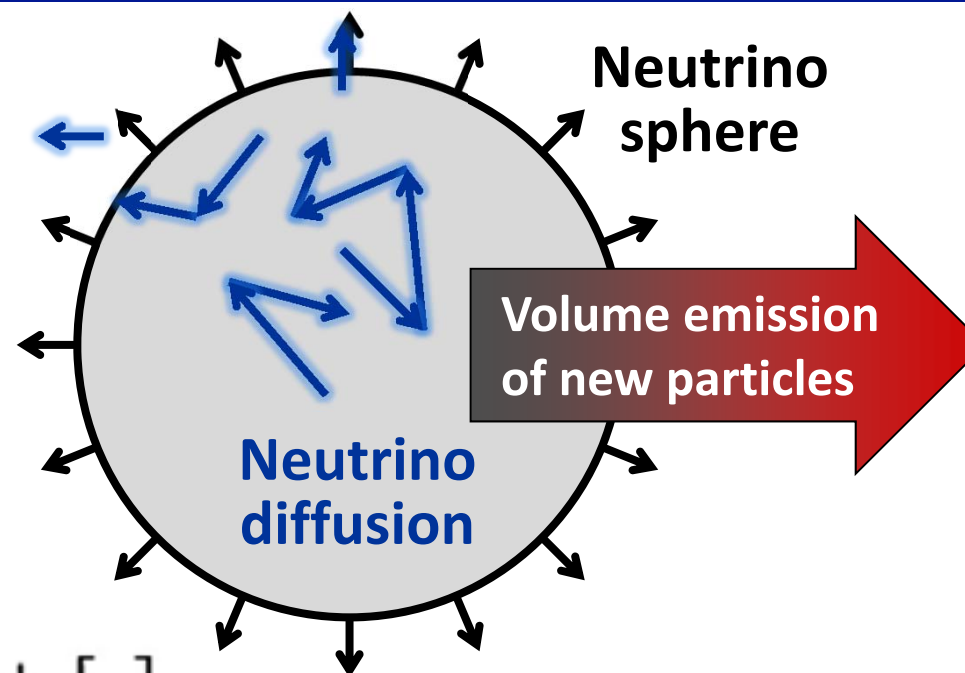
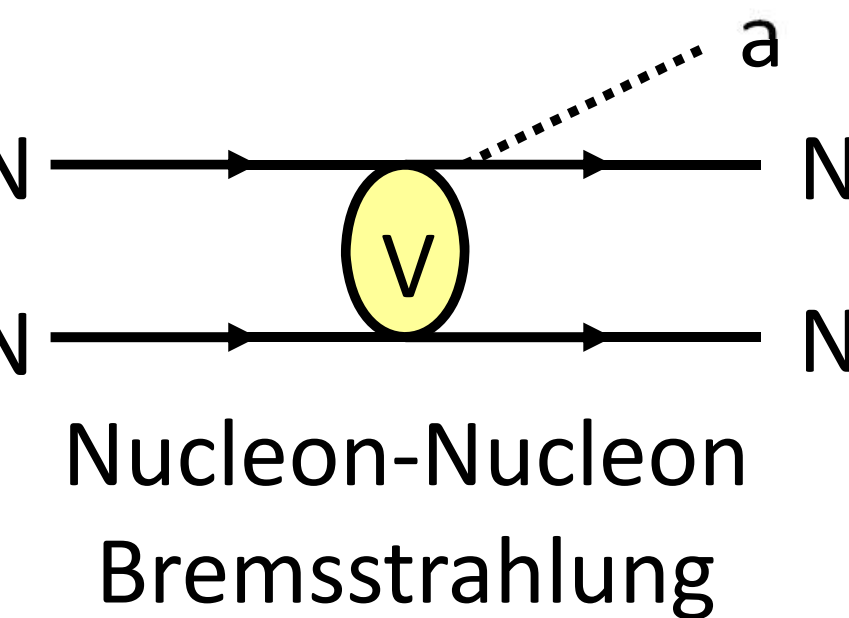
Lakic 2012

* IAXO proposal: 15-20m length magnet, optimized shape
[not LHC DUD]

Making axions in (exploding) stars, III

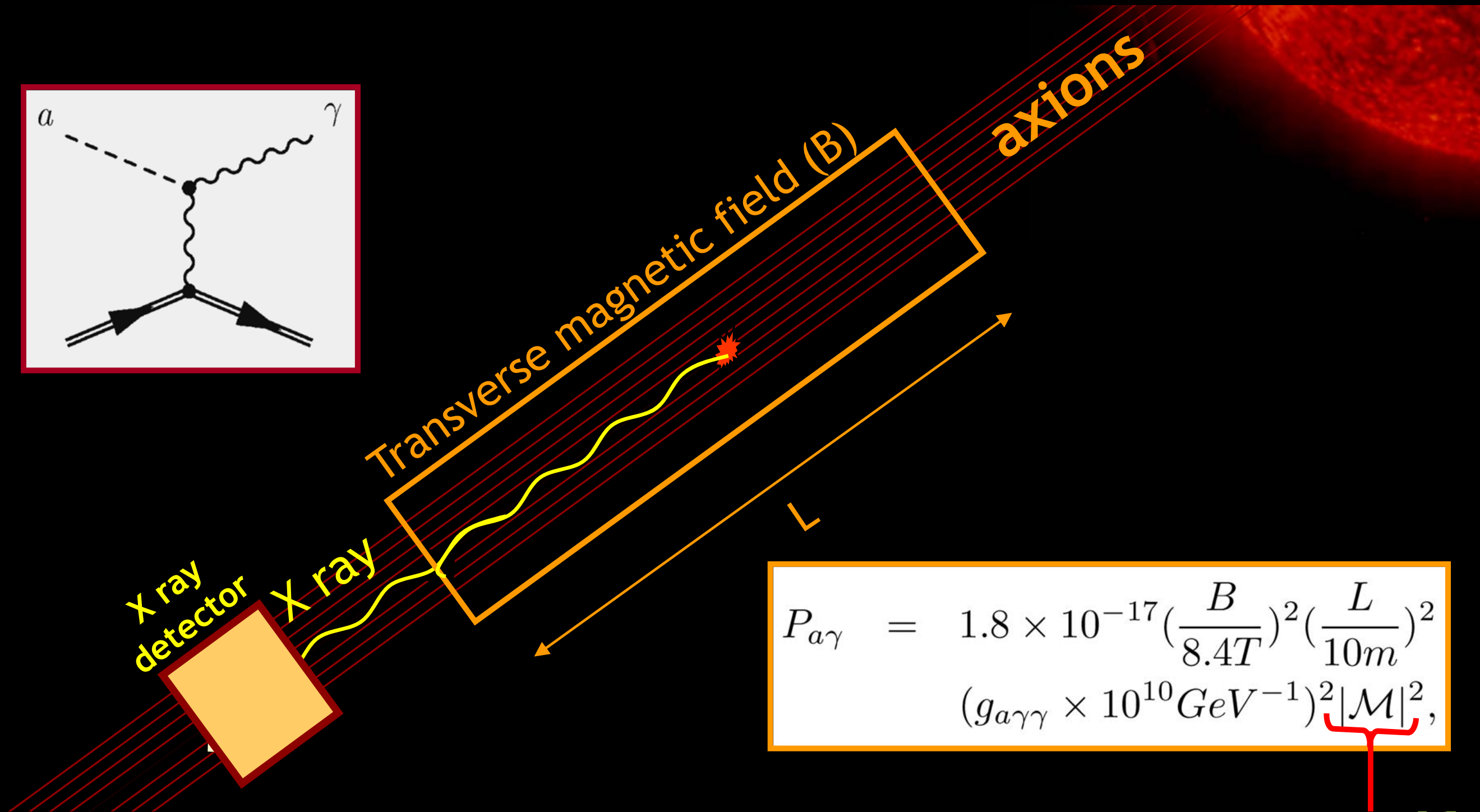
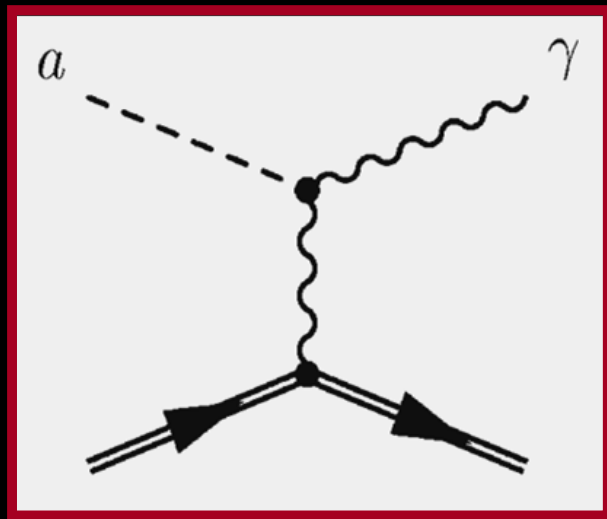


Making axions in (exploding) stars, III



Axion helioscopes

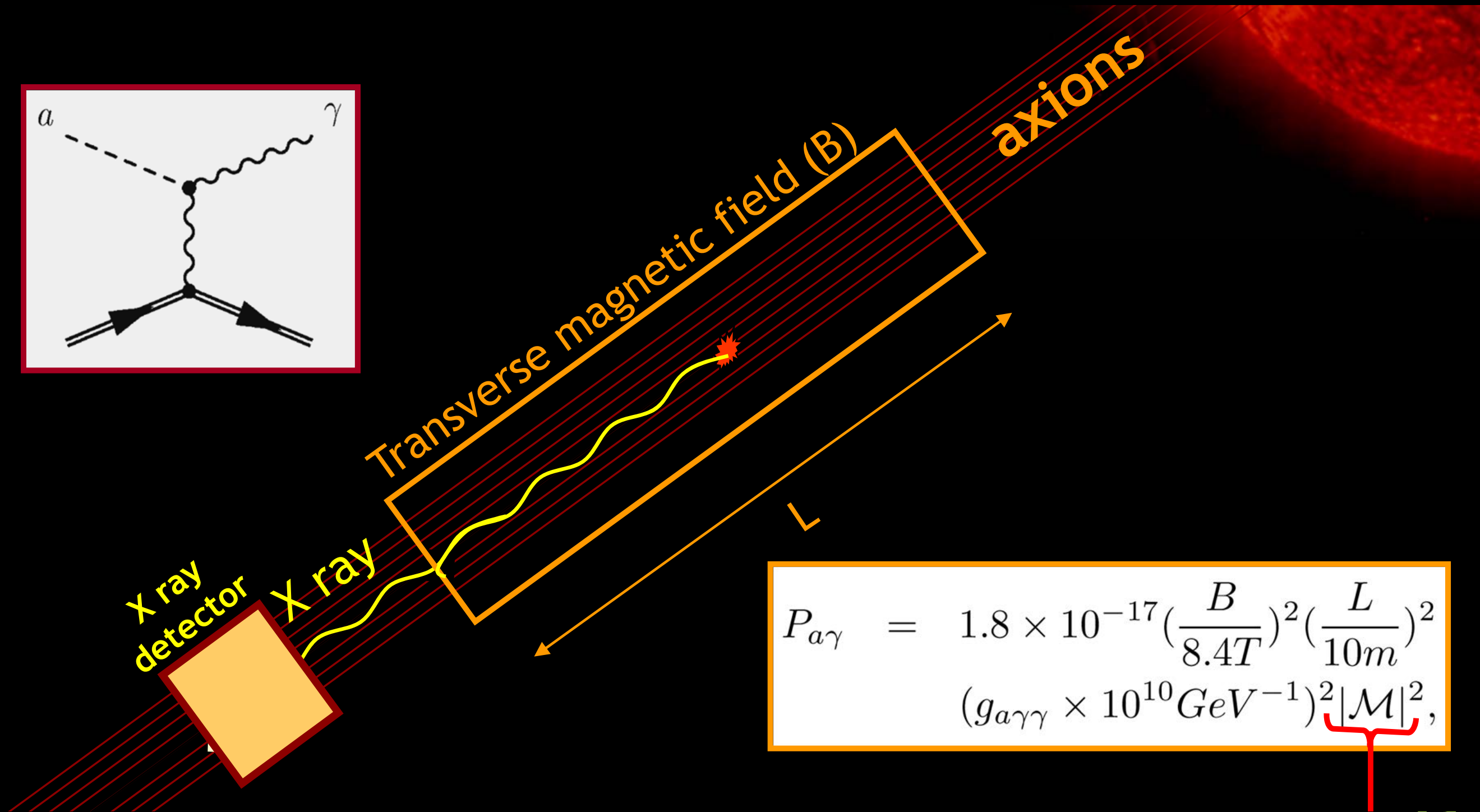
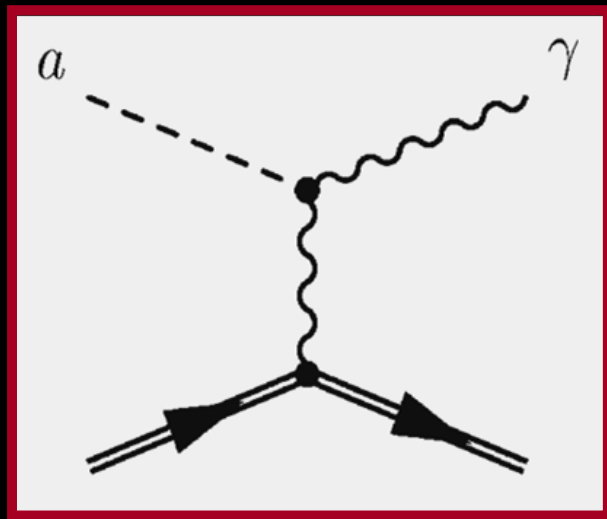
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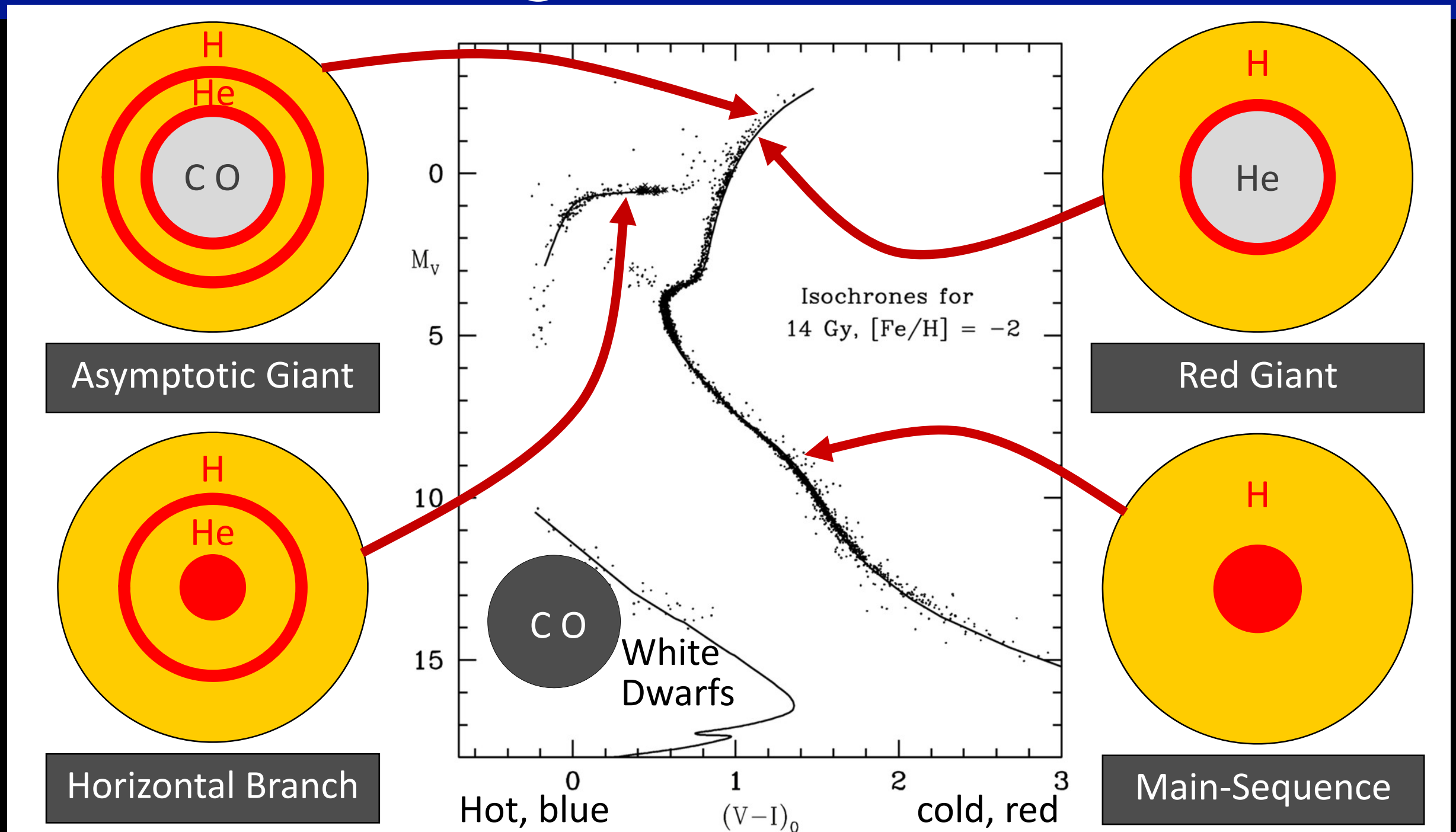
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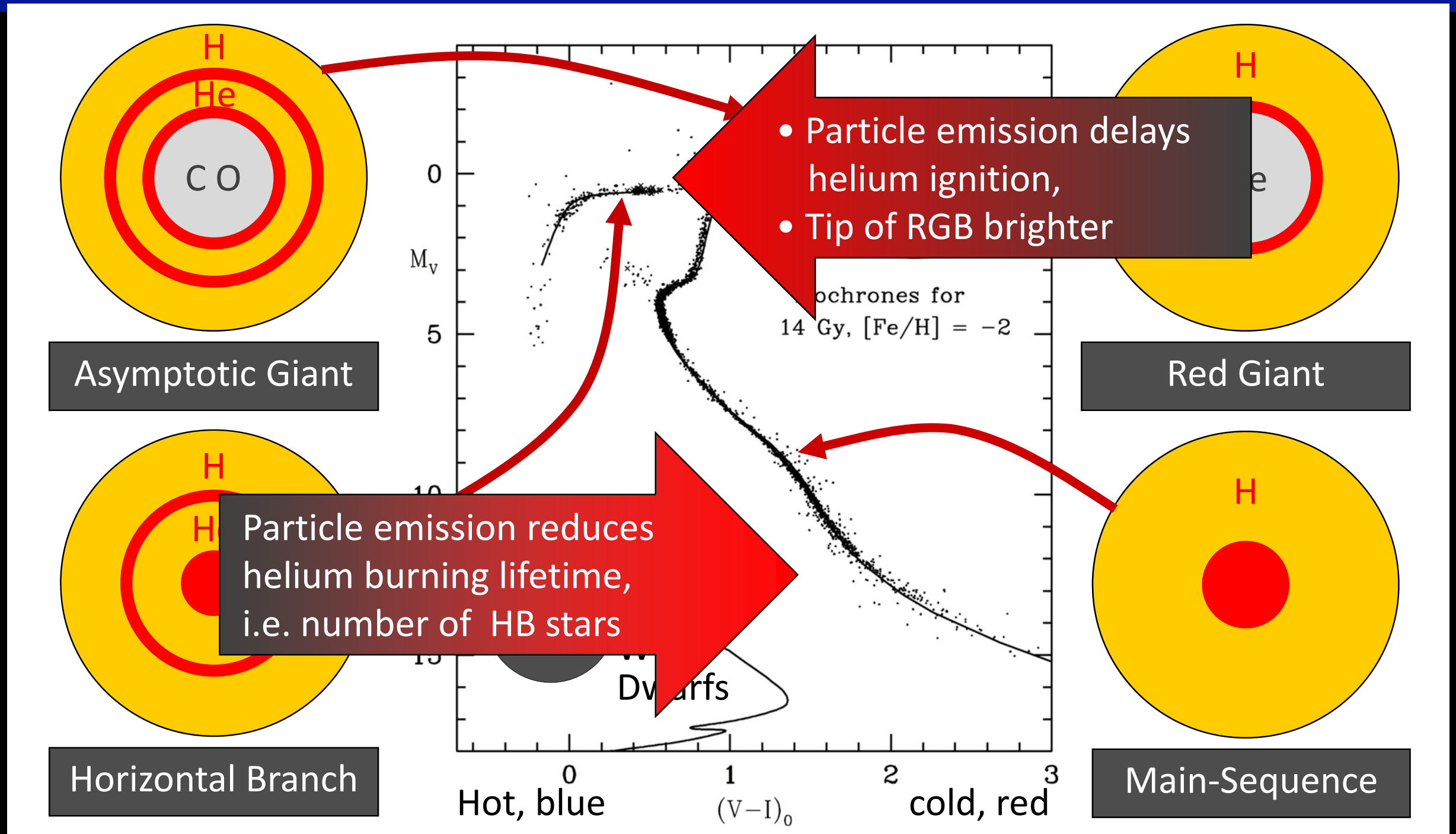
Making axions in stars, II



From Raffelt 2012

$$g_{a\gamma\gamma} \lesssim 10^{-10} \text{ GeV}^{-1}$$

Making axions in stars, II



From Raffelt 2012

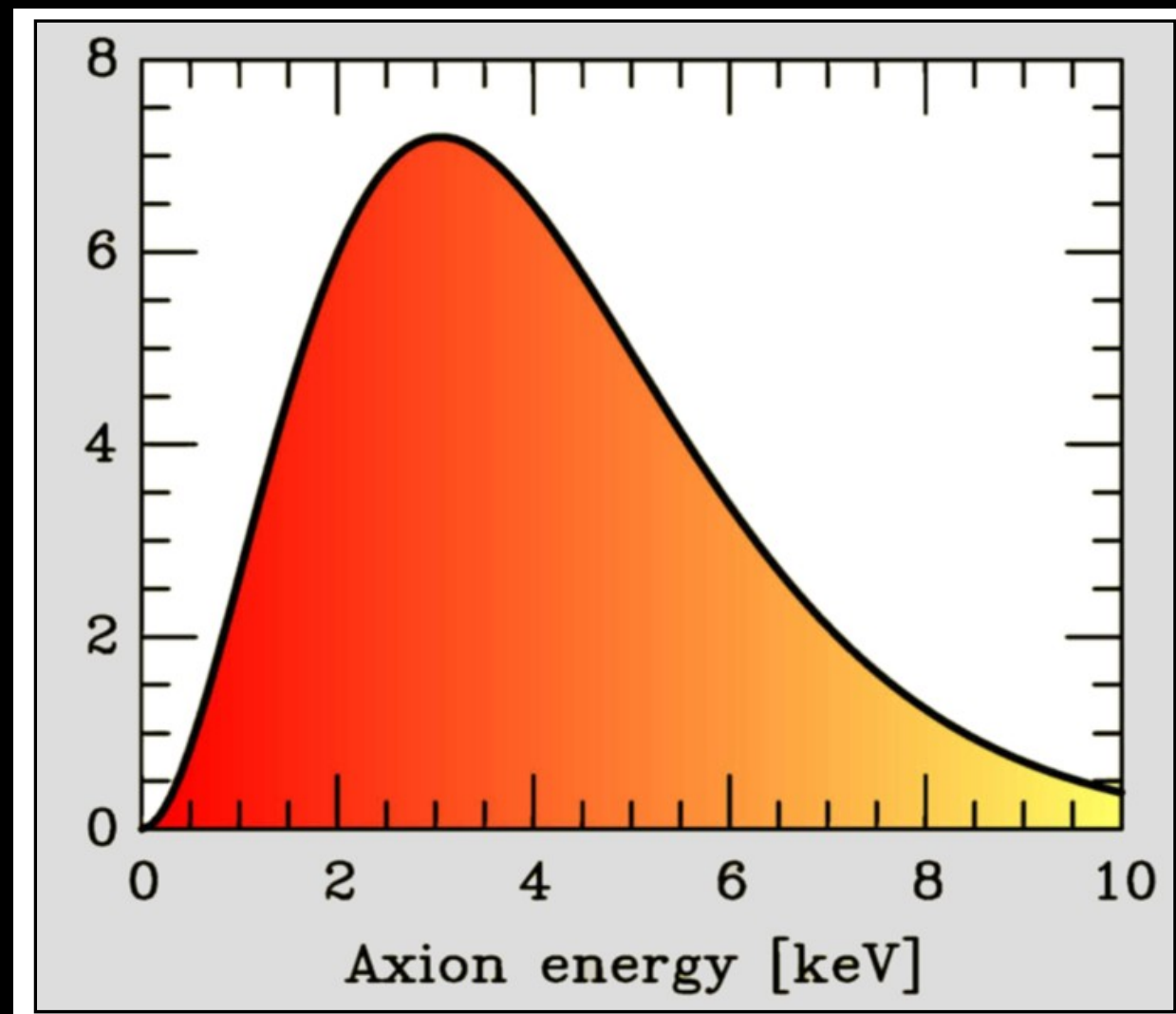
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Axion helioscopes

* Resonance condition

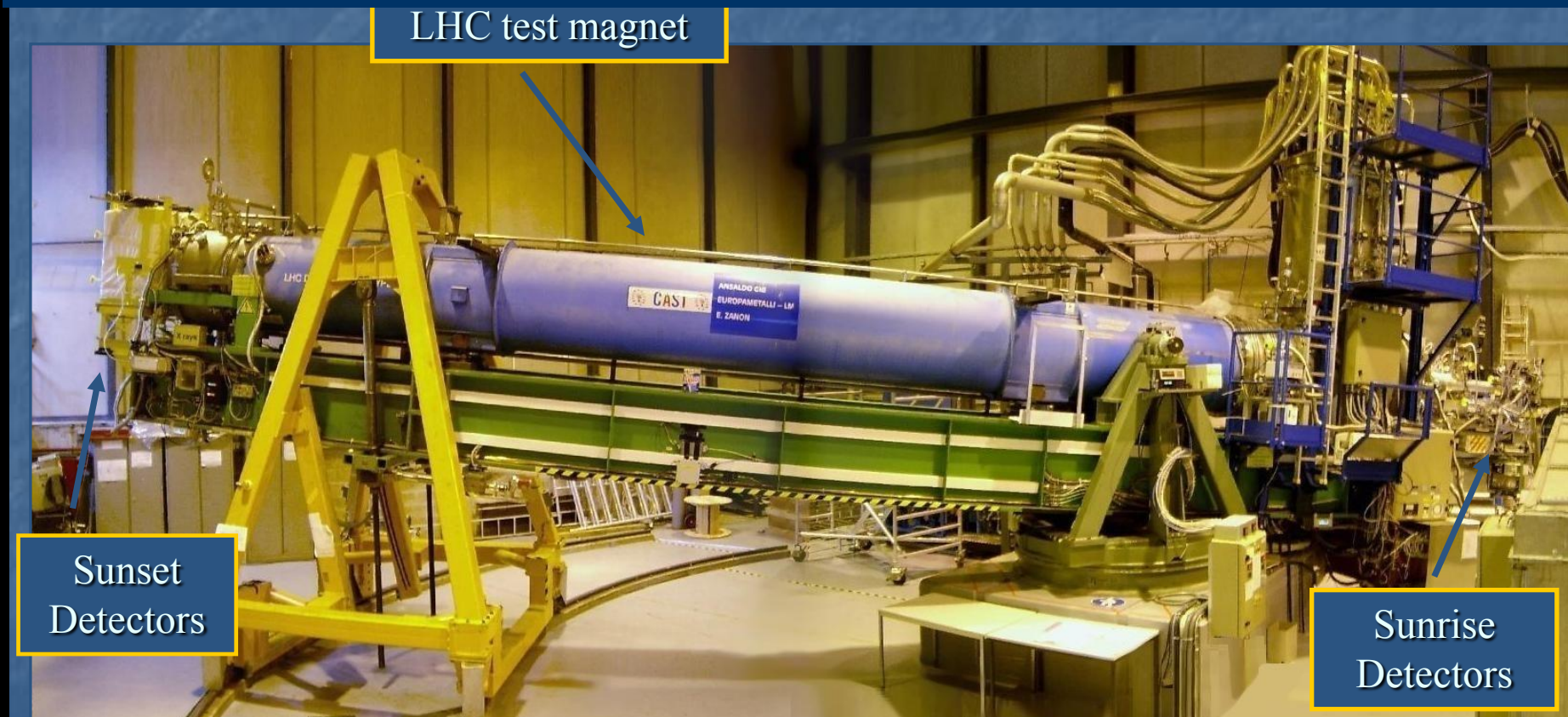
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CAST/IAXO

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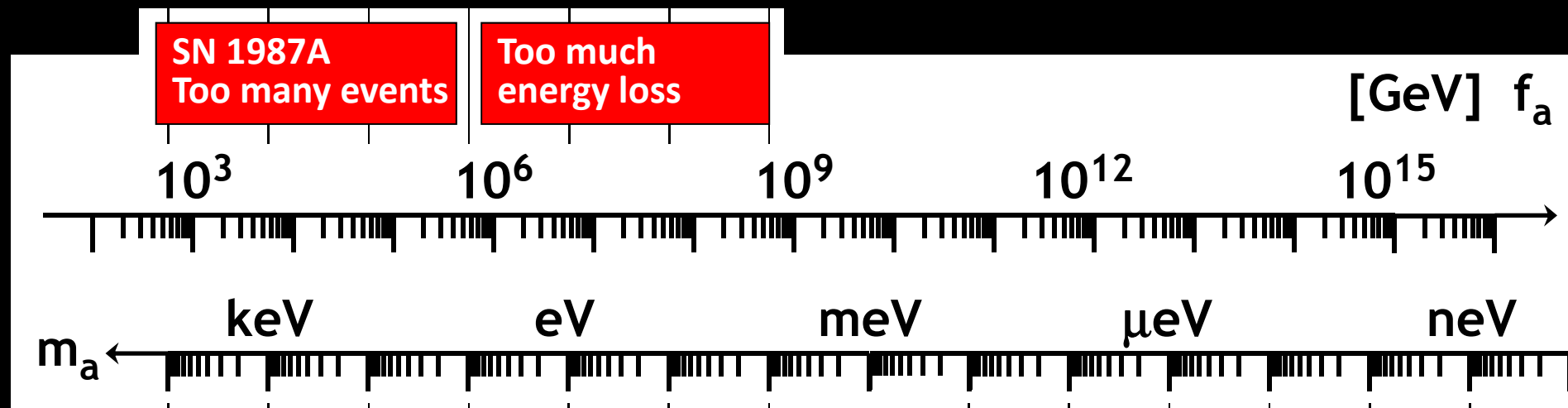
CAST/IAXO

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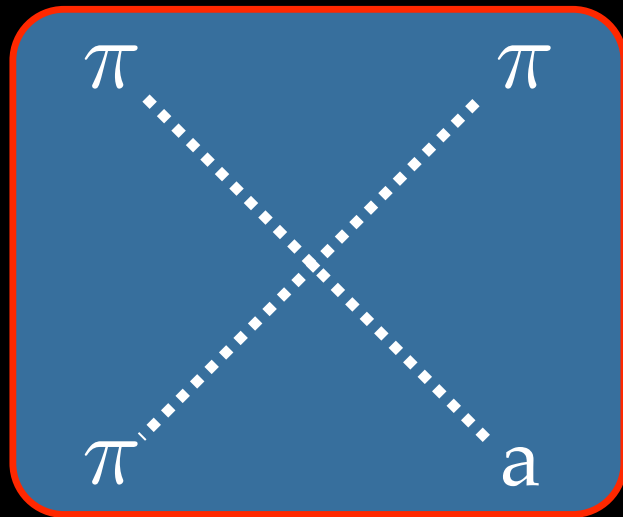
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Making axions in (exploding) stars, III

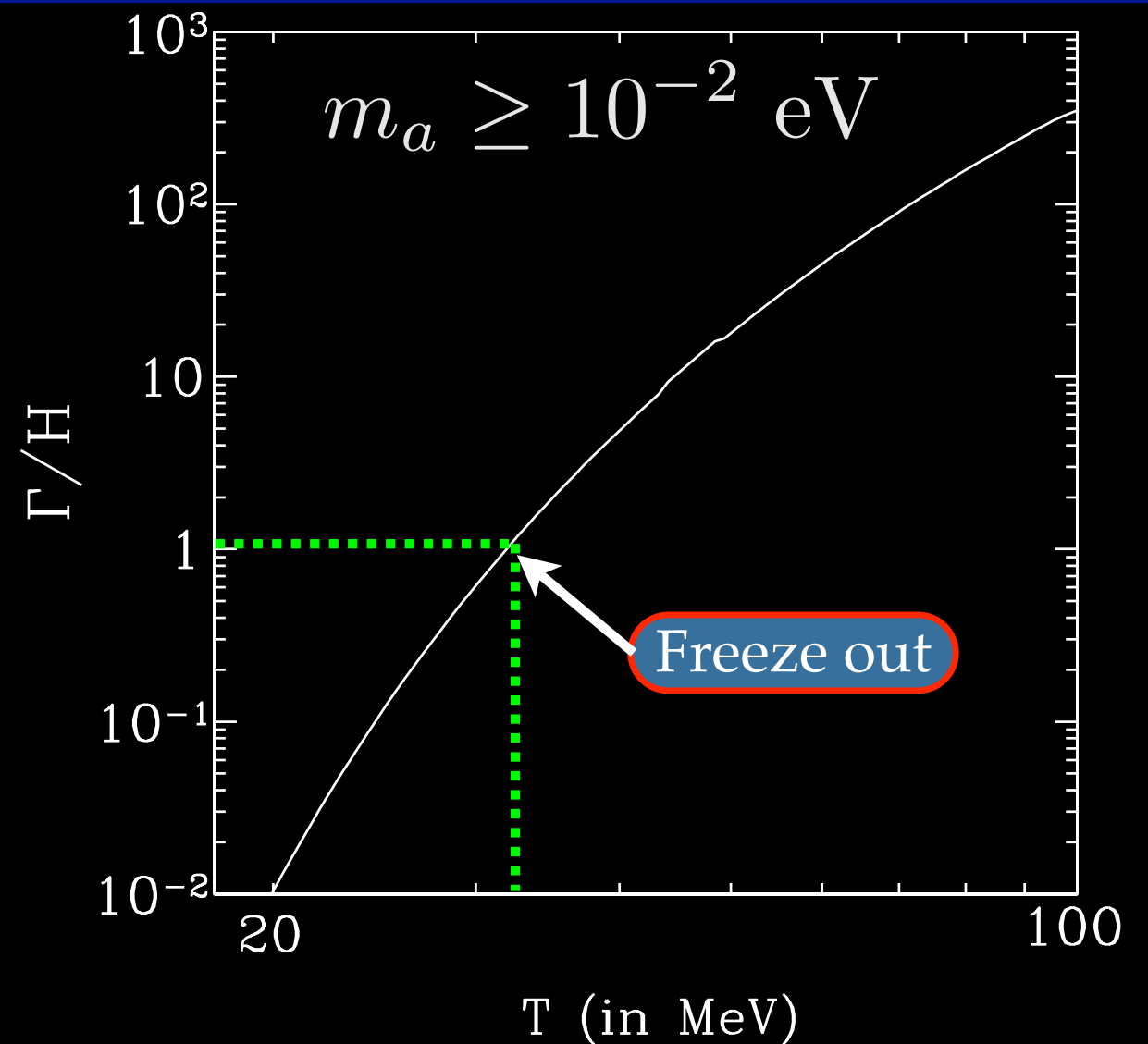


Hot axion production at early times

Axion Production:



$$\Omega_a h^2 = \frac{m_{a,\text{eV}}}{130} \left(\frac{10}{g_{*,\text{F}}} \right)$$



- * Axions produced through interactions between non-relativistic pions in chemical equilibrium with rate

Axion hot dark matter

- * Axion free-streaming length

$$\lambda_{\text{fs}} \simeq \frac{196 \text{ Mpc}}{m_{\text{a,eV}}}$$

- * Entropy generation, e.g. modulus decay

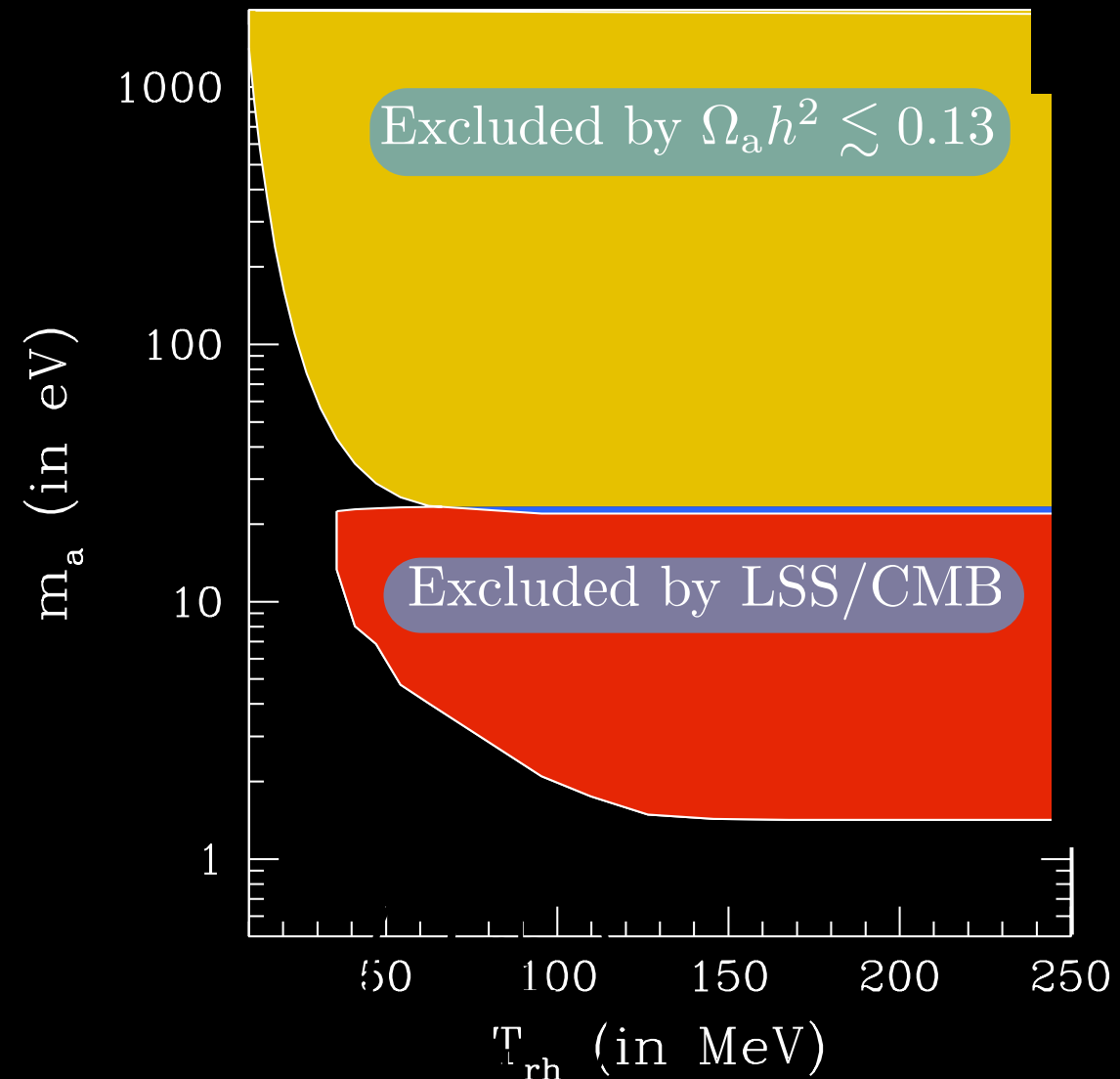
$$T_{\text{rh}} \sim 10 \text{ MeV} \left(\frac{m_{\phi}}{\text{TeV}} \right)^{3/2}$$

- * Axion temperature lowered

$$\frac{T_{\text{a}}}{T_{\nu}} \propto \left(\frac{T_{\text{rh}}}{T_{\text{F}}} \right)^{5/3}$$

- * Free streaming-length modified

$$\lambda_{\text{fs}} \simeq \frac{196 \text{ Mpc}}{m_{\text{a,eV}}} \left(\frac{T_{\text{a}}}{T_{\nu}} \right)$$



with T.L. Smith and M. Kamionkowski
 Phys. Rev. D77 085020, 0711.1342

$$\Omega_a \rightarrow \Omega_a \left(\frac{T_{\text{rh}}}{T_{\text{F}}} \right)^5$$

Axion hot dark matter

A new telescope search for decaying relic axions

with K.Z. Khor, M. Kamionkowski, E.Jullo, G.Covone, J.P-Kneib

Axion HDM: Decay line

* Monochromatic emission line:

$$\lambda = \frac{c}{m_a c^2 / 2h} = 24800 \text{Å} \frac{(1 + z_c)}{m_a / \text{eV}}$$

* Axions decay:

$$\tau = 6.8 \times 10^{24} \xi^{-2} m_{a,\text{eV}}^{-5} \text{ s}$$

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Visible

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$$\tau = 6.8 \times 10^{24} \xi^{-2} m_{a,\text{eV}}^{-5} \text{ s}$$

Following in the footsteps of Ressell, Bershadsky, Turner 1991

Axion HDM: Galaxy clusters

✳ Galaxy clusters are huge axion reservoirs

$$N_{\text{ax}} = 10^{80} m_{a,\text{eV}}^{-1} !$$

✳ Reasonably wide line $\sigma_{1000} \sim 1$

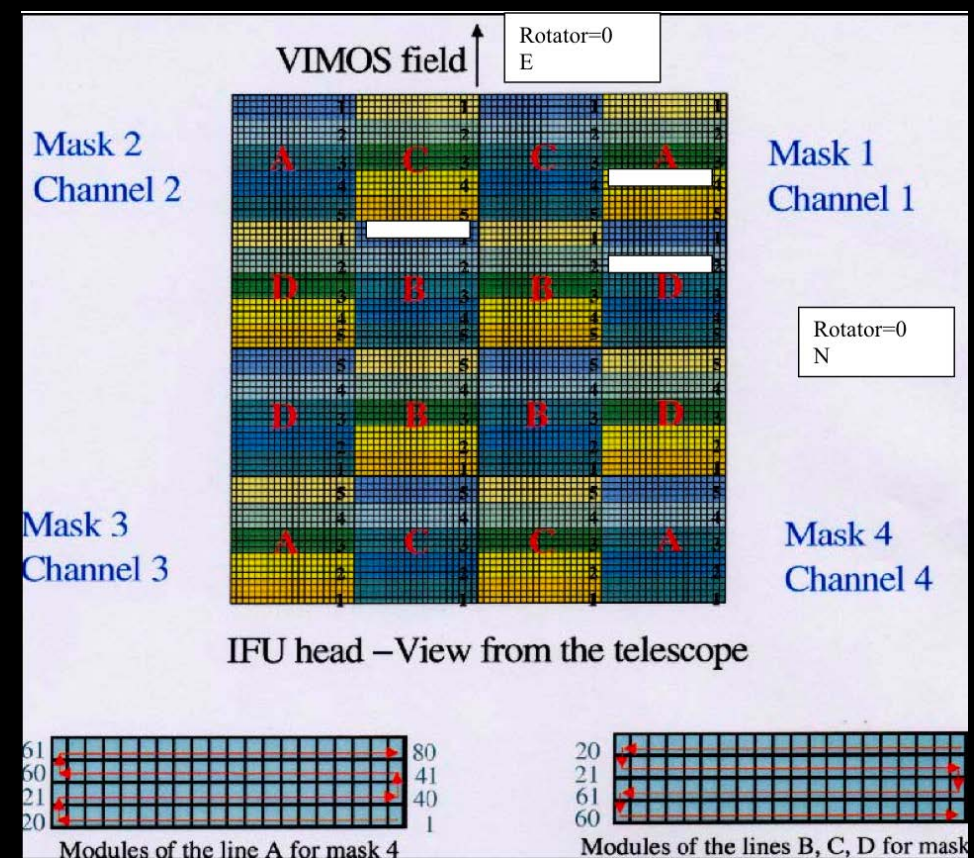
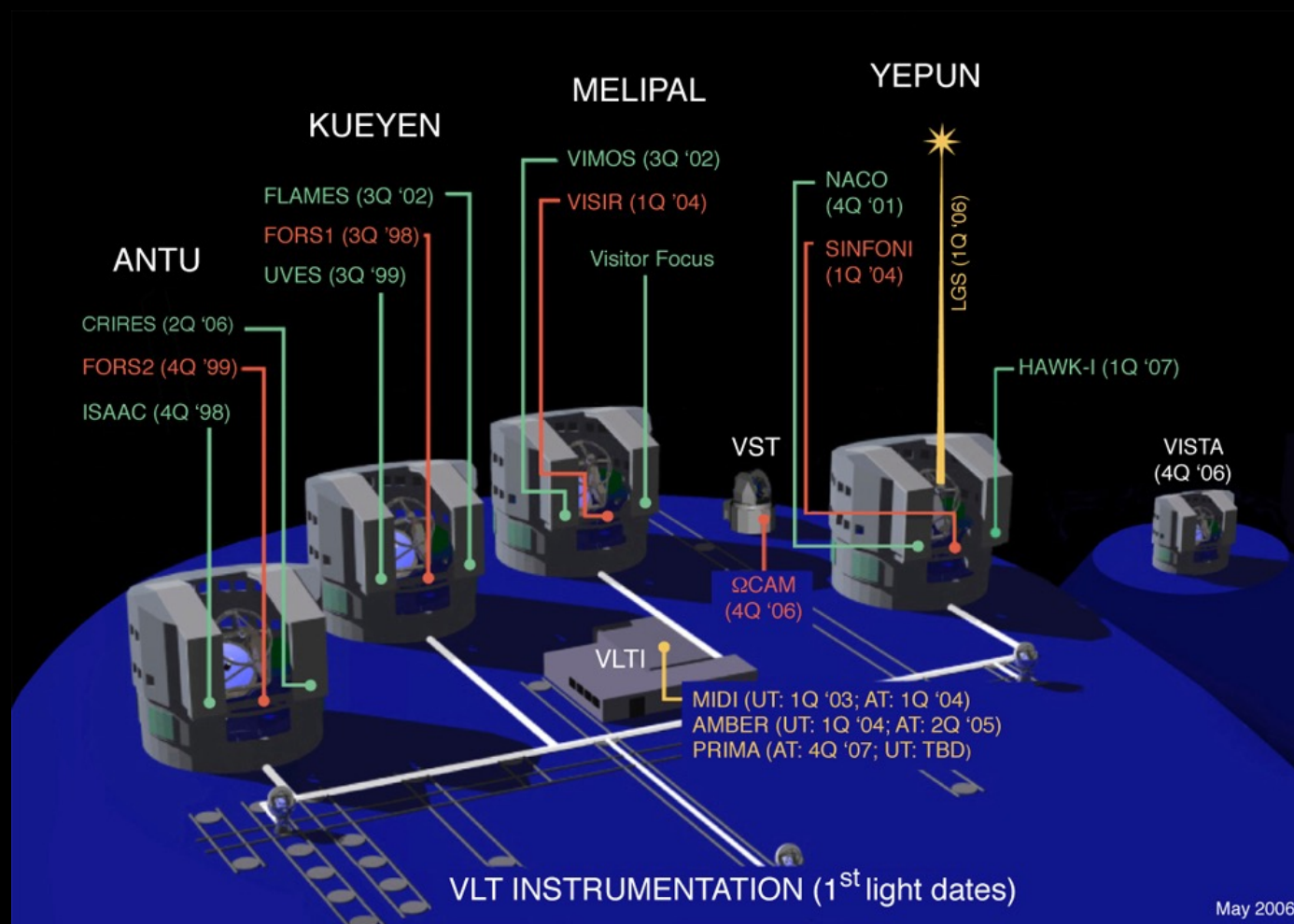
✳ Strong/weak gravitational lensing mass maps available

✳ Comparable to sky brightness

$$I_{\lambda} \simeq 10^{-18} \text{ cgs} \frac{m_{a,\text{eV}}^7 \xi^2}{(1+z_c)^4} \frac{\Sigma}{10^{12} \text{M}_{\odot} \text{pix}^{-2}}$$

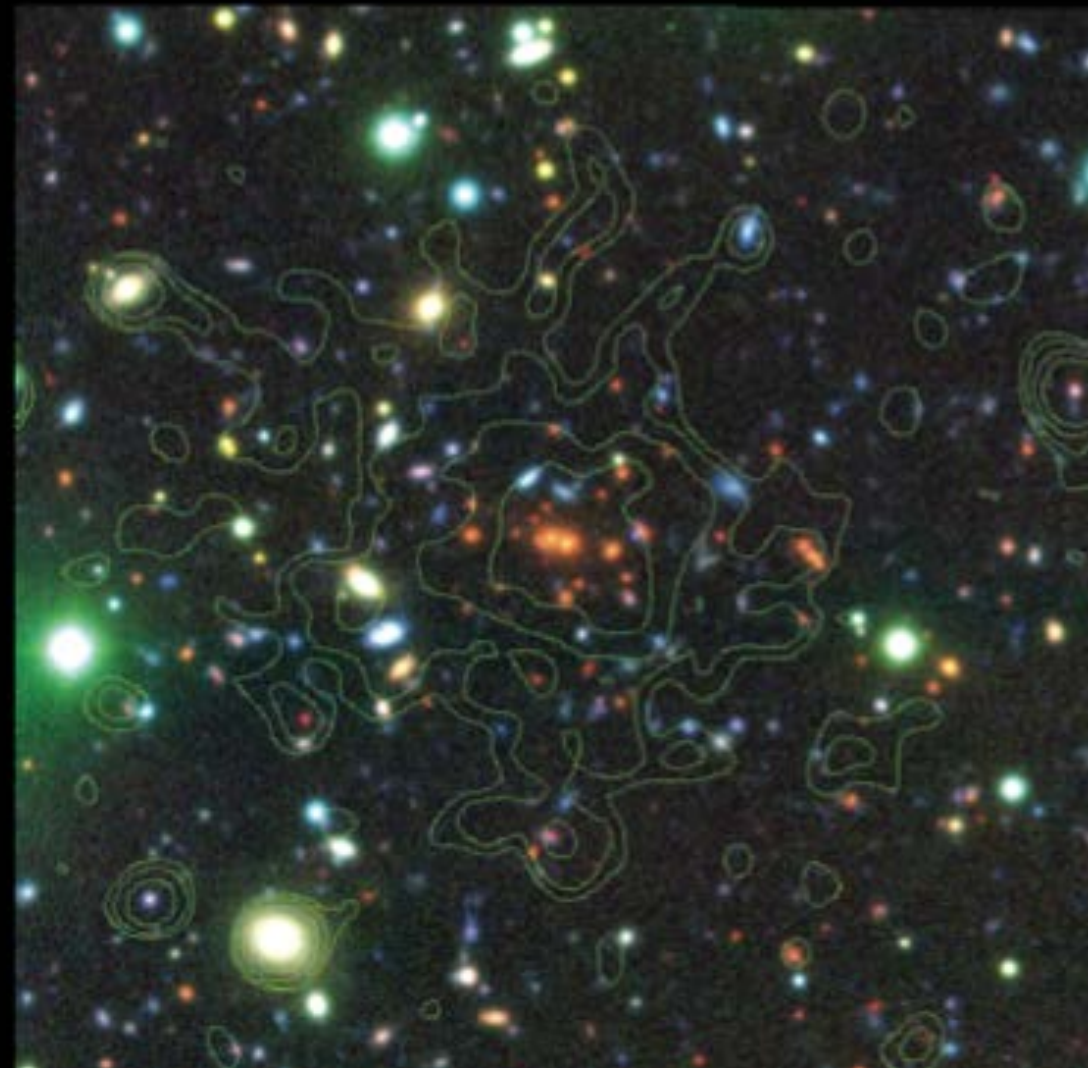
Axion HDM: VIMOS IFU

- ✦ At VLT (Very Large Telescope) array of ~8 m instruments at Paranal, Chile
- ✦ VIMOS IFU yields spatially resolved spectroscopy (6400 fibers in 1 arcmin²)



Axion HDM: Modern optical telescope searches

- ✦ RDCS 1252 is a $8 \times 10^{14} M_{\odot}$ cluster at $z = 1.237$
- ✦ Obtained 17 hrs of time for VIMOS IFU spectra using LR-Blue grism
- ✦ Publicly available weak-lensing mass maps (Lombardi et al. 2005) + single confirmed SL arc



Axion HDM: Modern optical telescope searches



Axion HDM: Modern optical telescope searches

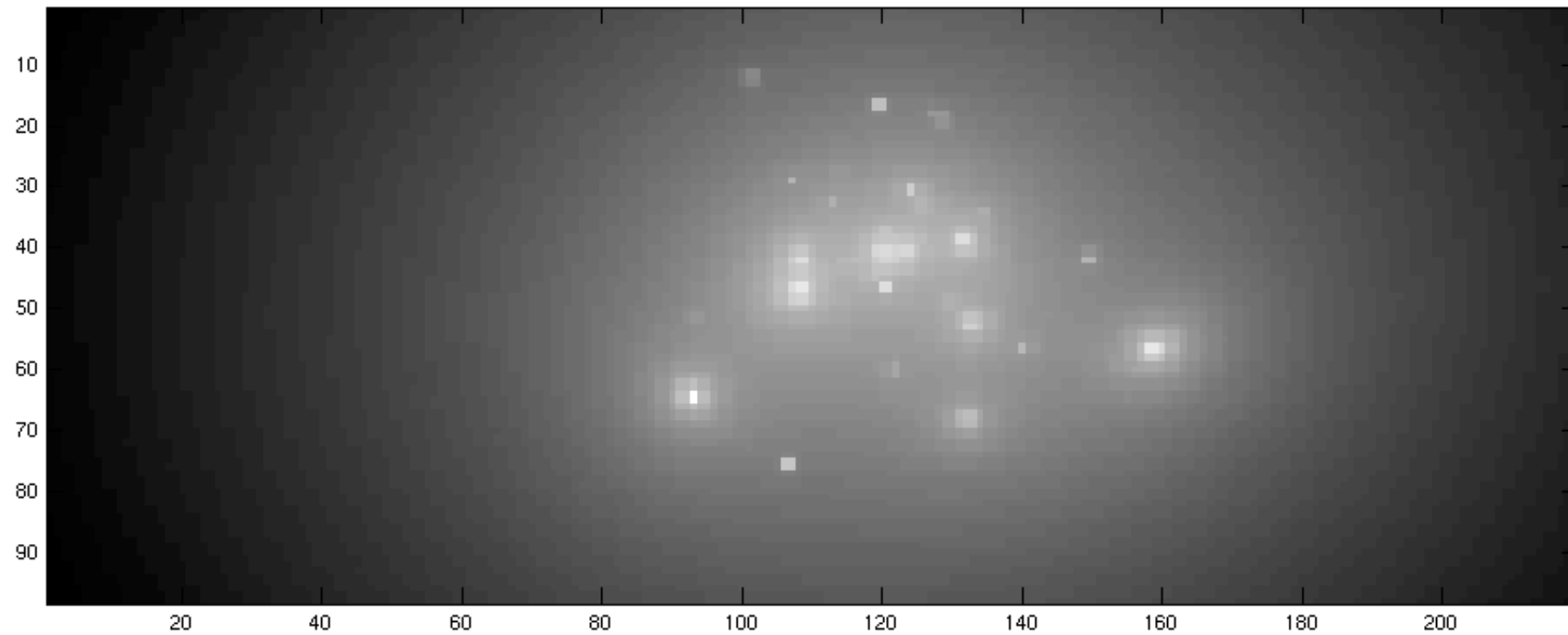
Grin et al. 2007: Abell 2667/2390

PRD, astro-ph/0611502

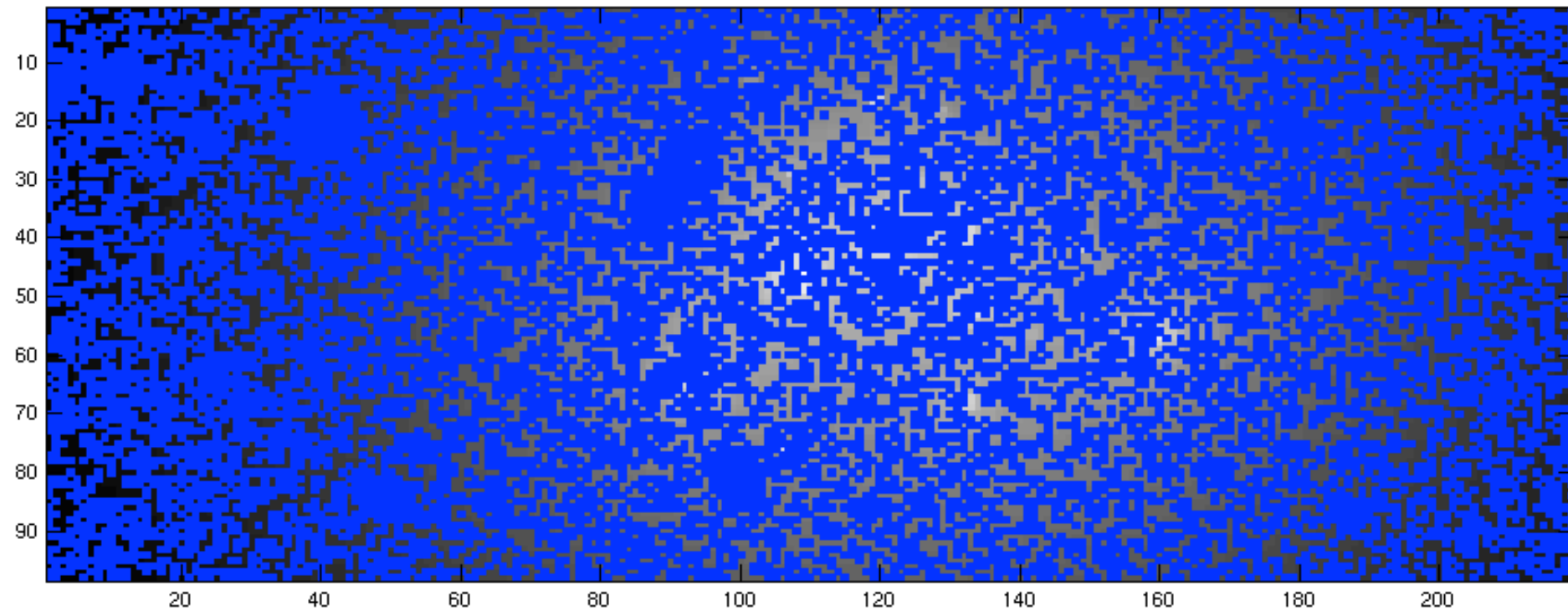
K.Z. Khor (Princeton Class of 2014)



Axion HDM: Cluster mass maps and

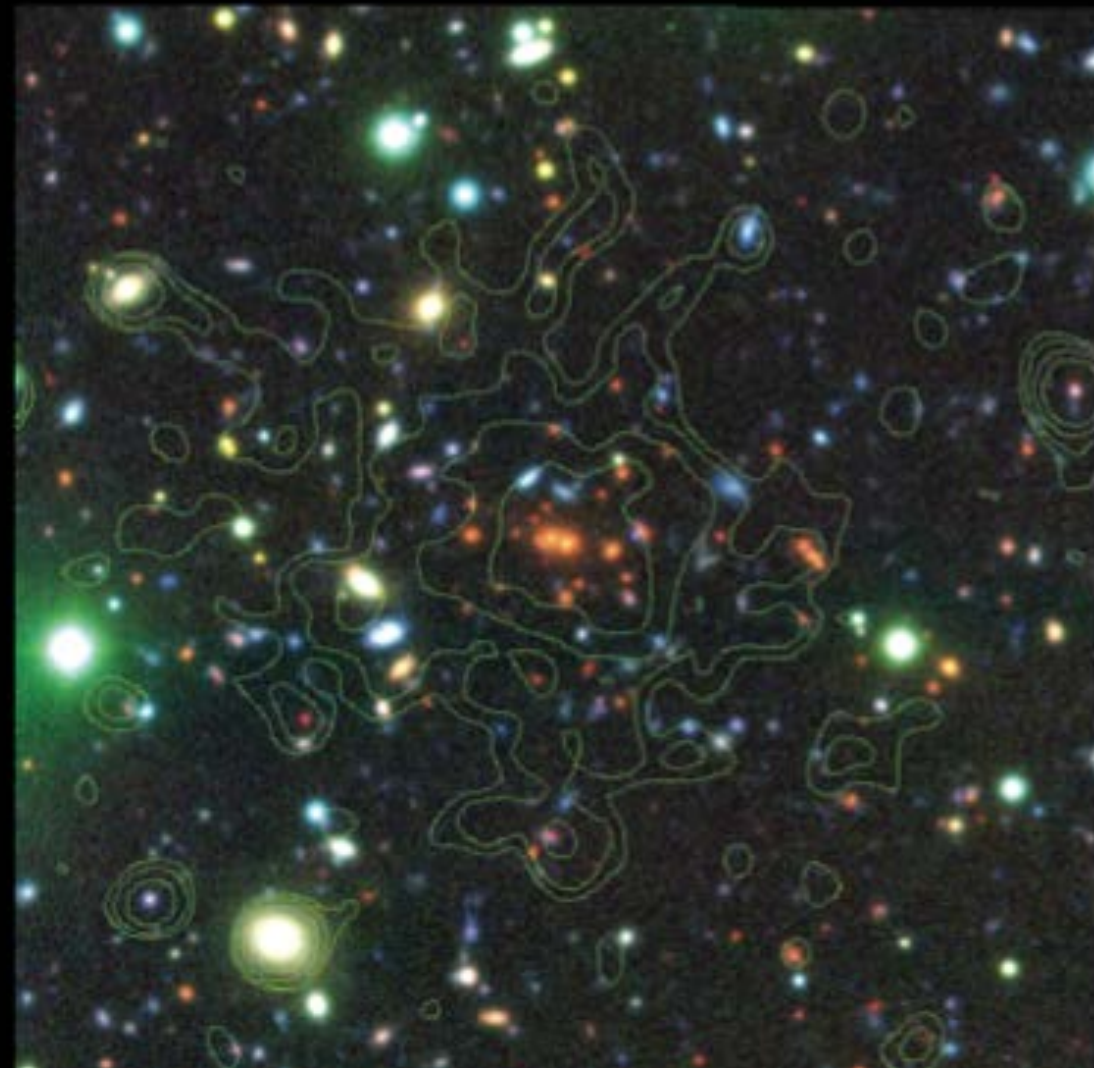


Axion HDM: Cluster mass maps and



Axion HDM: RDCS 1252/A2667+A2390

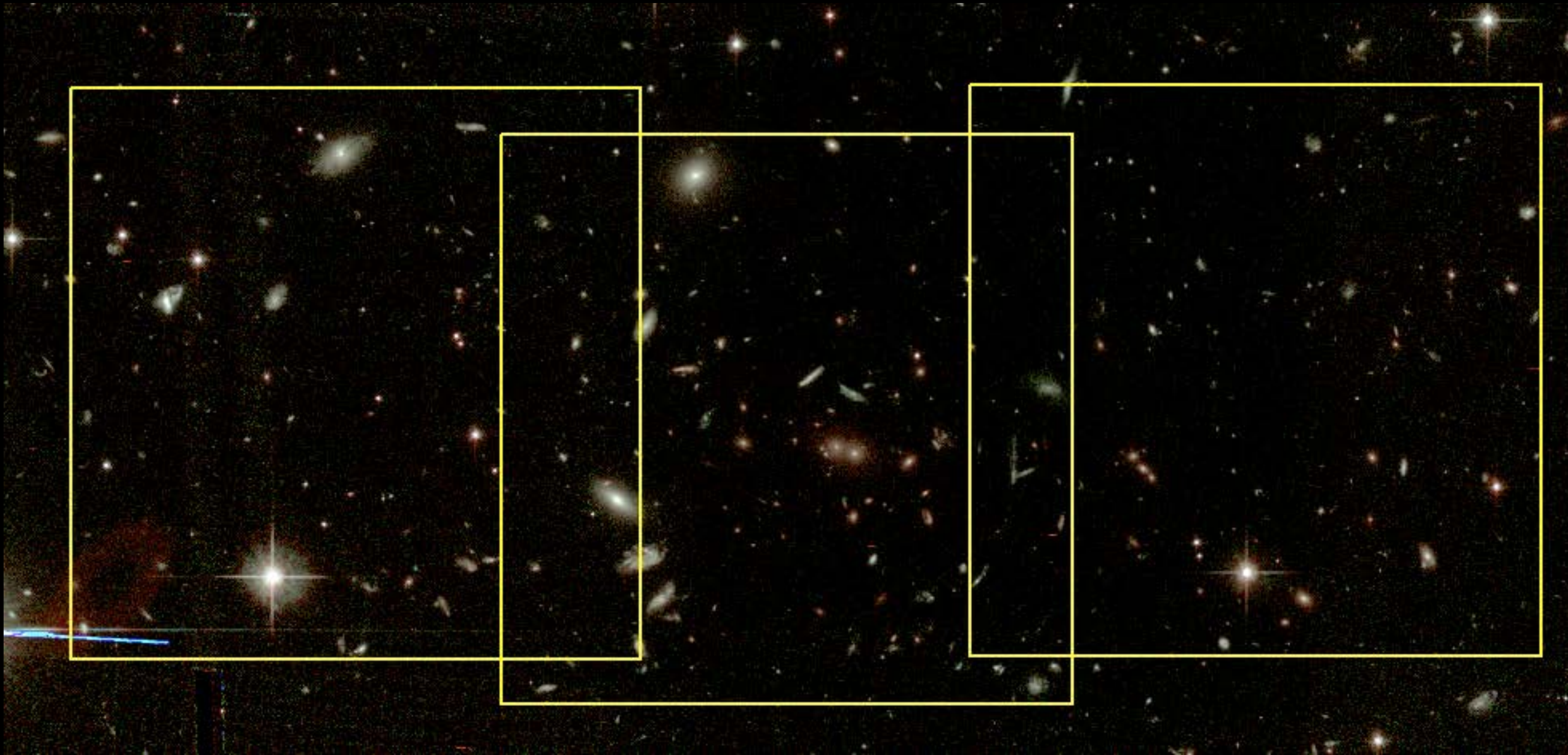
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astro-ph/0611502, Phys.Rev.D75:105018,2007

+manuscript in progress

Axion HDM: RDCS 1252/A2667+A2390



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+manuscript in progress

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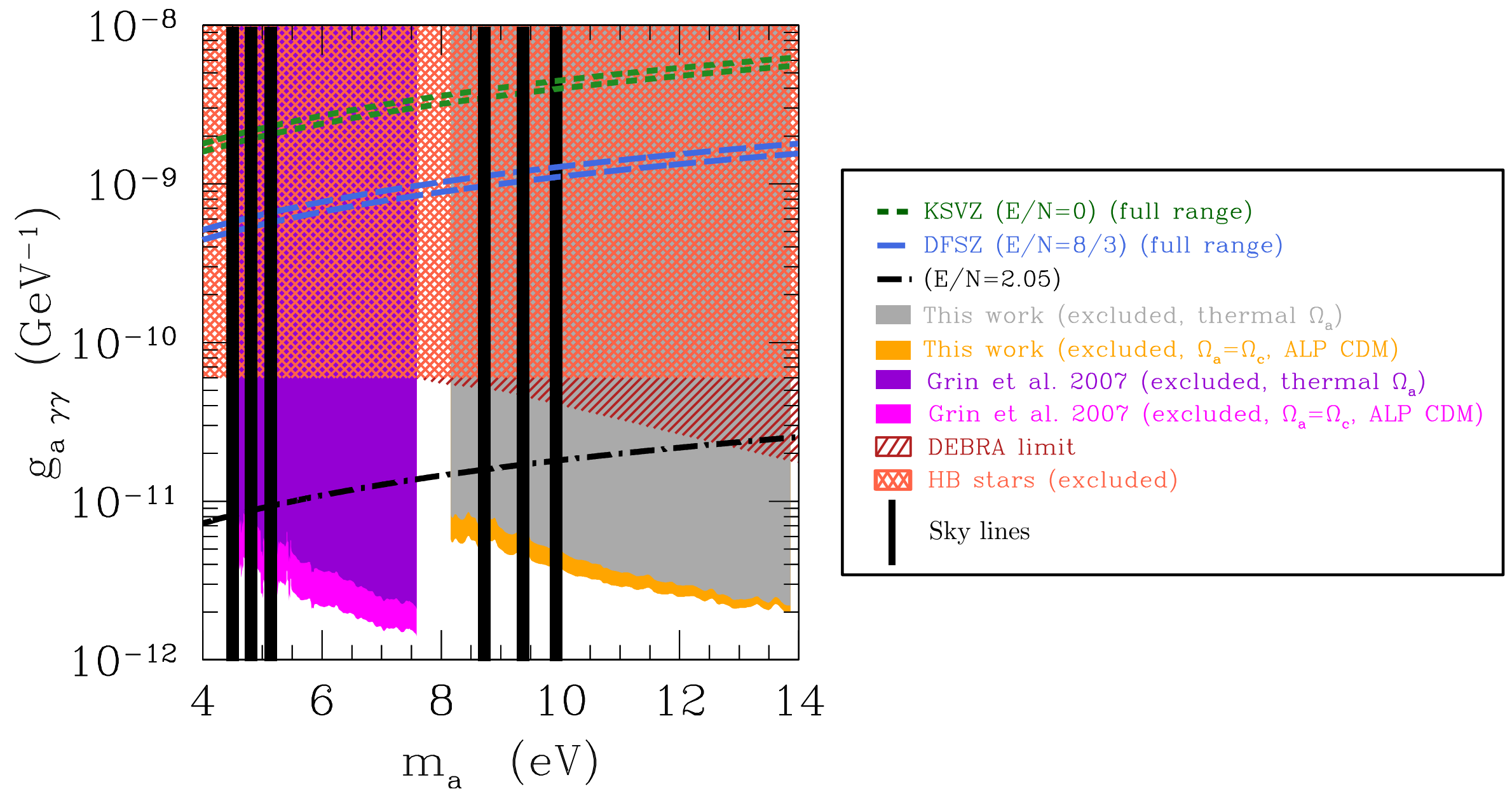


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Axion HDM: RDCS 1252/A2667+A2390

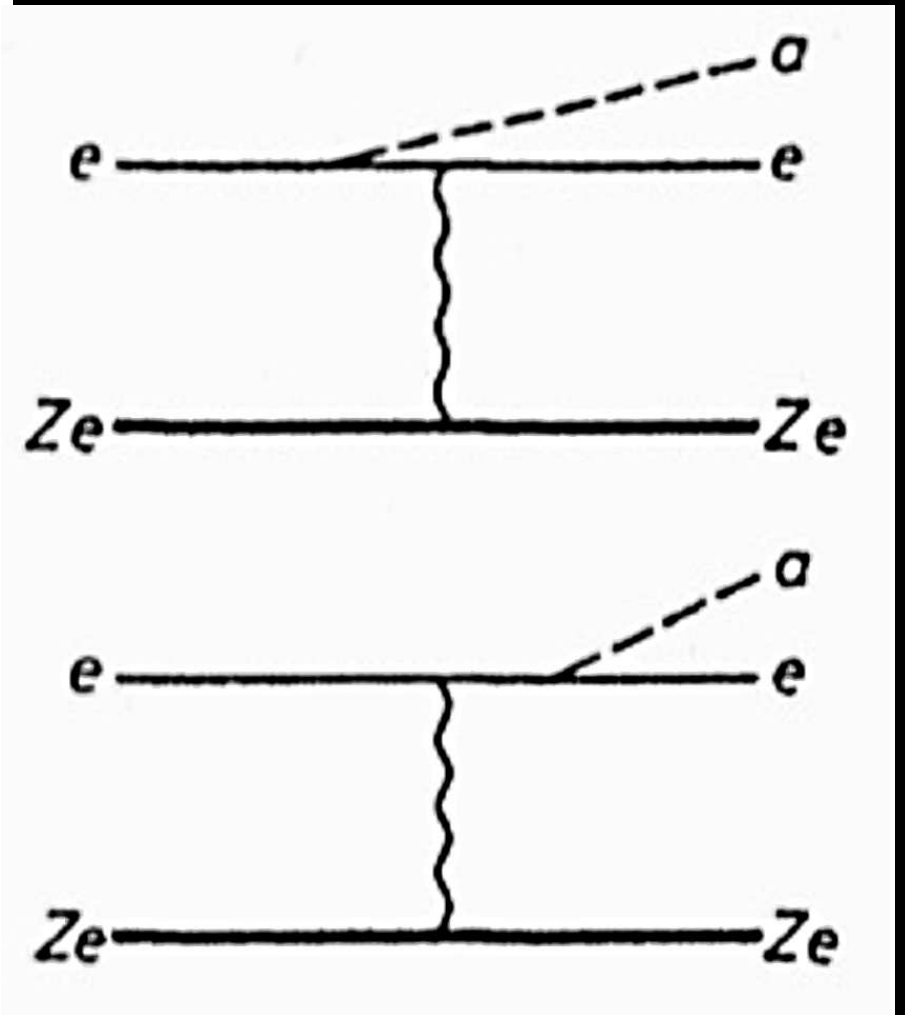
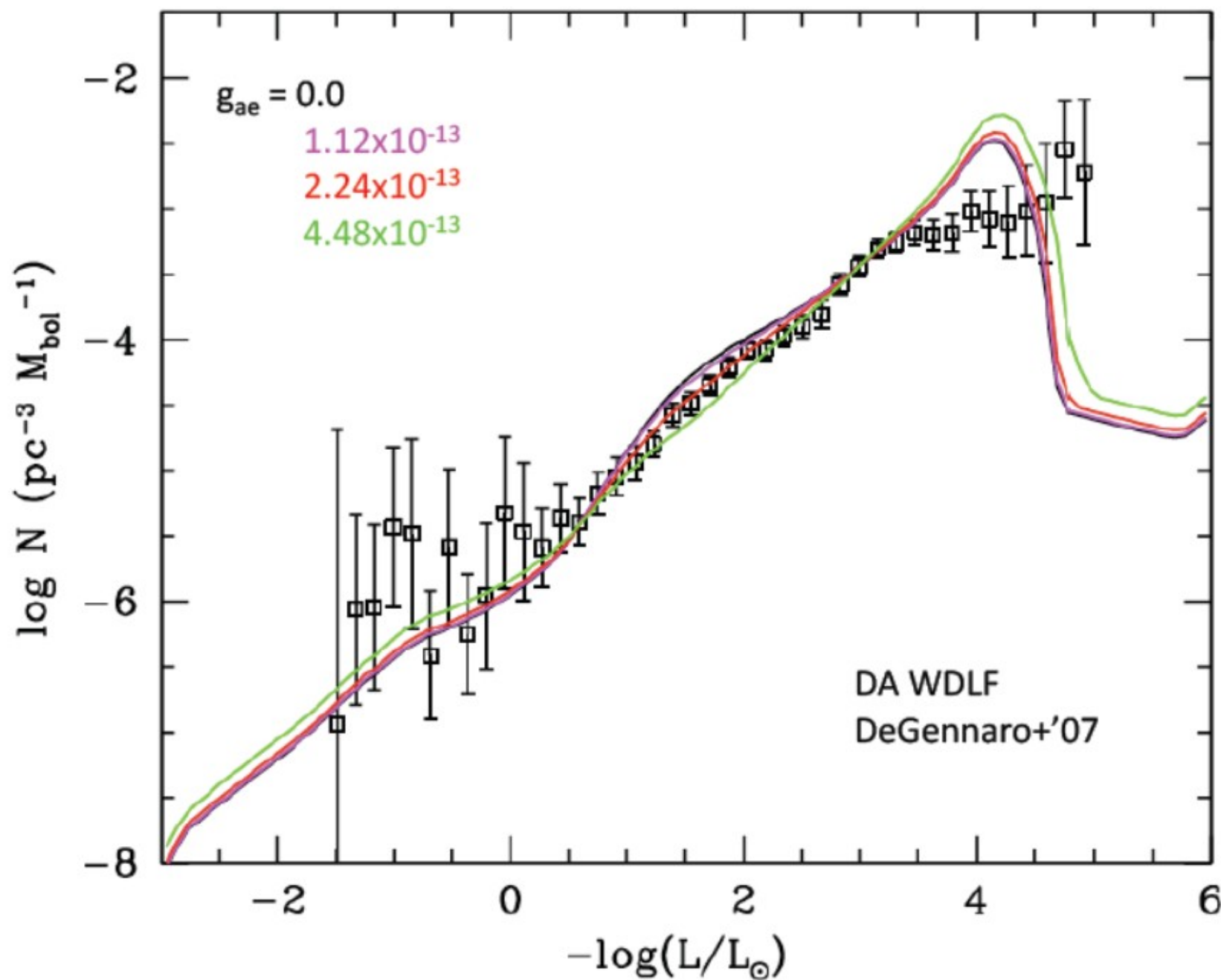


astro-ph/0611502, Phys.Rev.D75:105018,2007

+manuscript in progress

Making axions in degenerate stars, IV

- ✧ WDs are remnants of $1 M_{\odot}$ main – sequence stars
- ✧ Axio-electric coupling provides additional cooling channel



Axion HDM: Decay line

* Monochromatic emission line:

$$\lambda = \frac{c}{m_a c^2 / 2h} = 24800 \text{Å} \frac{(1 + z_c)}{m_a / \text{eV}}$$

* Resolvable $\delta\lambda = 195 \sigma_{1000} m_{a,\text{eV}}^{-1} \text{Å}$

* Axions decay:

$$\tau = 6.8 \times 10^{24} \xi^{-2} m_{a,\text{eV}}^{-5} \text{ s}$$

* Axion thermal abundance

$$\Omega_{\text{ax}} h^2 \simeq \frac{m_a}{130 \text{ eV}}$$

Axion HDM: Decay line

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Visible

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Following in the footsteps of Ressell, Bershadsky, Turner 1991

Classic axion window: $f_a < \max \{T_{\text{RH}}, H_{\text{I}}\}$

✳ Axion field is very inhomogeneous

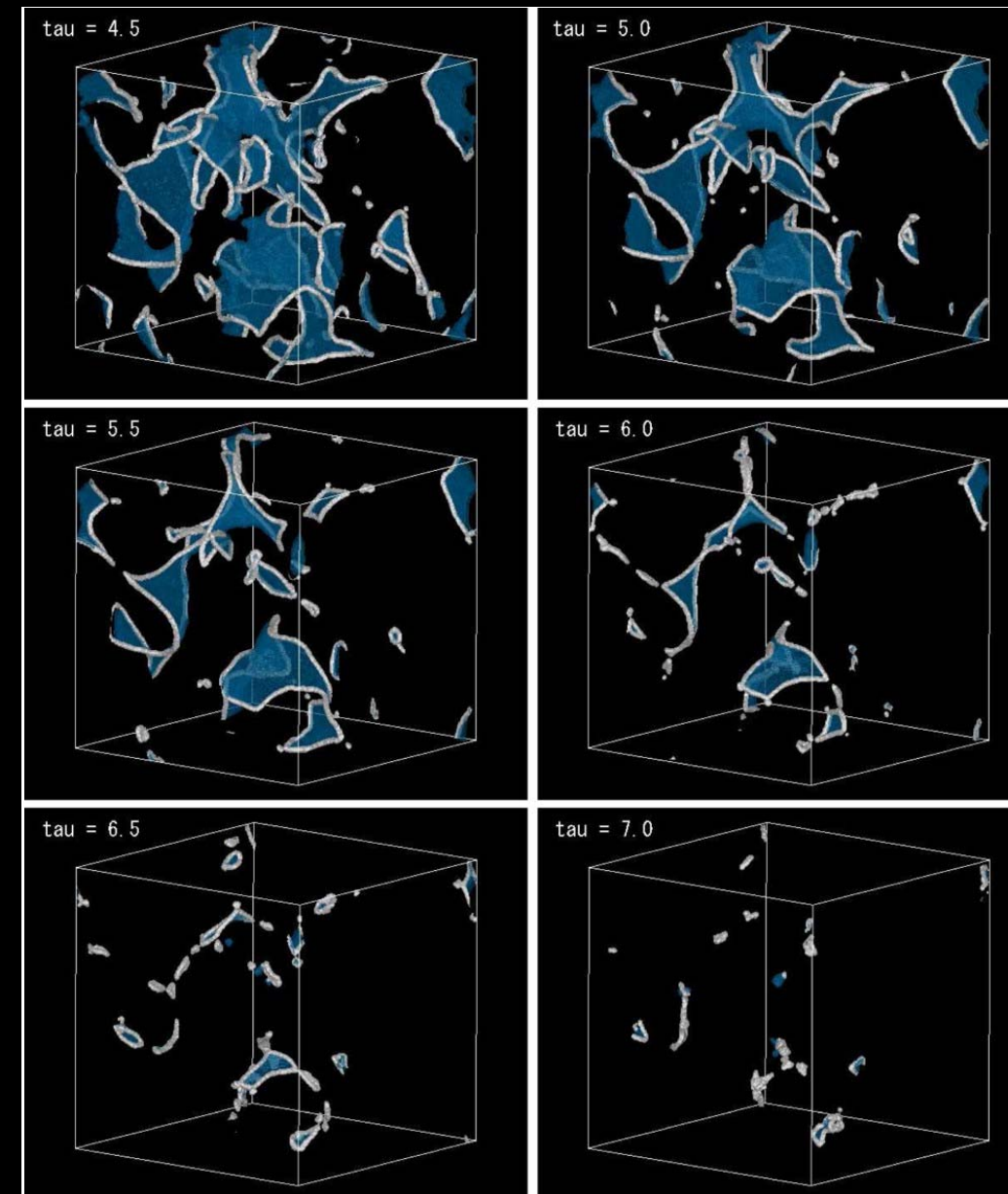
$$\langle \bar{\theta}_i^2 \rangle = \frac{\pi^2}{6}$$

✳ Defects [domain walls, strings, etc..]

$$\mathcal{O}(1) \lesssim \alpha_{\text{defect}} \lesssim \mathcal{O}(10^2)$$

✳ Abundance

$$\Omega_a h^2 \simeq 2.0 \{1 + f_{\text{defect}}\} \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{7/6}$$



Classic axion window: $f_a < \max \{T_{\text{RH}}, H_{\text{I}}\}$

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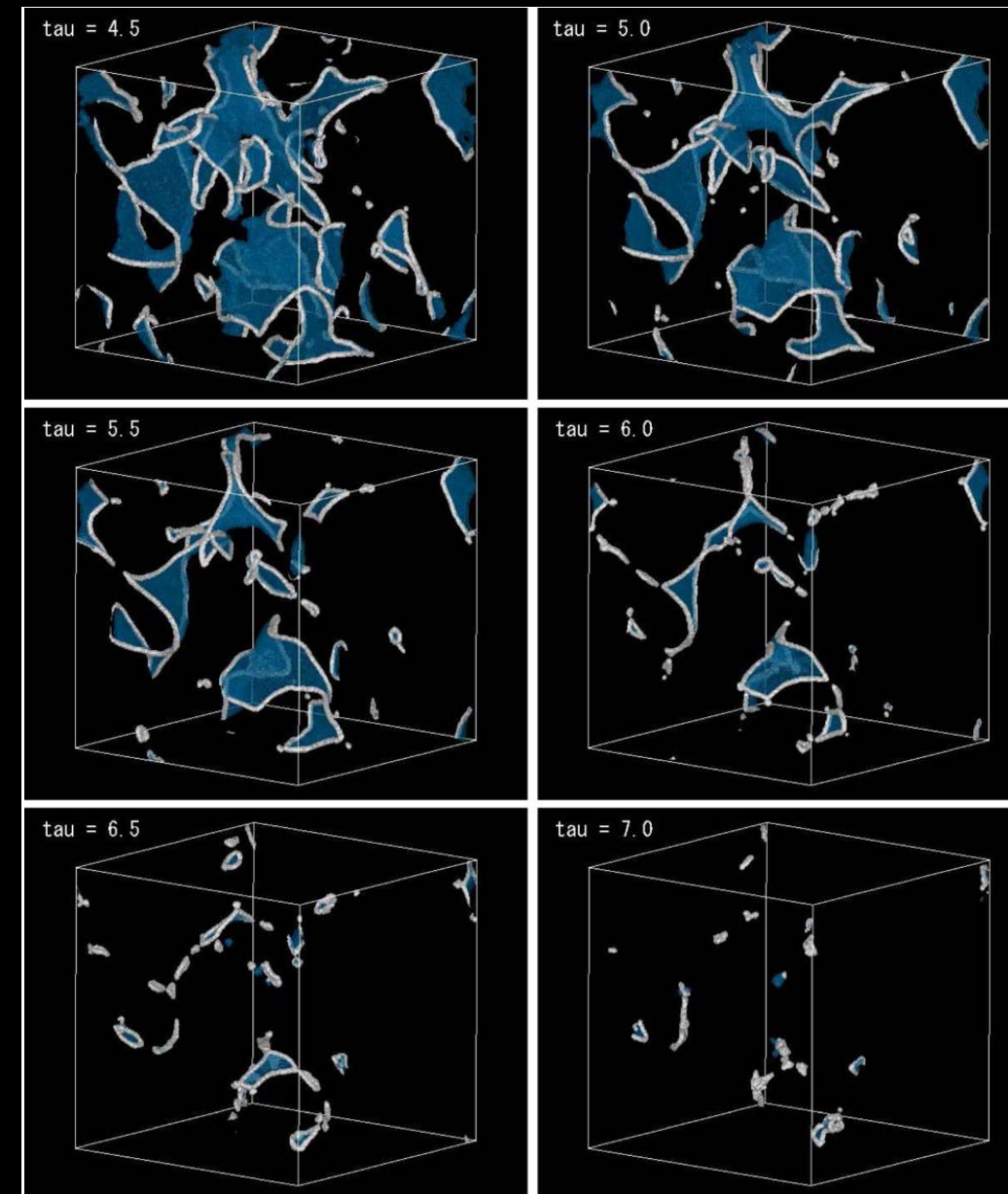
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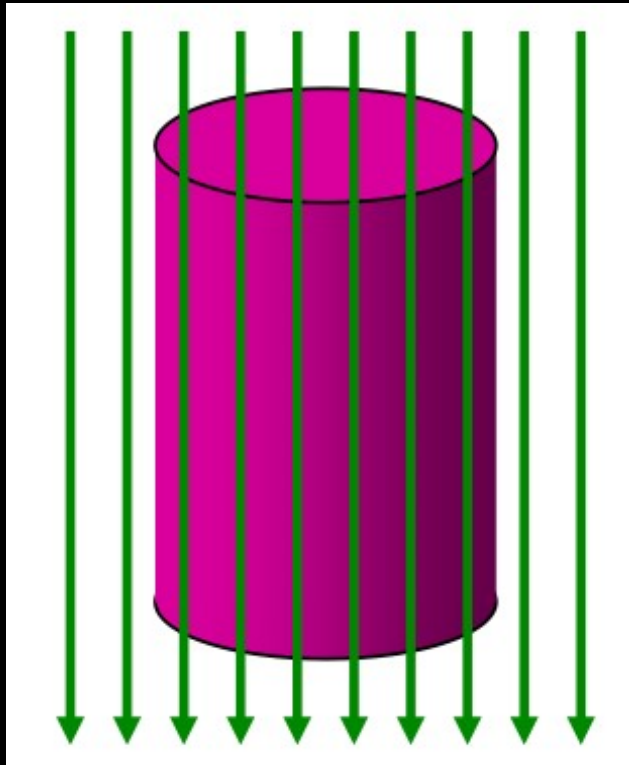
CONTROVERSY!

✳ Abundance

$$\Omega_a h^2 \simeq 2.0 \{1 + f_{\text{defect}}\} \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{7/6}$$



* Magnetized RF Cavity

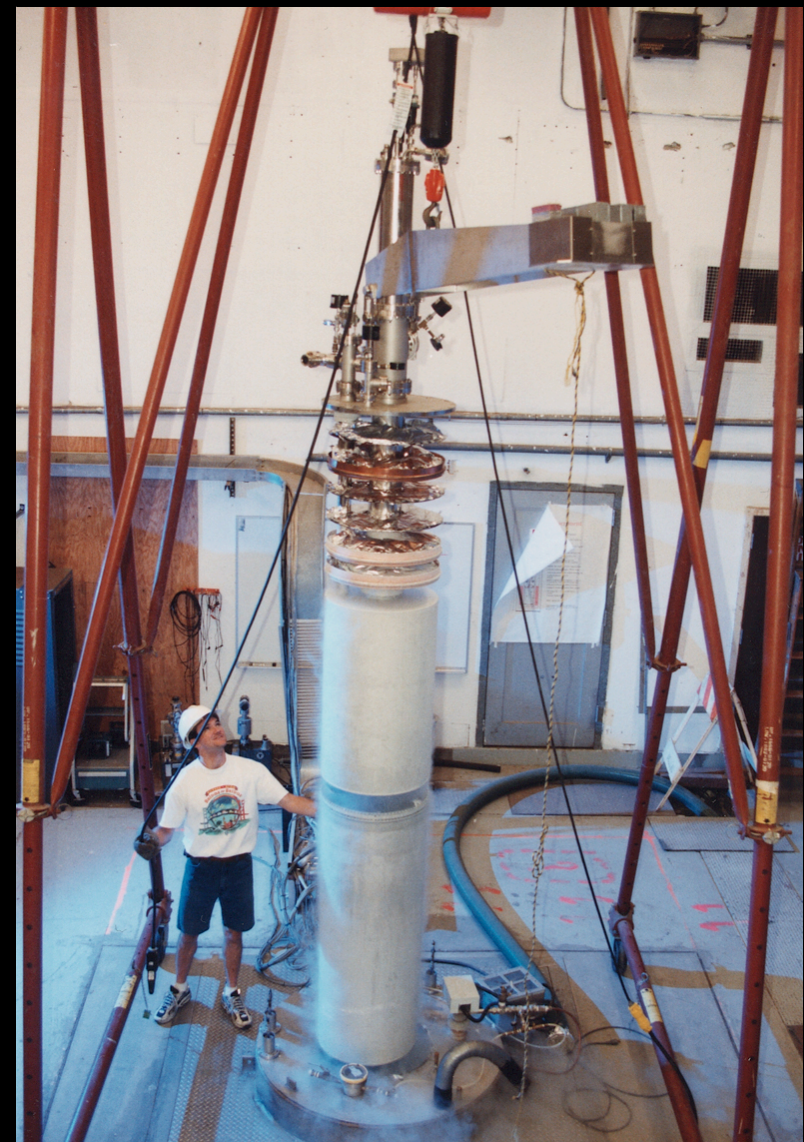


- * Axion excites cavity (TEM) modes [cavity must be tuned]

$$E_\gamma = m_a c^2$$

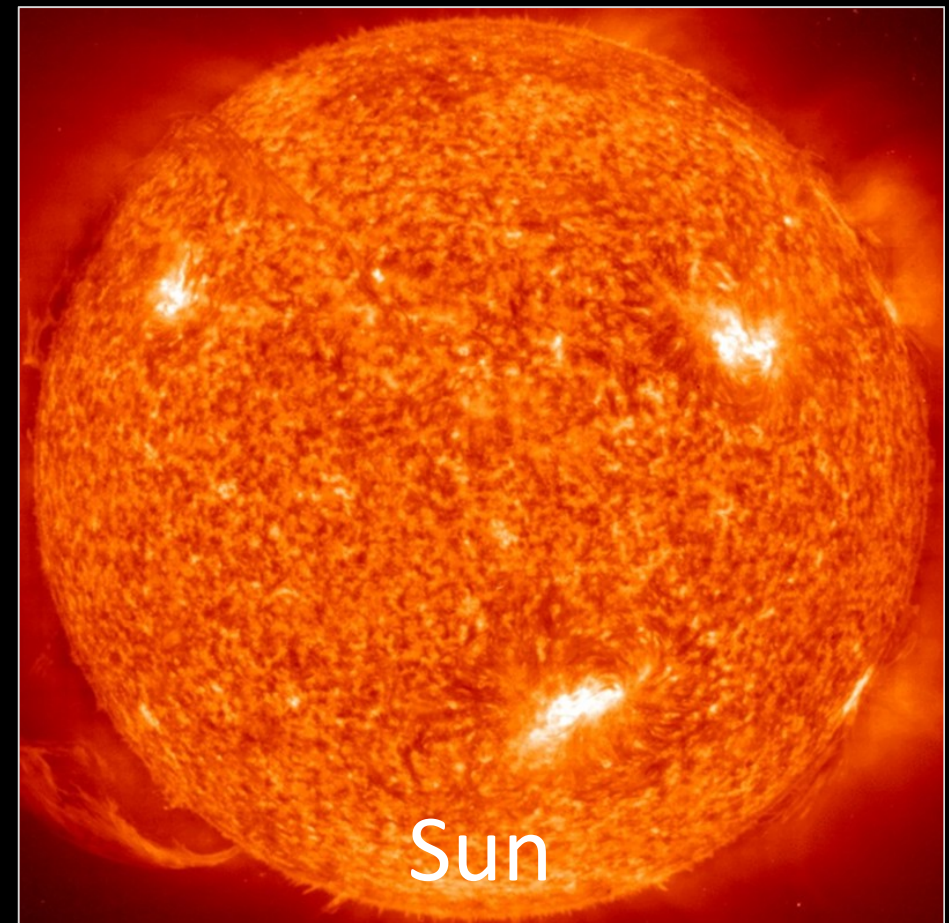
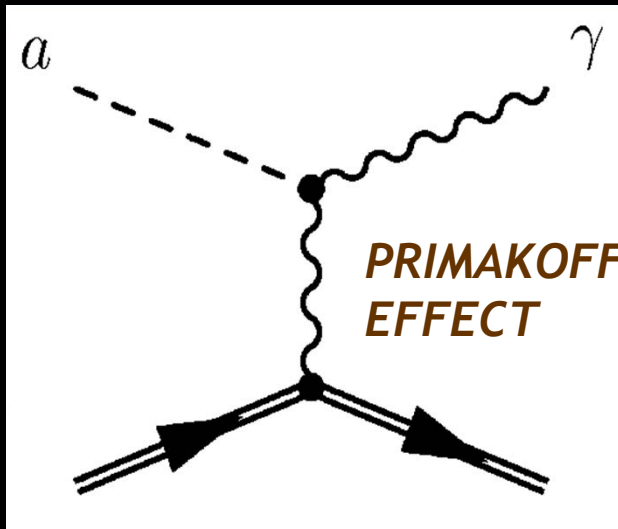
* Power

$$\text{Power} = g_{a\gamma}^2 \frac{\overset{\text{Volume}}{V} B^2 \underset{\substack{\text{Axion energy density} \\ m_a}}{\rho_a} \overset{\text{Quality factor}}{Q} \sim 10^{-21} \text{ Watts}$$



Making axions in stars

* Primakoff process

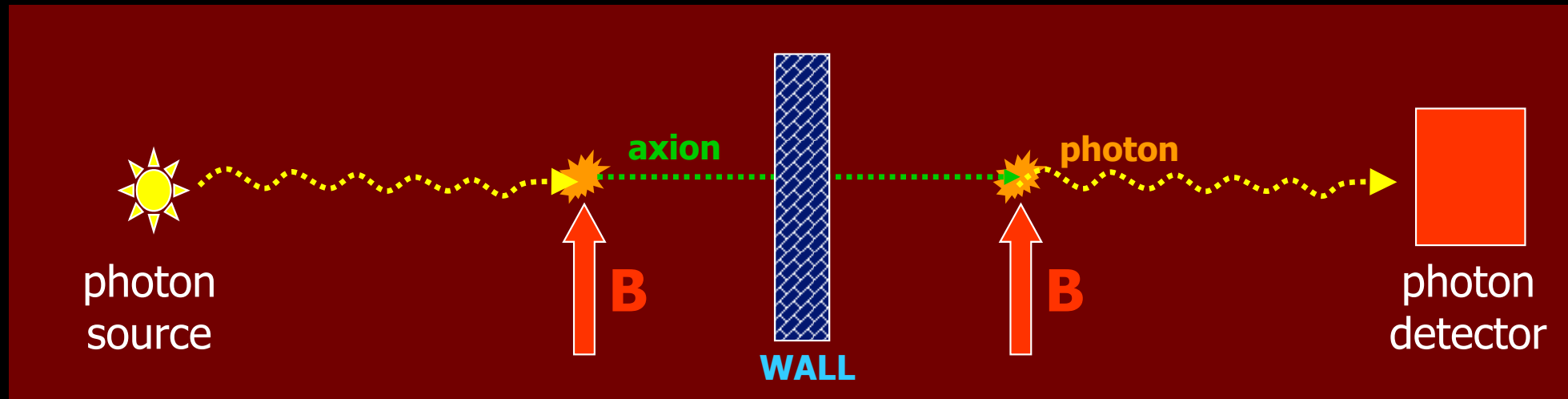


* Lifetime of our own sun/Solar luminosity/helioseismology impose constraint

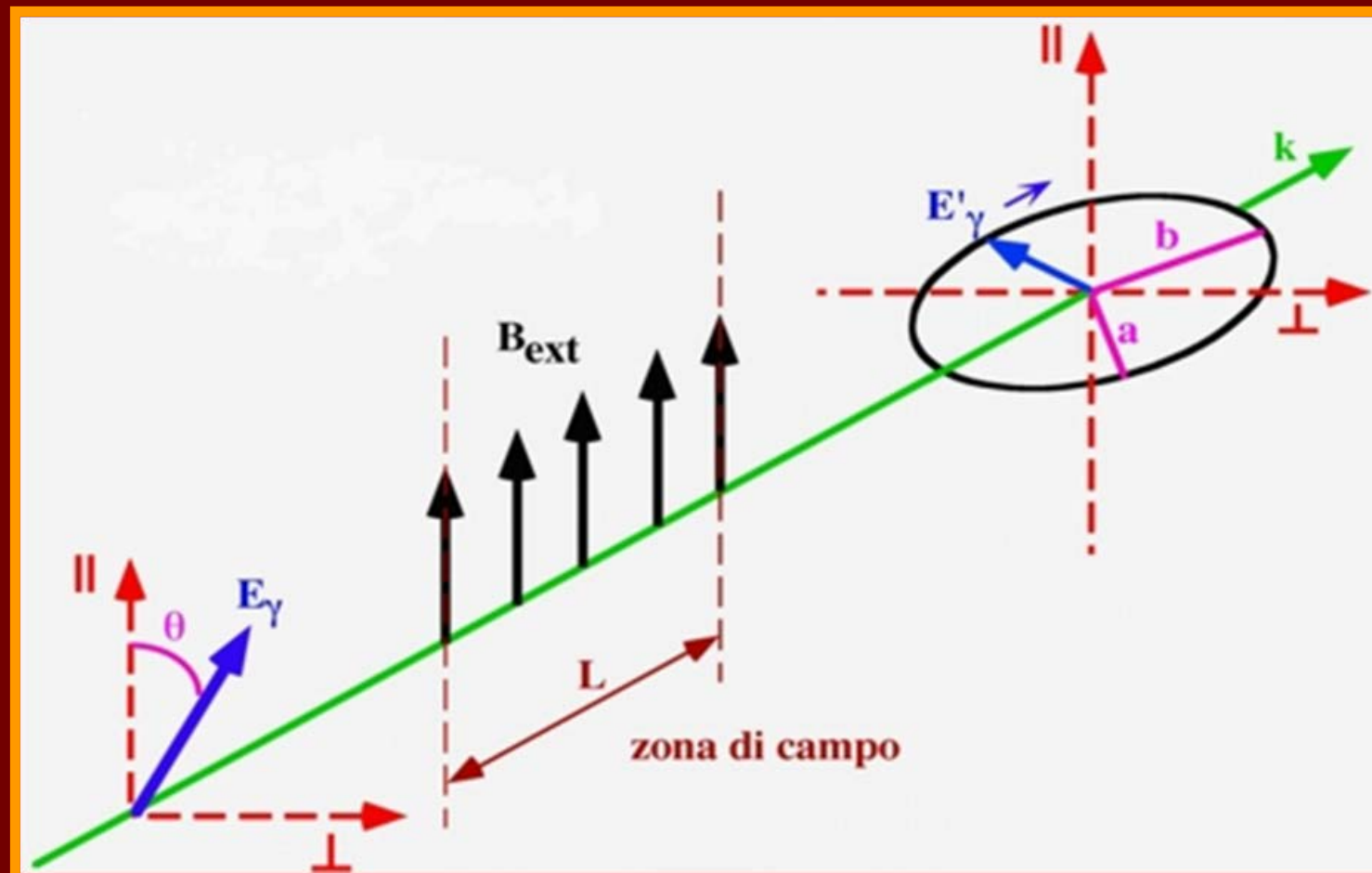
$$g_{a\gamma\gamma} \lesssim 1 - 3 \times 10^{-9} \text{ GeV}^{-1}$$

Laser experiments

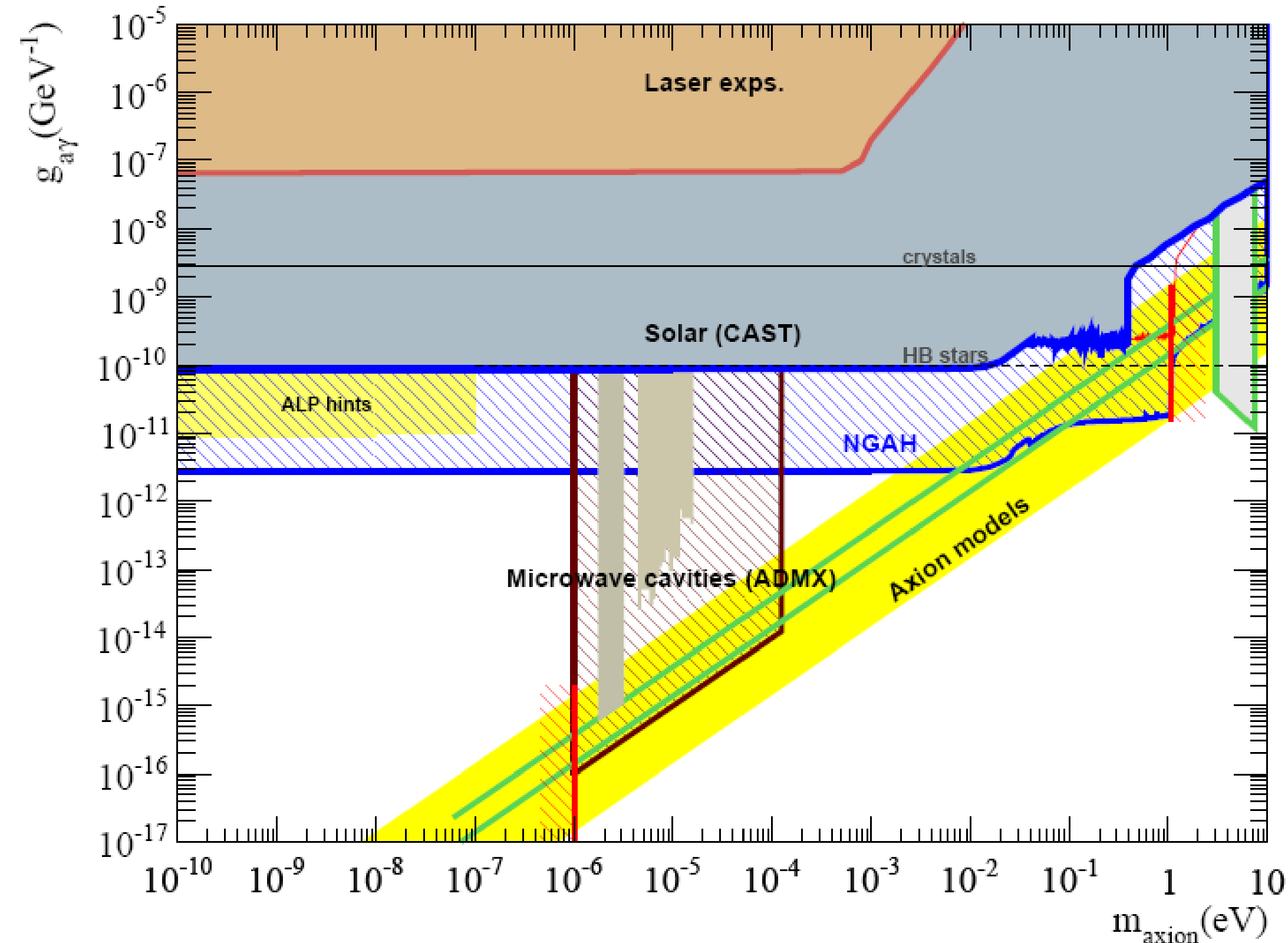
Light shining through walls (e.g. GammeV)



Polarization experiments (e.g. PVLAS)



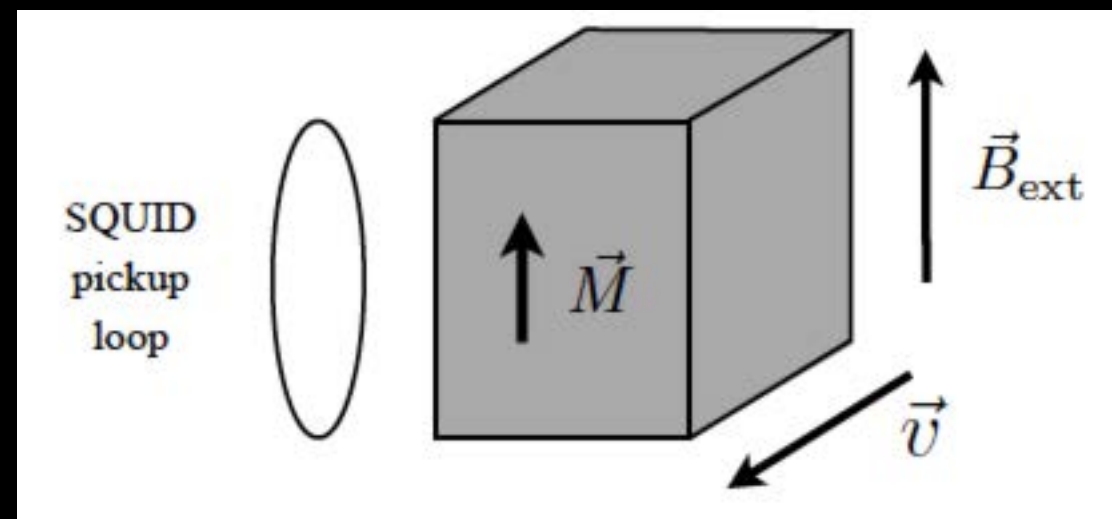
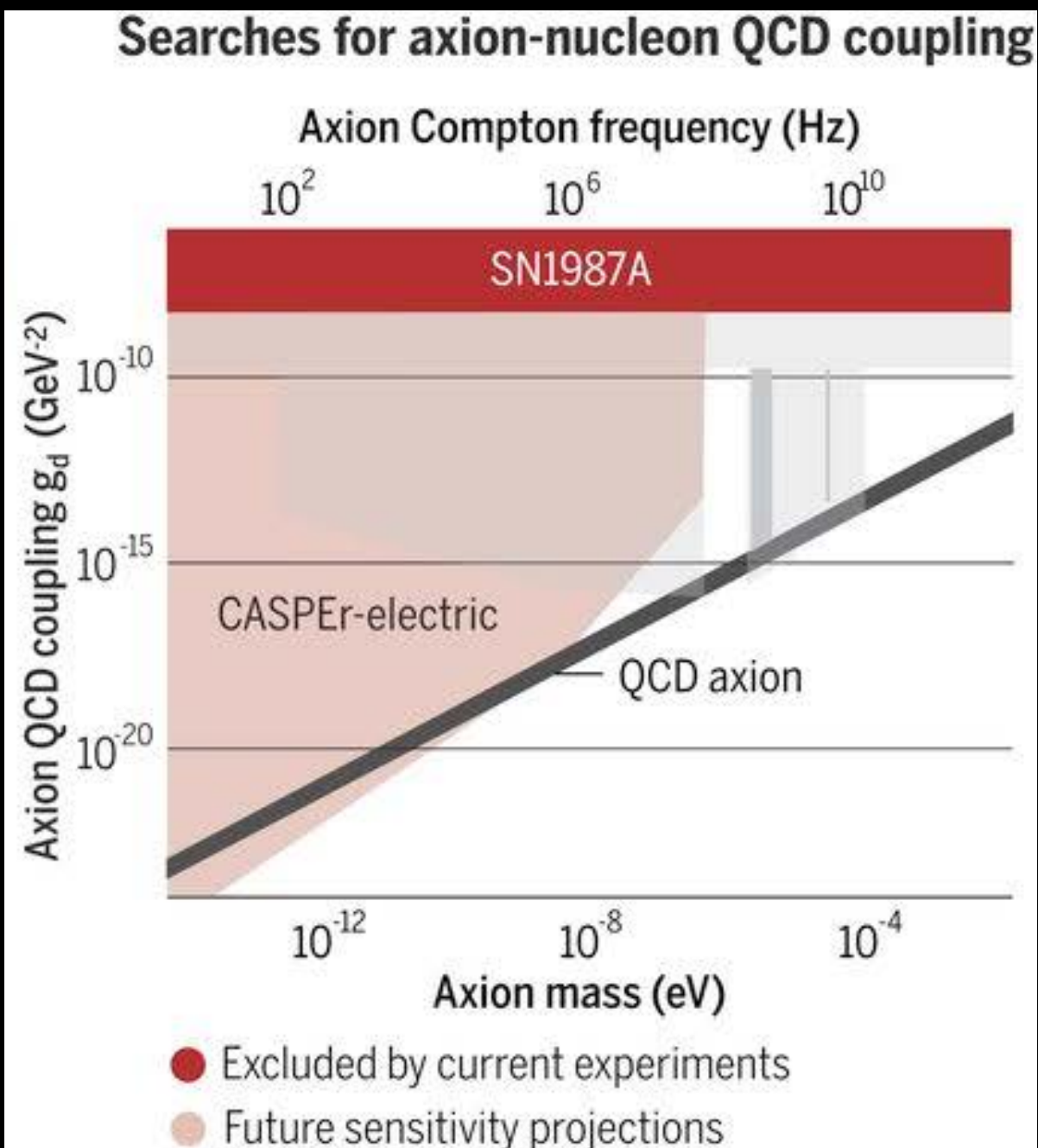
Limits and horizon



Other methods

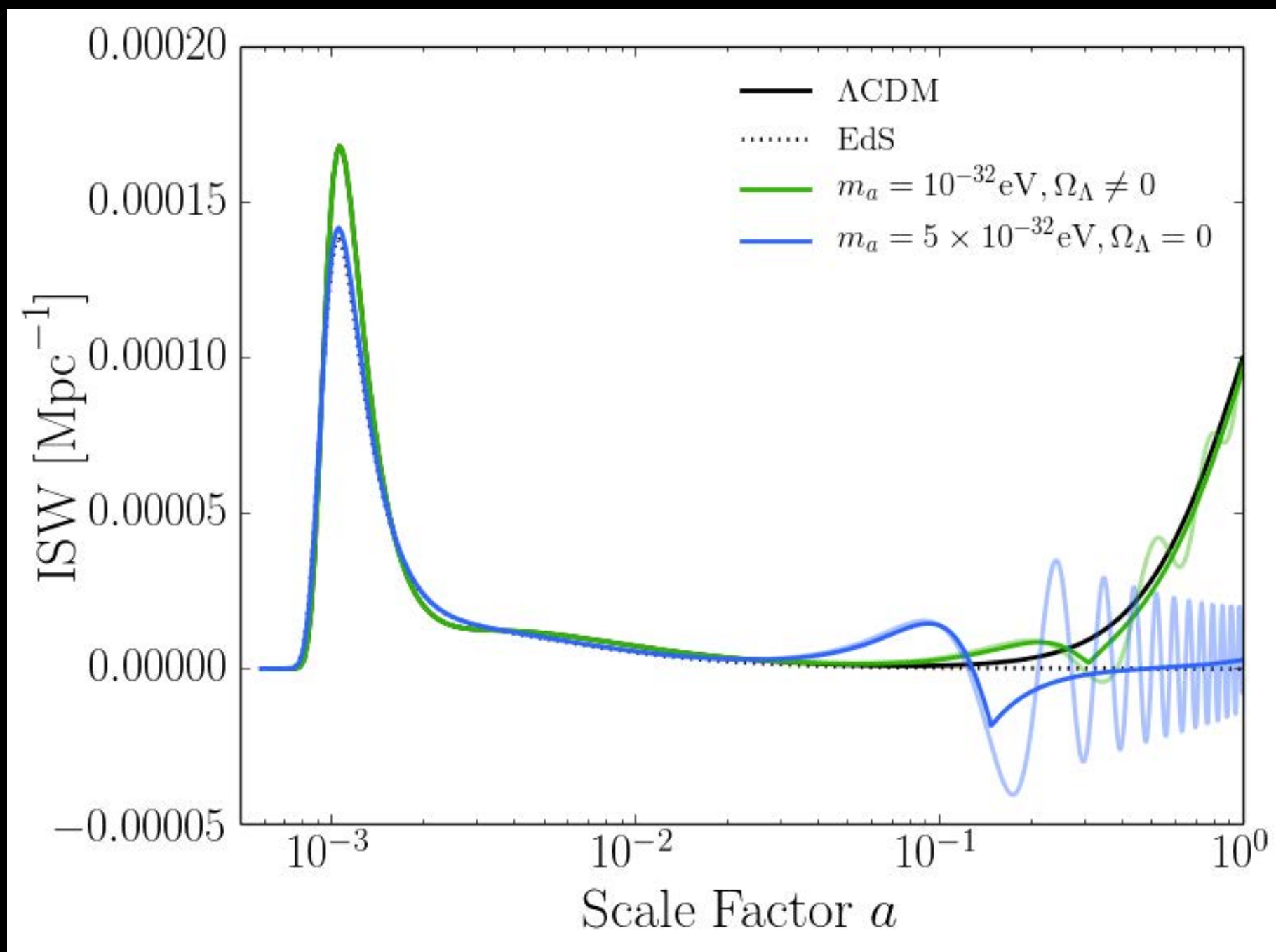
- * Spectra of magnetic white dwarves [New]
- * Extragalactic background light
- * Pulsating white dwarf seismology [New]
- * Dimming of gamma-ray blazars [New]
- * Two-photon decays in galaxy clusters
- * Light degrees of freedom at BBN [New]
- * Helioscope in space [New]
- * Supernovae 1987a
- * White dwarf luminosity function
- * Oscillating electric dipole moments of nucleons [NEW]

Demille, Doyle, Sushkov (Science 2017), idea of Graham and Rajendran (2014)

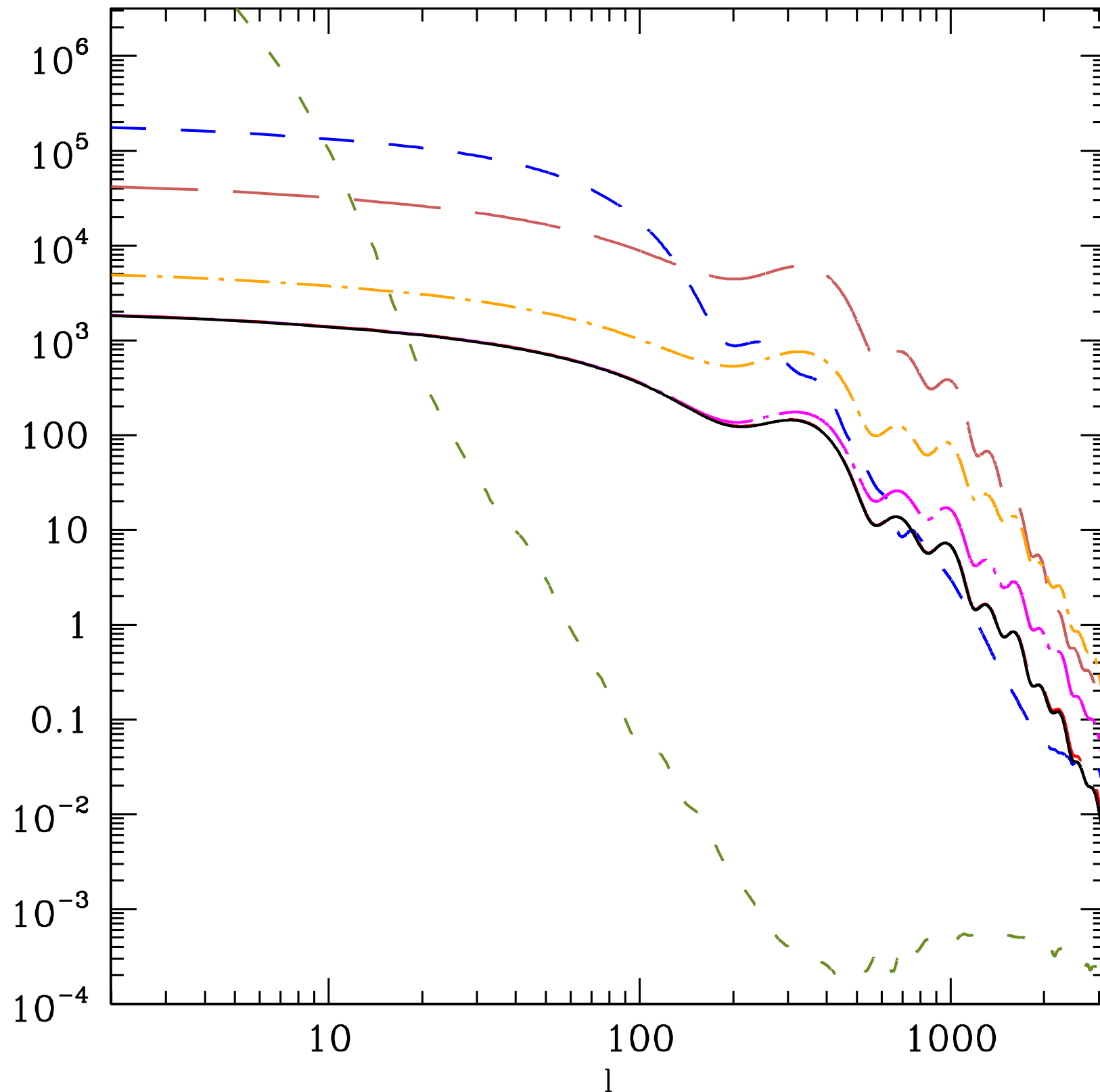


ULA Search Technical Details

ISW TEST



Getting under the hood: The need for numerical care



Getting under the hood: The need for numerical care

$$\dot{\delta}_a = 3\mathcal{H} [w_a - 1] \delta_a - (1 + w_a) \left(kv_a + \dot{h} \right)$$

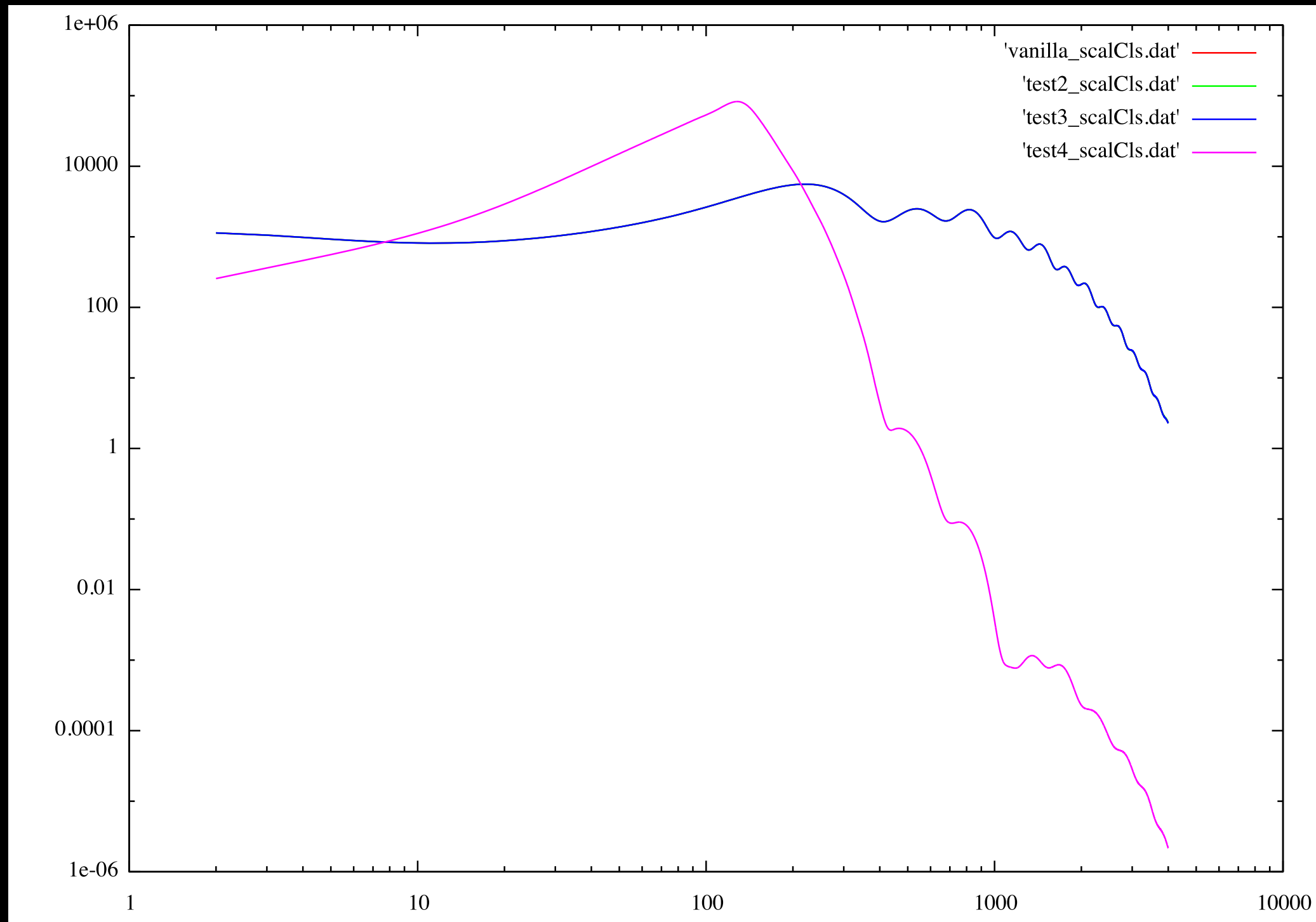
$$\dot{v}_a = -3\mathcal{H} [1 - 3w_a] v_a - \frac{\dot{w}_a}{(1 + w_a)} v_a + \frac{k\delta_a}{(1 + w_a)}$$

$$\dot{w}_a = -3\mathcal{H} (1 + w_a) [c_{\text{ad}}^2 - w_a]$$

$$c_{\text{ad}}^2 = \frac{\dot{P}_a}{\dot{\rho}_a} = -1 + \frac{2m_a a}{\mathcal{H}} \sqrt{\frac{(1 - w_a)}{(1 + w_a)}}$$

$$\dot{\rho}_a = -3\mathcal{H} \rho_a (1 + w_a)$$

Getting under the hood: The need for correct (super-horizon) initial conditions



Getting under the hood: The need for correct (super-horizon) initial conditions

Synchronous gauge 00-Einstein $\dot{h} \propto \eta \left[\frac{3\delta_{\text{R}}}{a^2} + 3a^2 \mathcal{A} \delta_a \right]$

Getting under the hood: The need for correct (super-horizon) initial conditions

Synchronous gauge 00-Einstein

$$\dot{h} \propto \eta \left[\cancel{\frac{3\delta_R}{a^2}} + 3a^2 \mathcal{A} \delta_a \right]$$

Perrotta and Baccigalupi, astro-ph/9811156

Getting under the hood: The need for correct (super-horizon) initial conditions

Synchronous gauge 00-Einstein

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$$\dot{h} \propto \eta \left[\cancel{\frac{3\delta_R}{a^2}} + 3a^2 \mathcal{A} \delta_a \right]$$

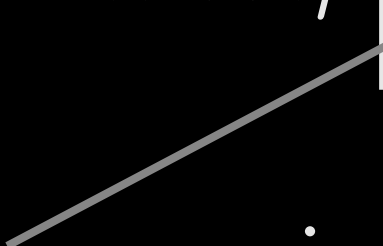
$$\dot{\delta}_\gamma \simeq -\frac{\dot{h}}{2}$$

NOT KOSHER!

Getting under the hood: The need for correct (super-horizon) initial conditions

Synchronous gauge 00-Einstein

Perrotta and Baccigalupi, astro-ph/9811156

$$\dot{h} \propto \eta \left[\cancel{\frac{3\delta_R}{a^2}} + 3a^2 \mathcal{A} \delta_a \right]$$
$$\dot{\delta}_\gamma \simeq -\frac{\dot{h}}{2}$$


NOT KOSHER!

Solve Eigensystem and expand systematically

$$\frac{d\vec{U}_{\vec{k}}}{d \ln x} = (\underline{A}_0 + \underline{A}_1 x + \dots \underline{A}_n x^n) \vec{U}_{\vec{k}}$$

Bucher, Moodley, and Turok, PRD62, 083508, sol'ns can be obtained using this technique, outlined in Doran et al. , astro-ph/0304212

ULAS AND THE ANGULAR SOUND HORIZON

$$\theta_s \equiv \frac{r_s}{d_A(z = 1100)} = \left(l_{\text{CMB}}^{\text{peak}}\right)^{-1}$$

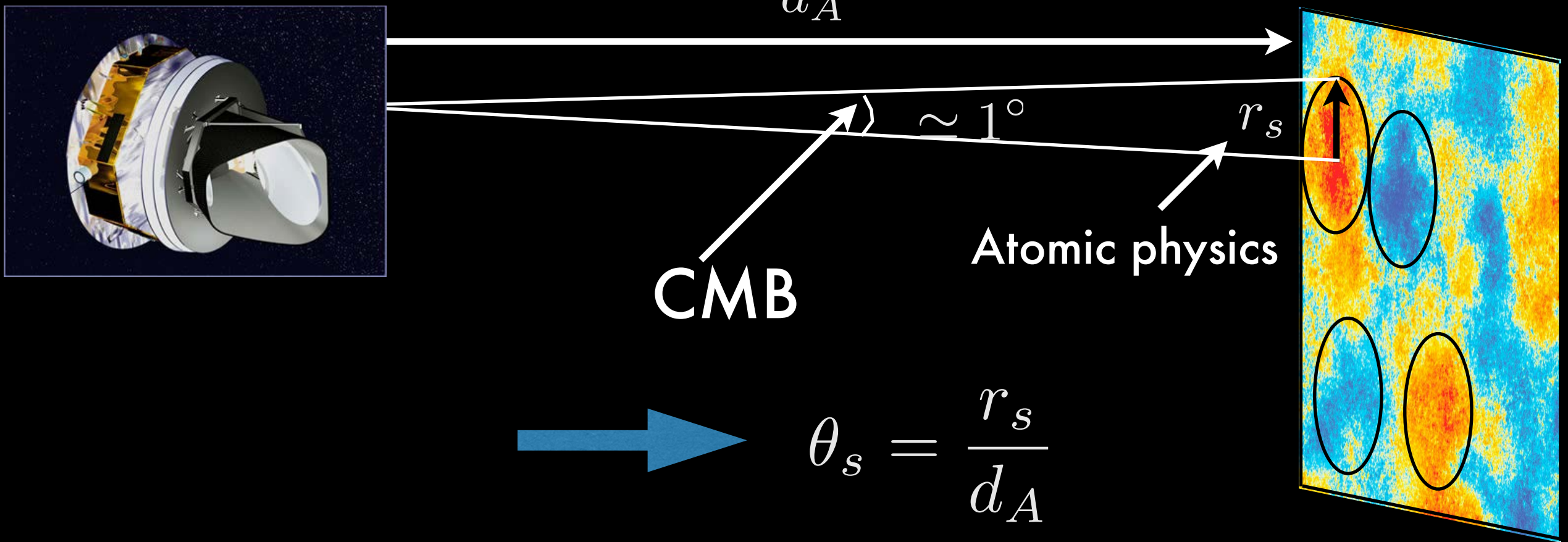
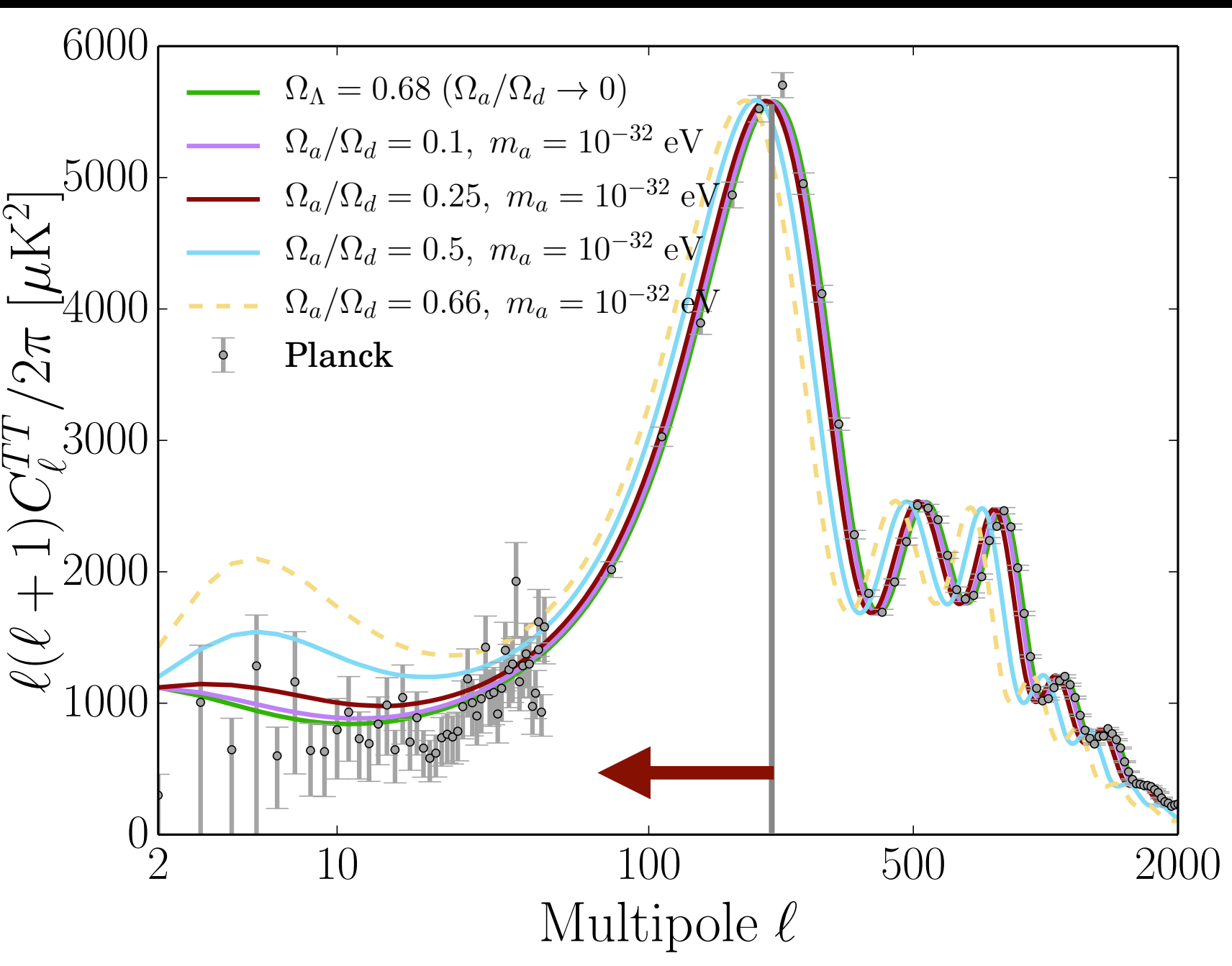


Diagram by T. Smith (used with permission)

ULAS AND THE ANGULAR SOUND HORIZON



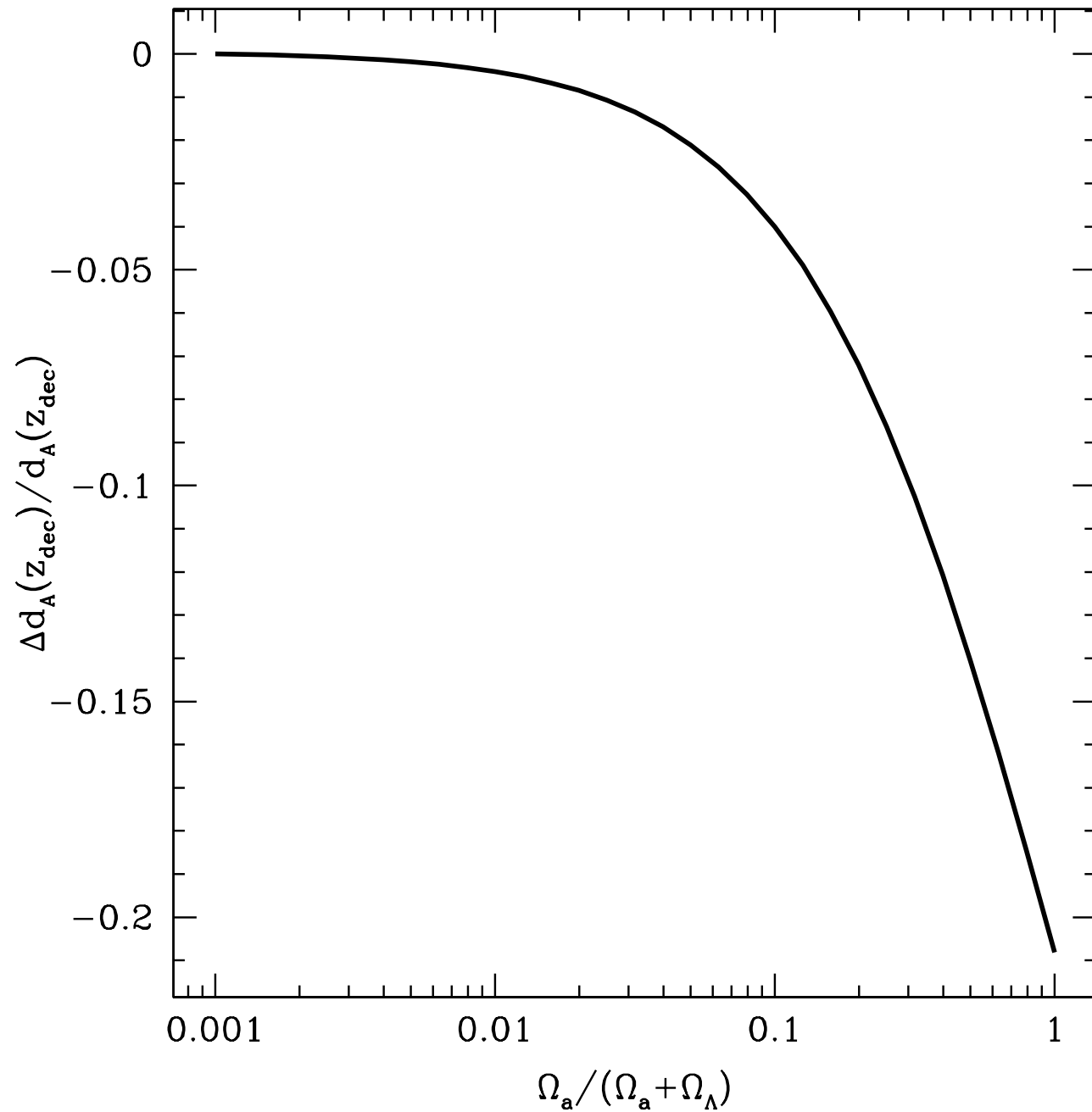
$$\theta_s \equiv \frac{r_s}{d_A(z=1100)} = \left(l_{\text{CMB}}^{\text{peak}}\right)^{-1}$$

$$d_A \propto \int \frac{dz}{H(z)}$$

$$H(z) = H_0 \left\{ \frac{\Omega_m}{a^3} + \frac{\Omega_{\text{axion}}}{a^3 \int [1+w(\eta)] d\eta} \right\}^{1/2}$$

Faster early expansion brings LSS closer

ULAS AND THE ANGULAR SOUND HORIZON



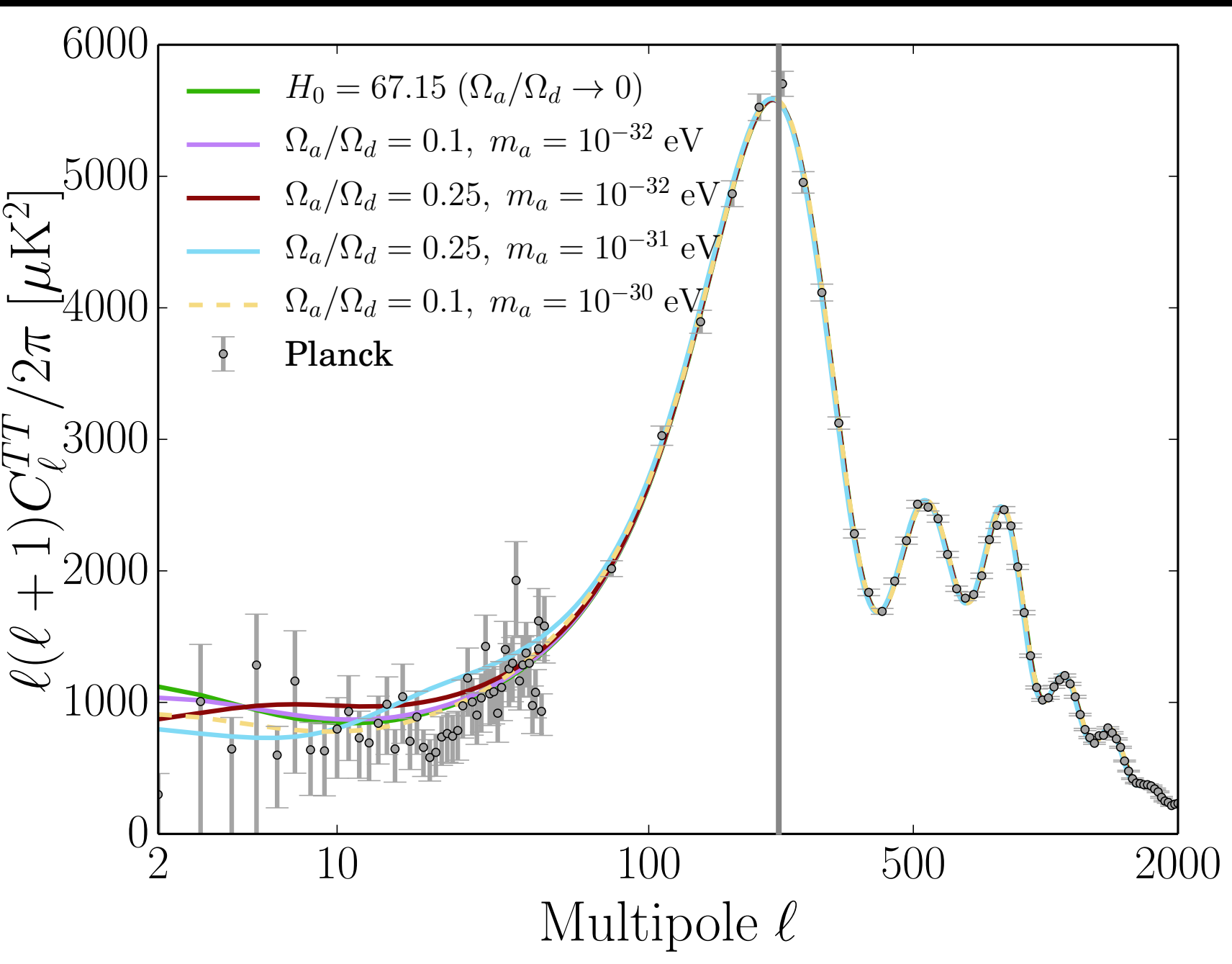
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ULAS AND THE ANGULAR SOUND HORIZON



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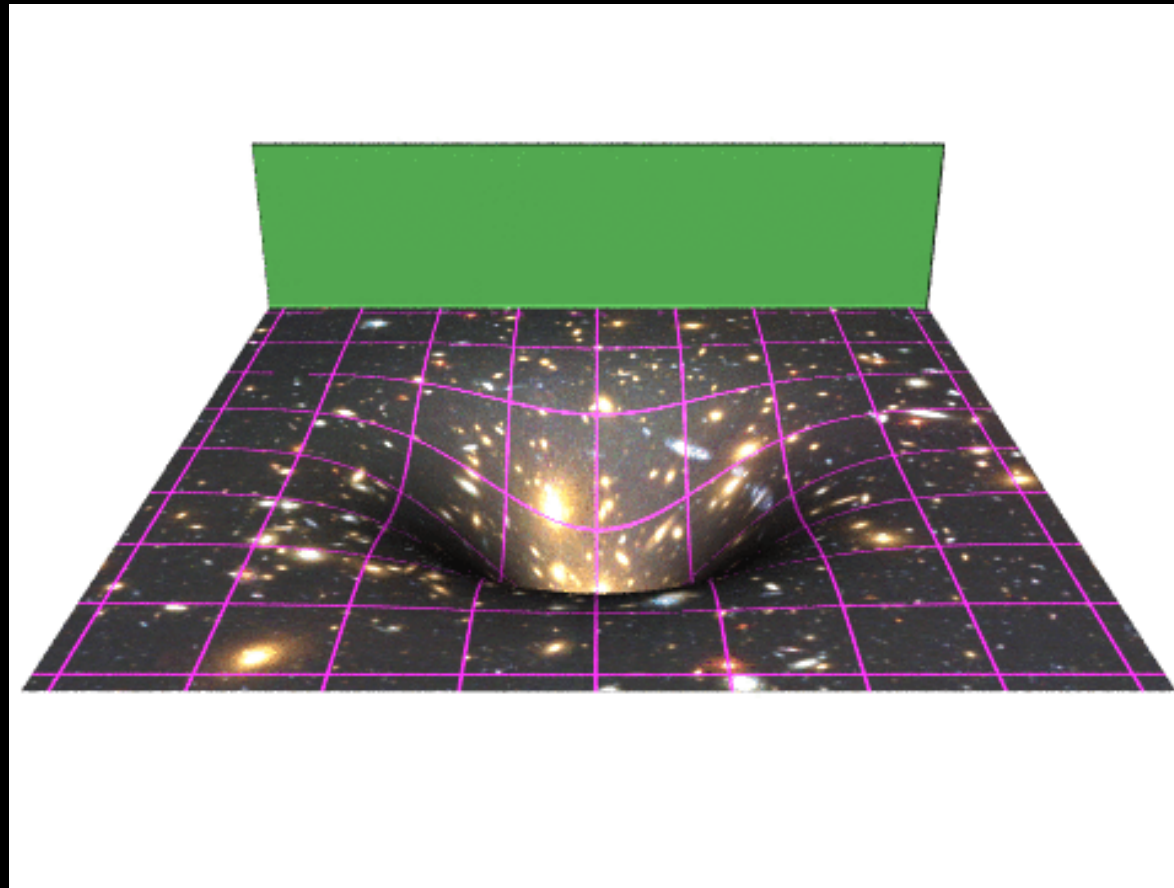
Absorb and lock onto
usual peaks by lowering
 H_0

$$H(z) = H_0 \left\{ \frac{\Omega_m}{a^3} + \frac{\Omega_{\text{axion}}}{a^3 \int [1+w(\eta)] d\eta} \right\}^{1/2}$$

Faster early expansion brings LSS closer

ULAs and the CMB: high mass and early ISW

Higher mass (DM-like) case: high- l ISW



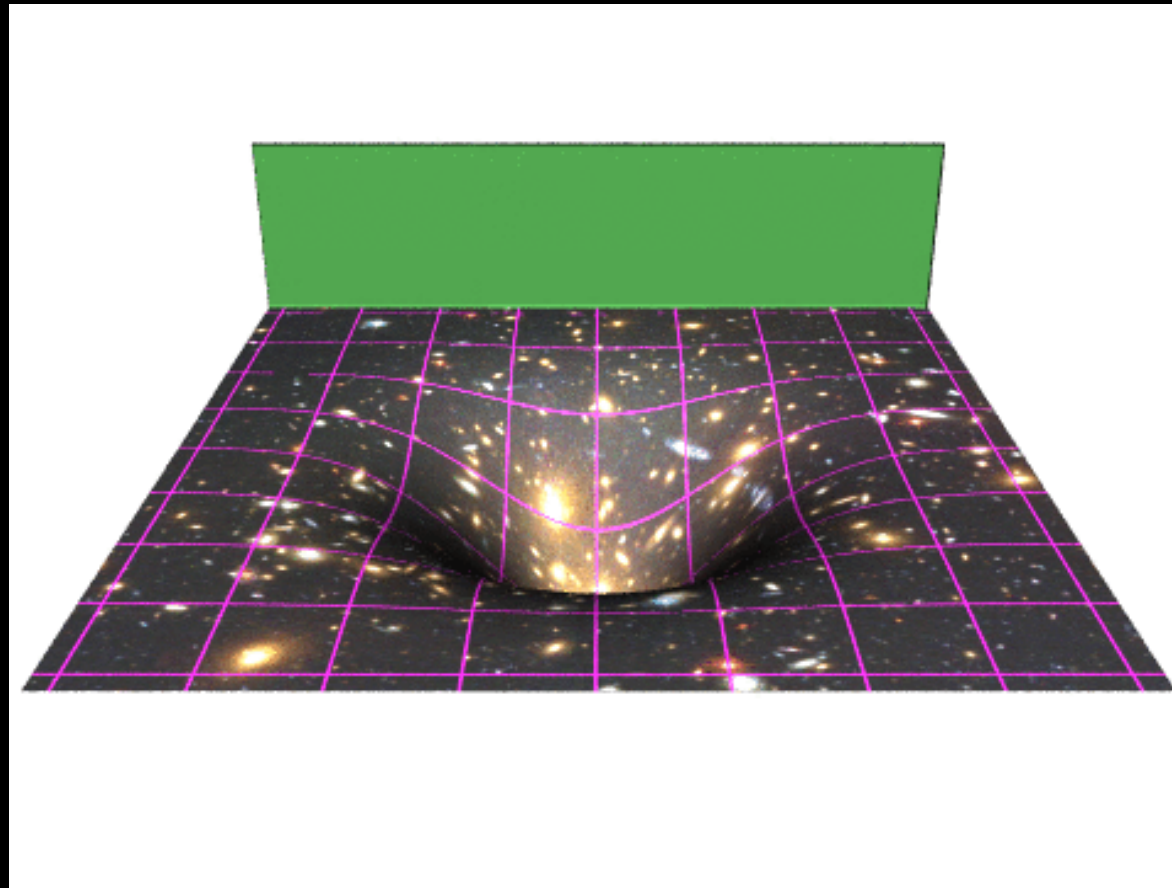
CMB temperature anisotropies from potential decay

$$\Delta T_{\text{ISW}} = -2 \int_0^{\eta_{\text{dec}}} d\eta \dot{\Phi}(\eta, \hat{n}\eta)$$

$$\Phi \propto \frac{1}{k^2} \left\{ \frac{\Omega_m \delta_m \left(1 - \frac{\Omega_a}{\Omega_m} \right)}{a^3} + \frac{\delta_R \Omega_R}{a^4} \right\}$$

ULAs and the CMB: high mass and early ISW

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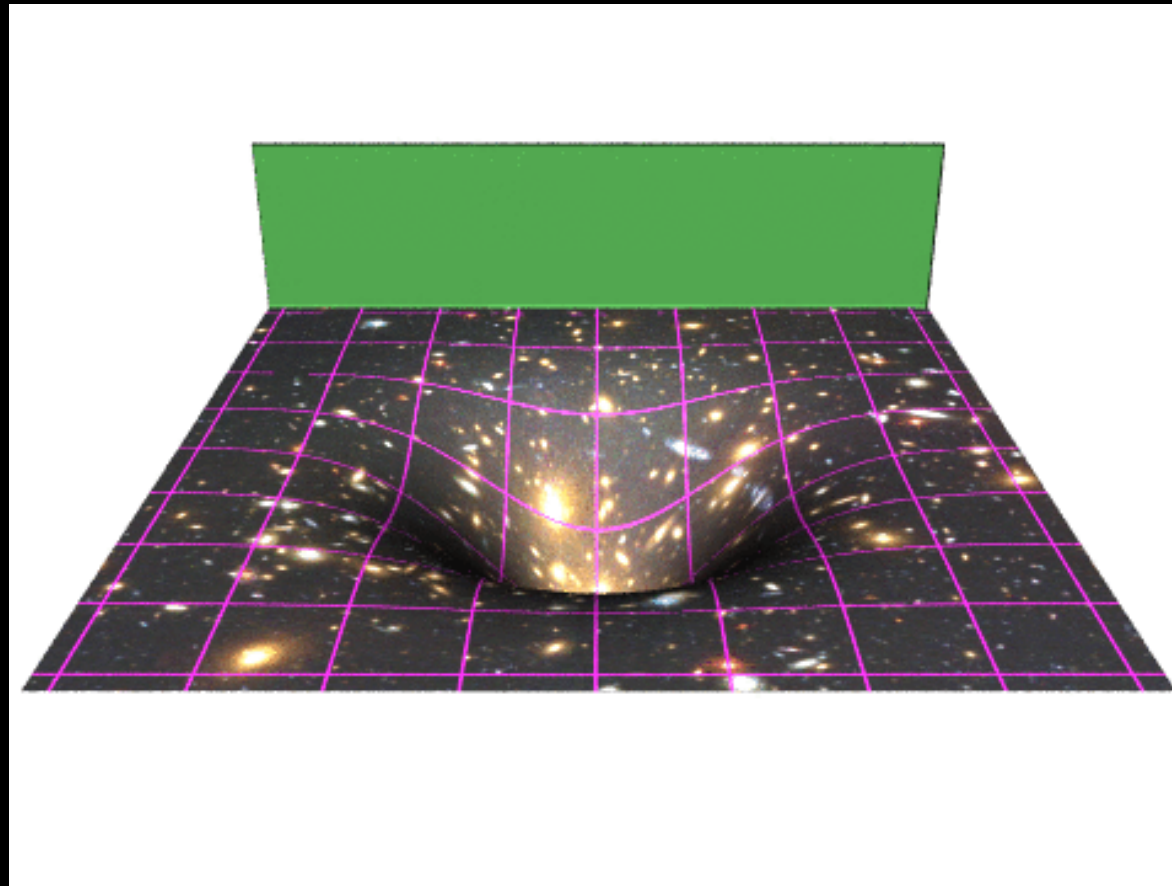
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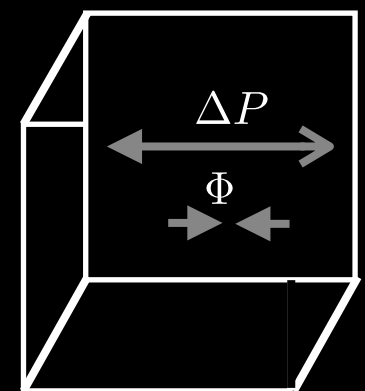
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ULAs and the CMB: high mass and early ISW

Higher mass (DM-like) case: high- l ISW



Radiation pressure causes potential decay

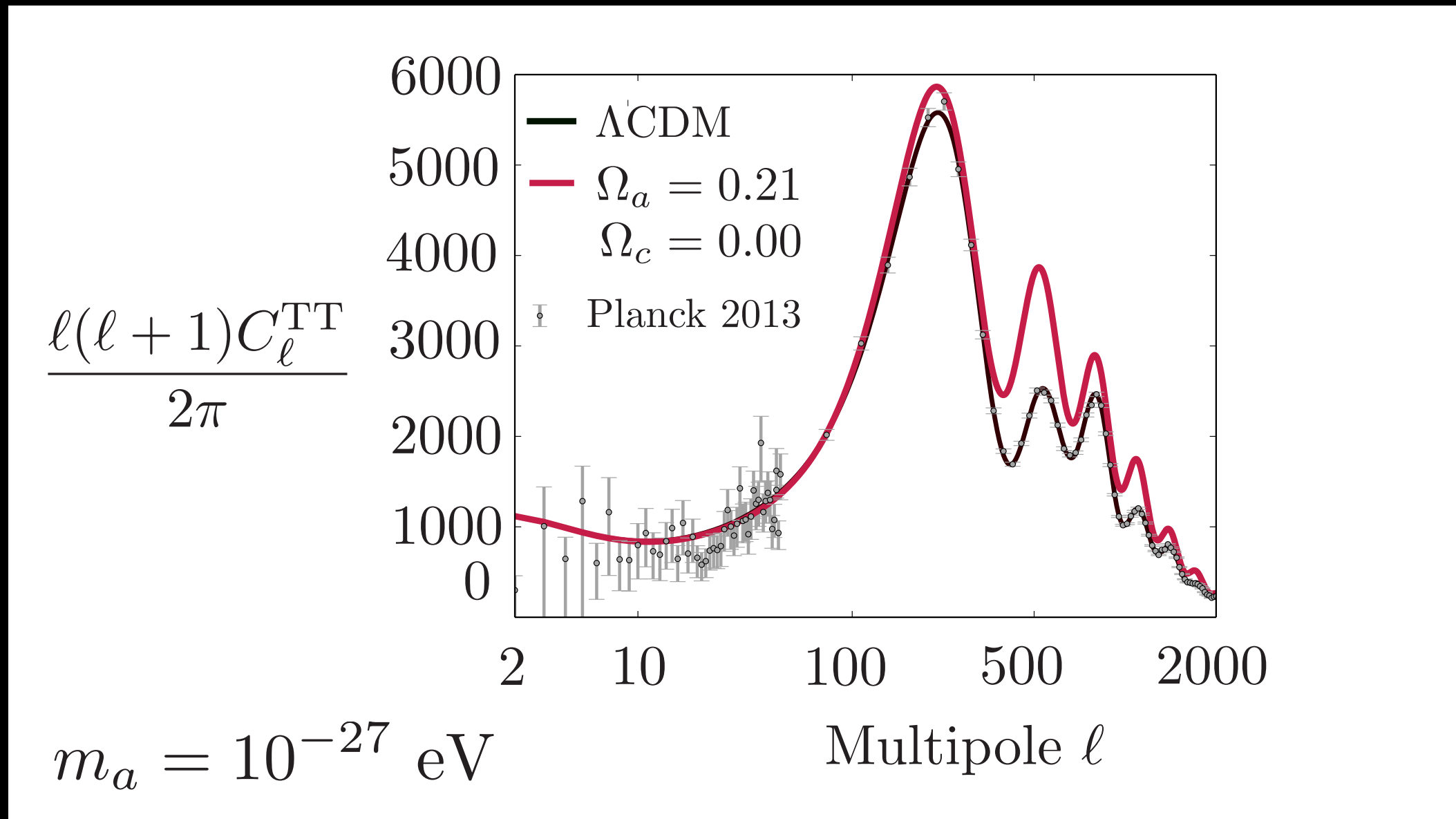


$$\Phi \propto \frac{1}{k^2} \left\{ \frac{\Omega_m \delta_m \left(1 - \frac{\Omega_a}{\Omega_m} \right)}{a^3} + \frac{\delta_R \Omega_R}{a^4} \right\}$$

$$\Delta P \Delta A > \rho \delta V \nabla \Phi$$

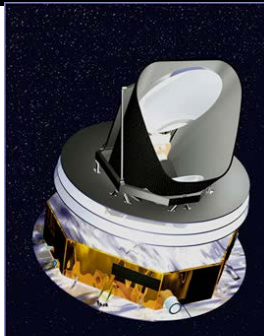
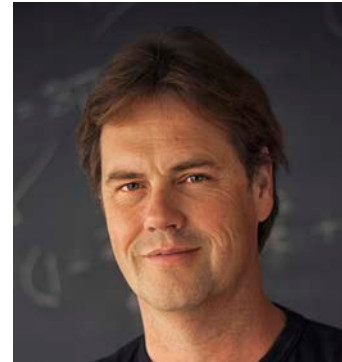
ULAs and the CMB: high mass and early ISW

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CONSTRAINTS

Comparison with data



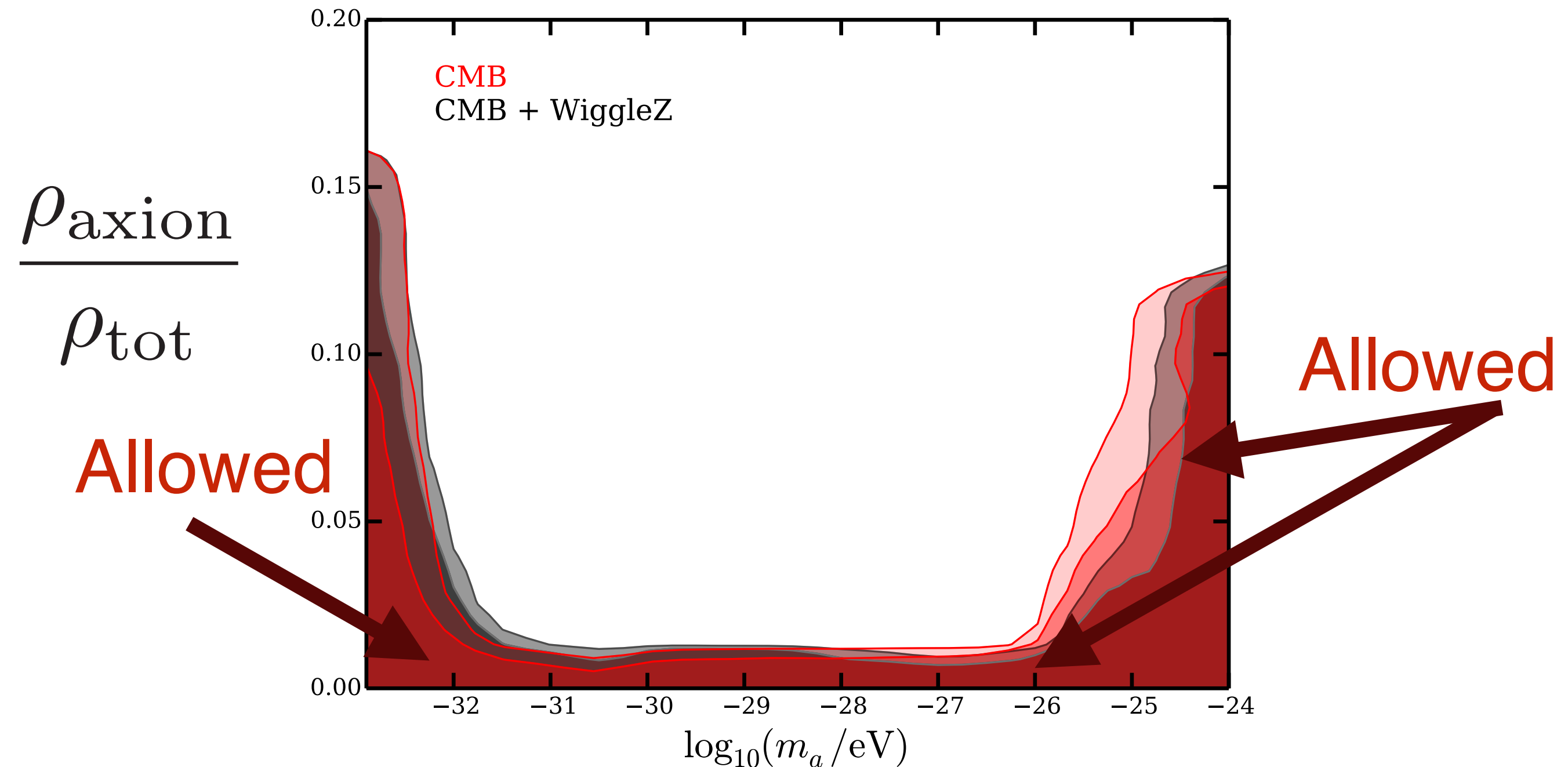
R.Hlozek, DG, D.J. E. Marsh, P.Ferreira

arXiv:1410.2896, Phys. Rev. D 91, 103512 (2015)

arXiv:1403.4216, Phys. Rev. Lett. 113, 011801 (2014)

arXiv:1303.3008, Phys. Rev. D 87, 121701(R) (2013)

CONSTRAINTS

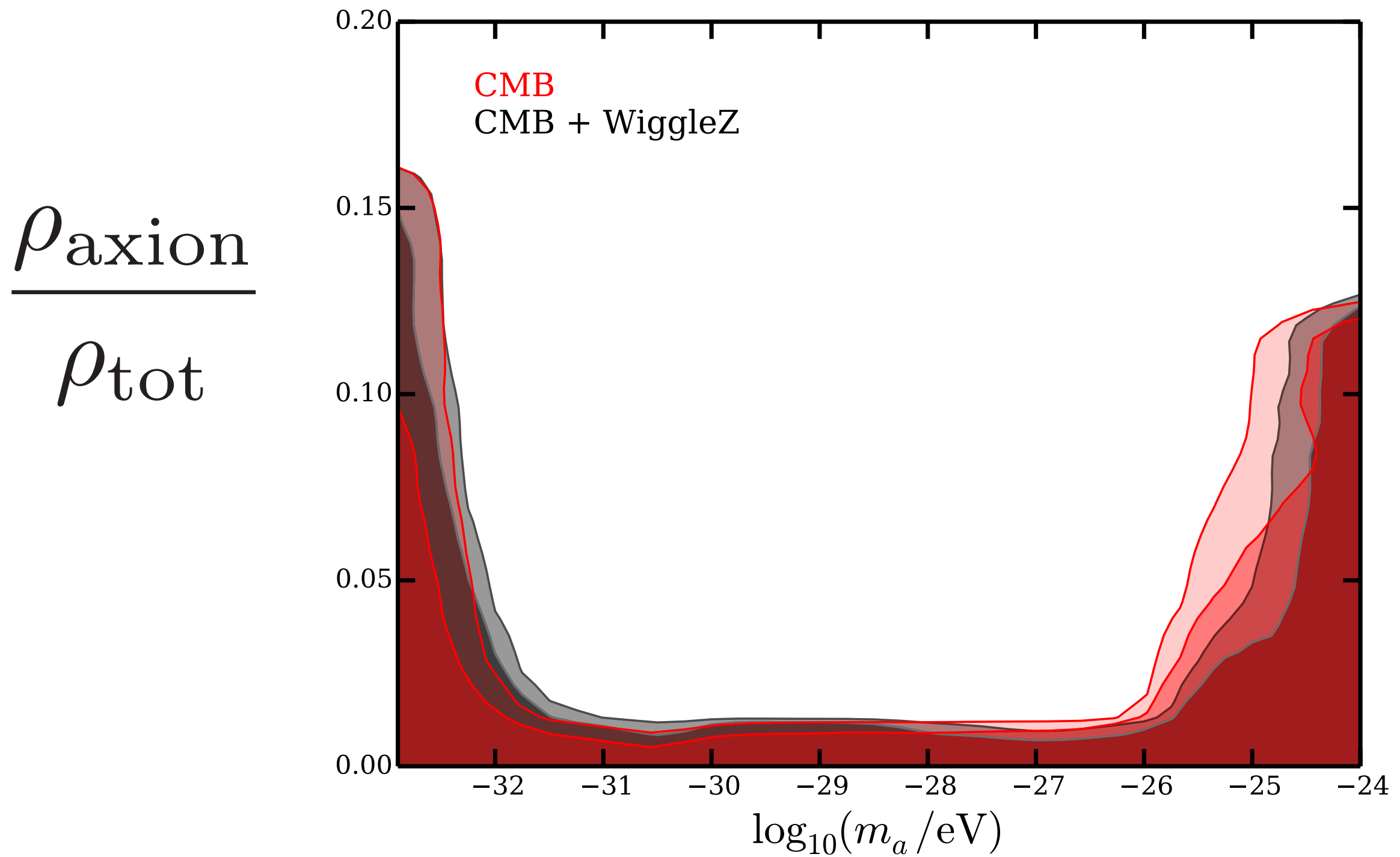


✳ Tight constraints over 7 orders of magnitude in mass:

Thanks to **AXICAMB** and **Planck**

✳ ULAs are viable DM/DE candidates in linear theory outside ``belly”

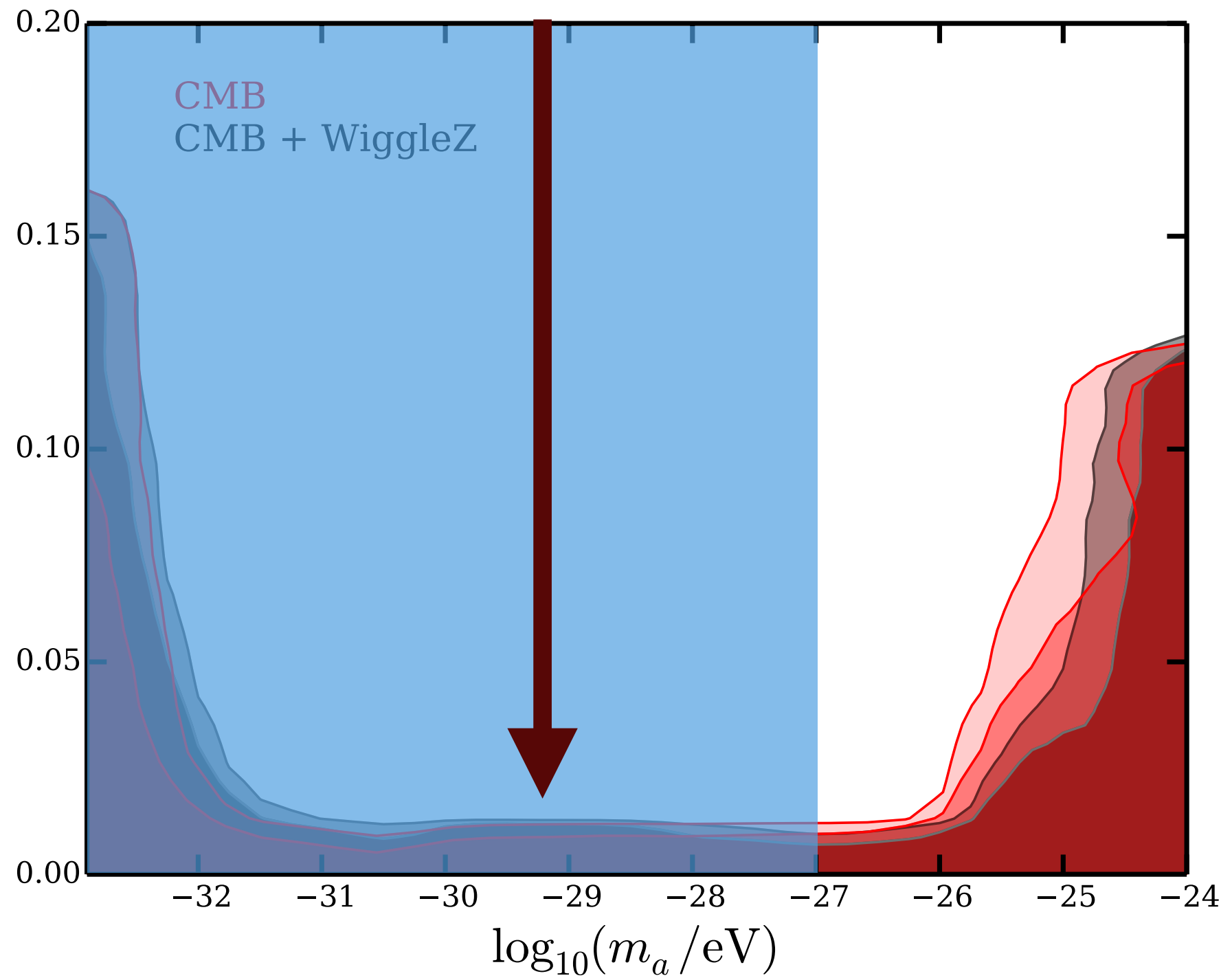
PHYSICS BEHIND THE CONSTRAINTS



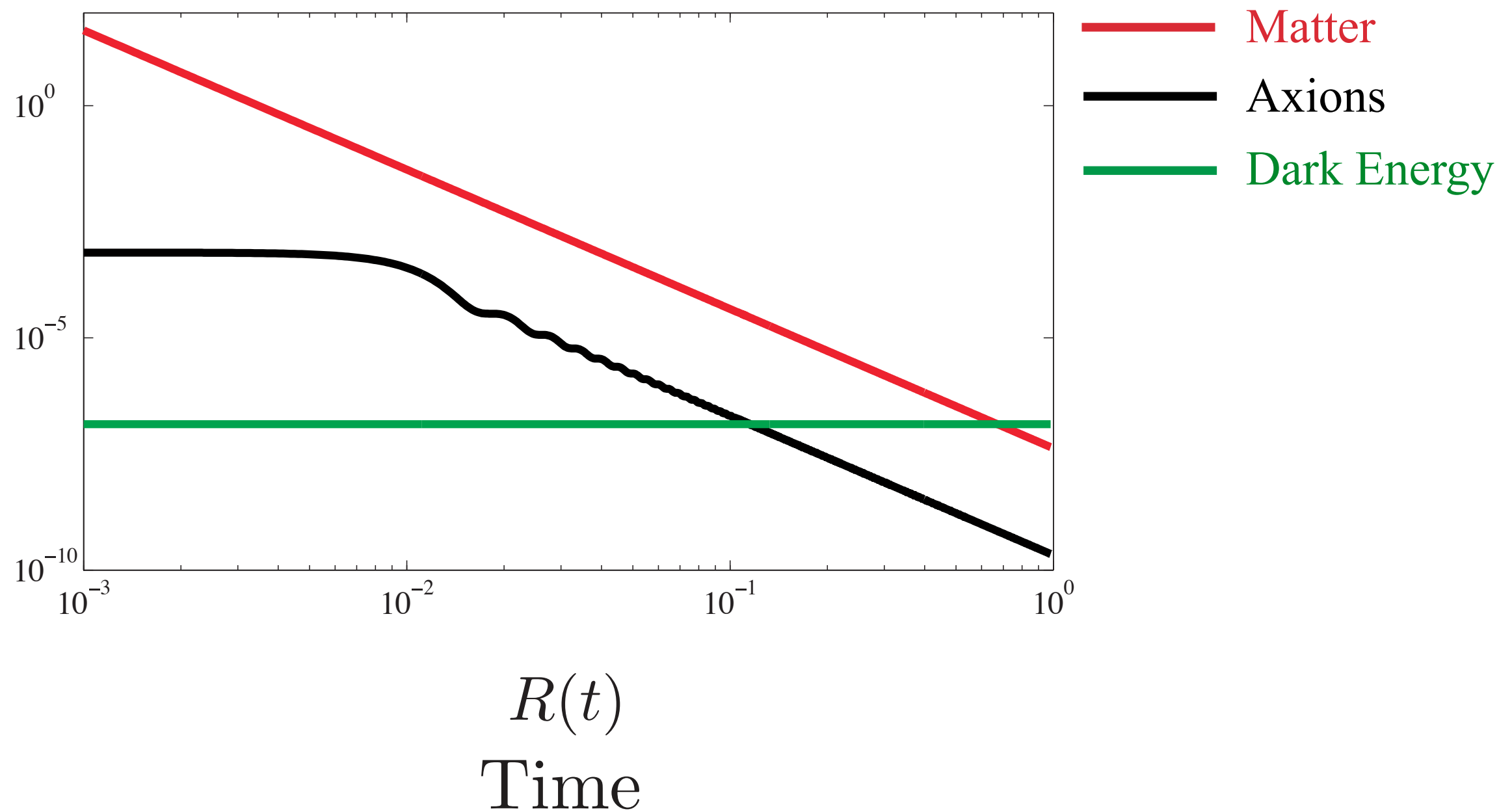
PHYSICS BEHIND THE CONSTRAINTS

Dark-energy type axions

$$\frac{\rho_{\text{axion}}}{\rho_{\text{tot}}}$$



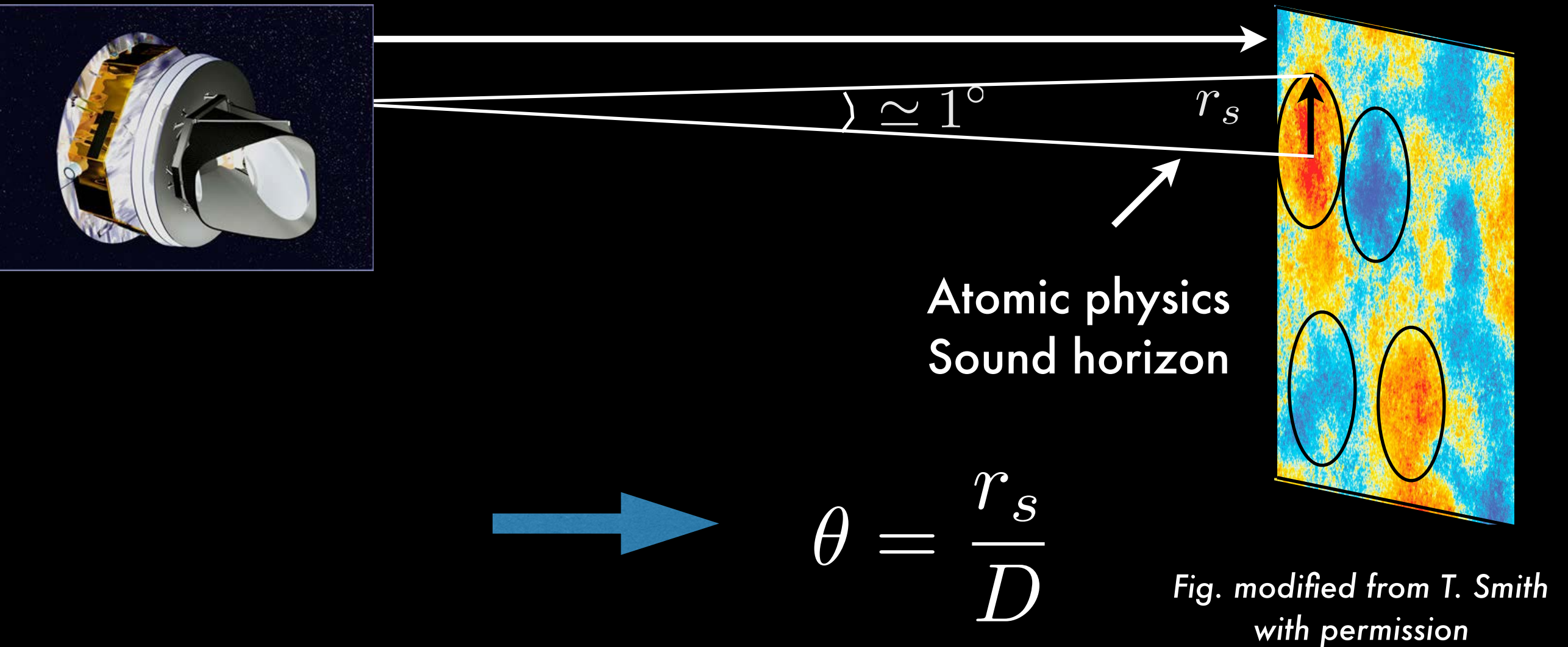
✴ Axion energy density behaves unusually



Faster early expansion brings CMB emission surface closer

CMB CONSTRAINTS AT LOW MASSES AND THE ANGULAR SOUND HORIZON

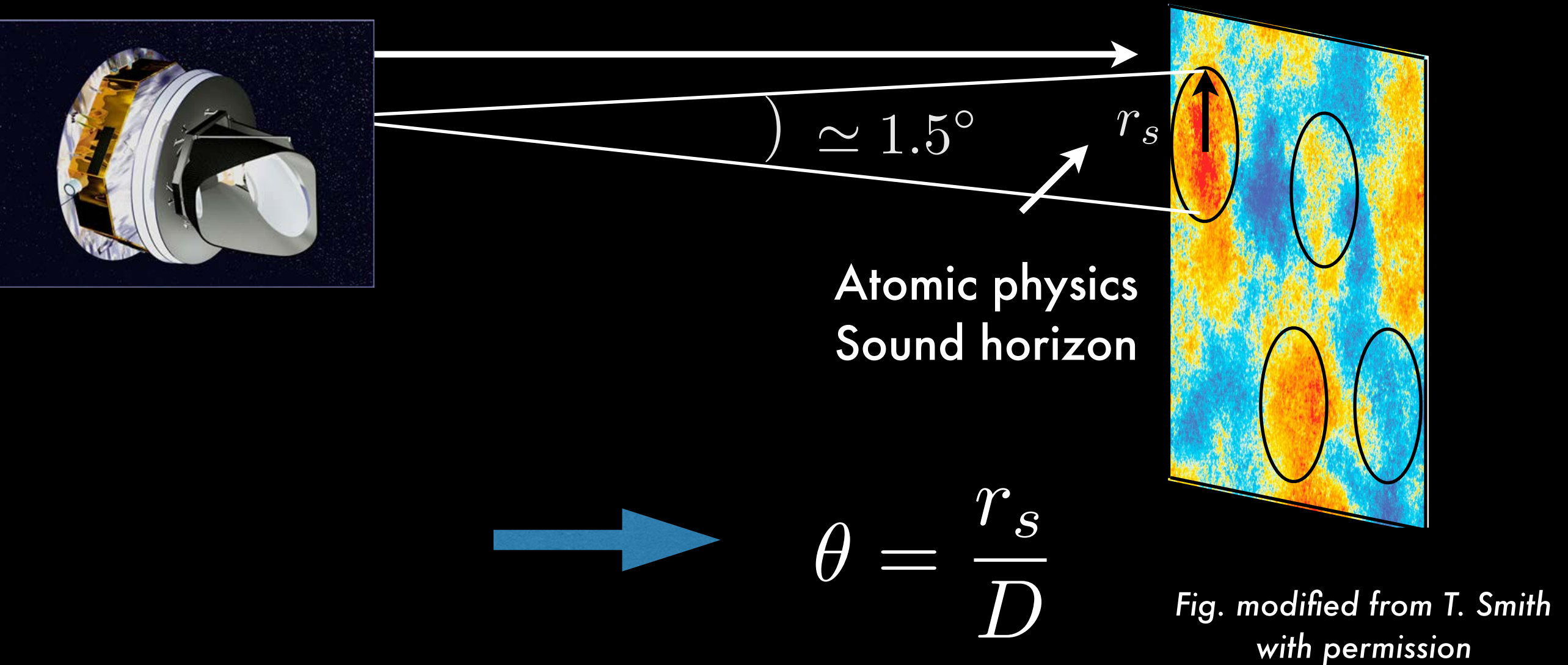
D (sensitive to any energy source)



Faster early expansion brings CMB emission surface closer

CMB CONSTRAINTS AT LOW MASSES AND THE ANGULAR SOUND HORIZON

D (sensitive to any energy source)



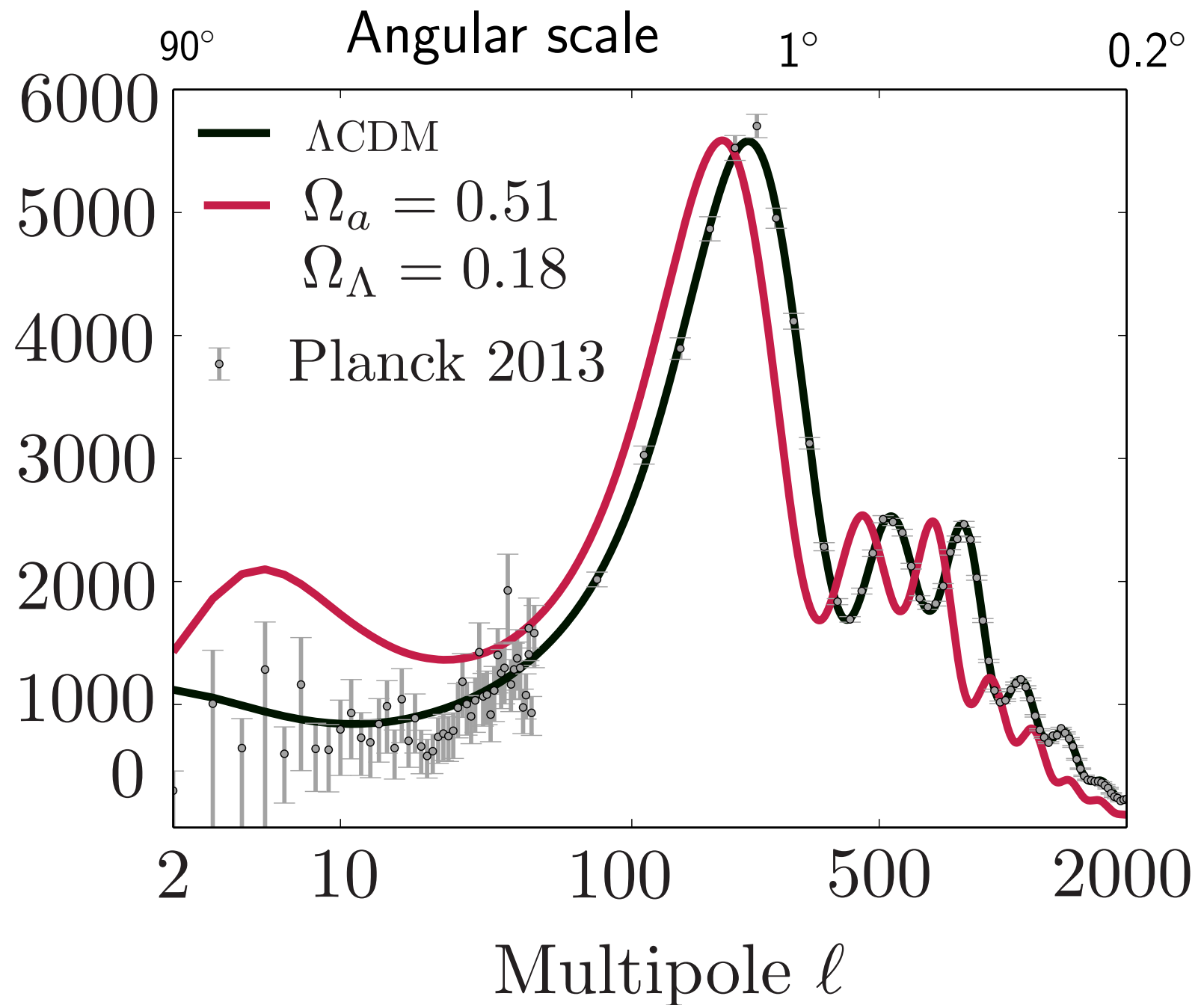
Faster early expansion brings CMB emission surface closer

CMB CONSTRAINTS AT LOW MASSES

$$m_a = 10^{-32} \text{ eV}$$

Temperature Variance

$$\frac{\mu\text{K}^2}{2\pi} \ell(\ell+1)C_\ell^{\text{TT}}$$



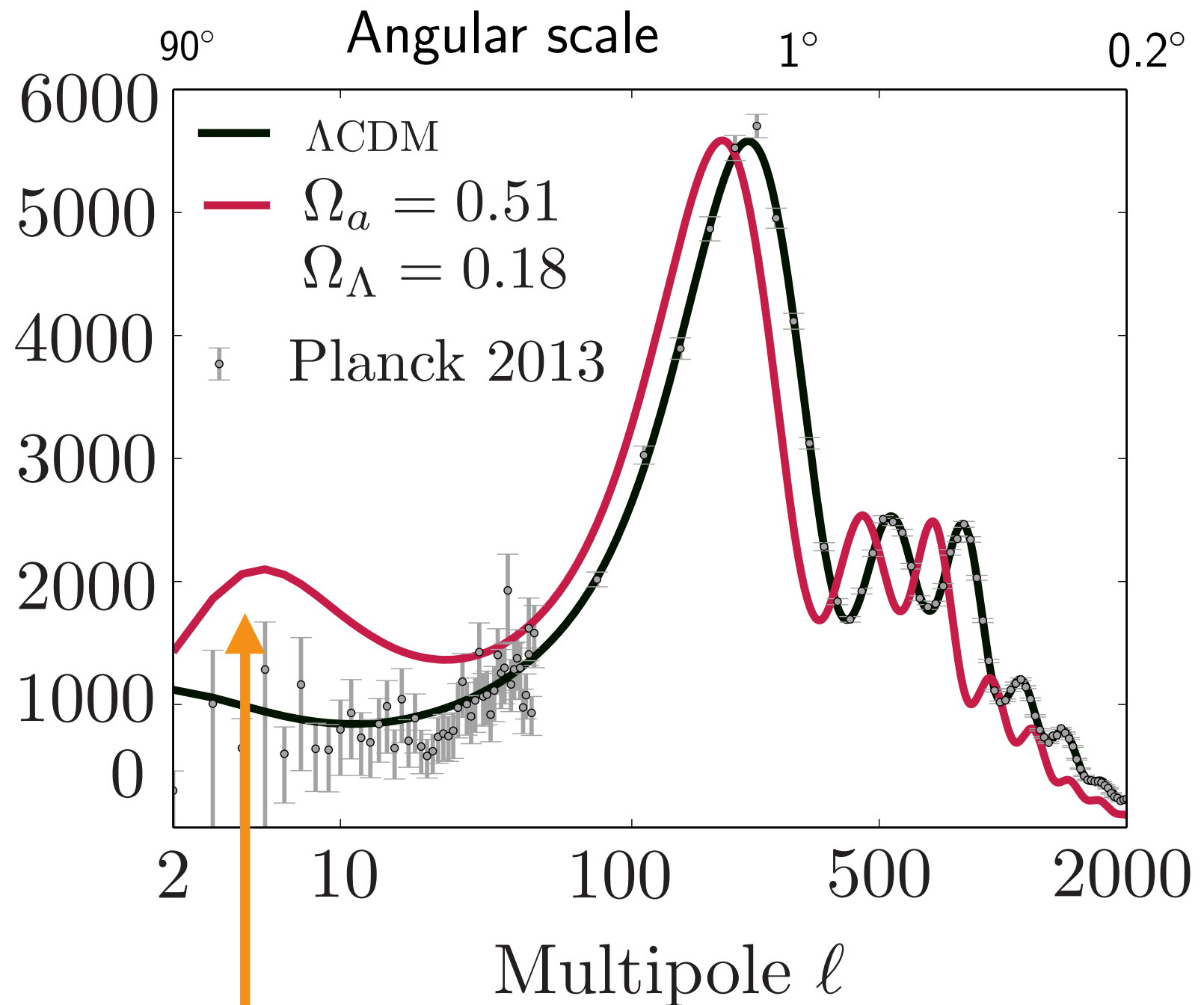
← Acoustic features shift!

CMB CONSTRAINTS AT LOW MASSES

$$m_a = 10^{-32} \text{ eV}$$

Temperature Variance

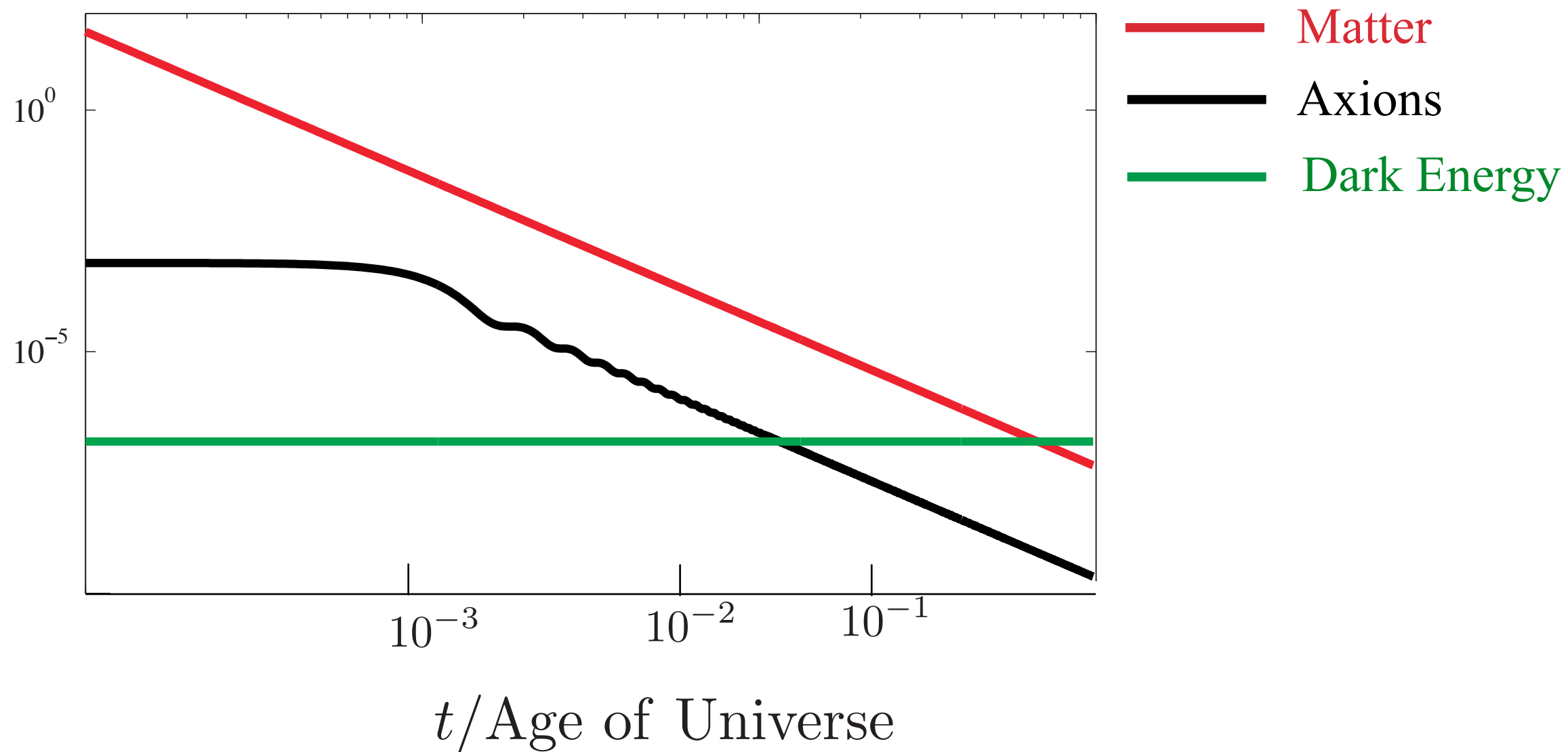
$$\frac{\mu\text{K}^2}{2\pi} \frac{\ell(\ell+1)C_\ell^{\text{TT}}}{\ell(\ell+1)}$$



What about this bump?

AXIONS IMPRINT ON COSMOLOGY

✴ Axion energy density behaves unusually

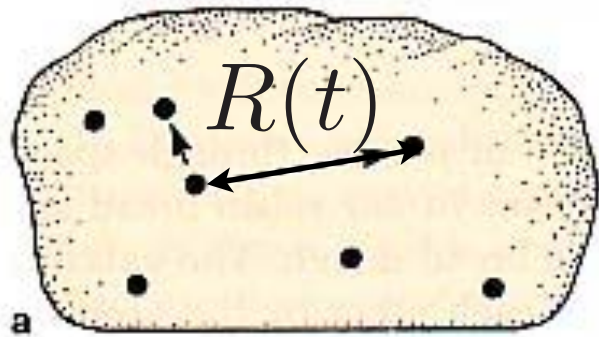


Time

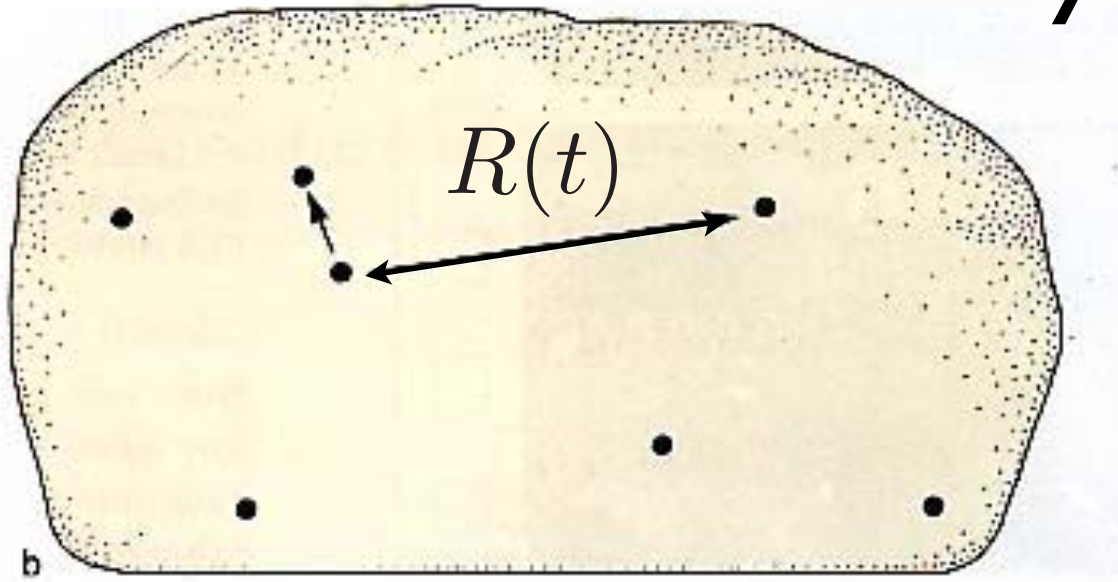
AXIONS IMPRINT ON COSMOLOGY

✴ Axion alters cosmic expansion history

Past

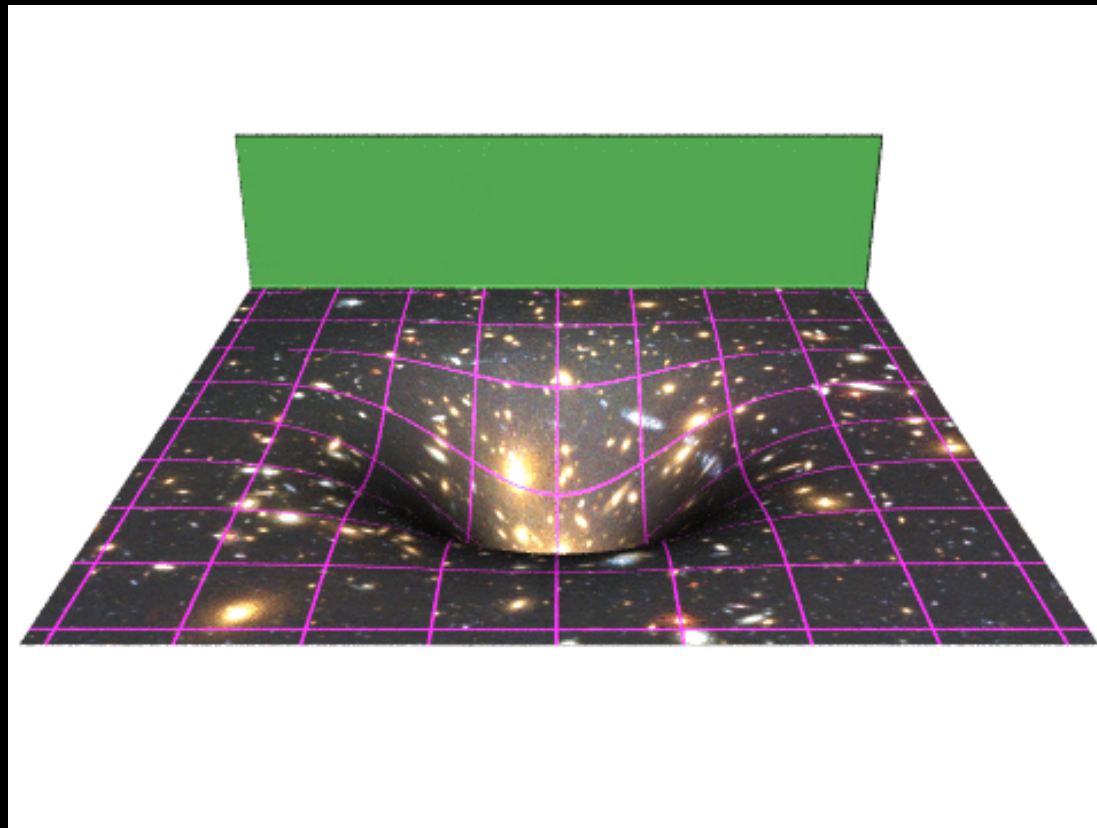


Today



$$\left[\frac{\dot{R}(t)}{R(t)} \right]^2 = \frac{8\pi G \rho}{3} \quad \text{Energy content (including axions) determines expansion history}$$

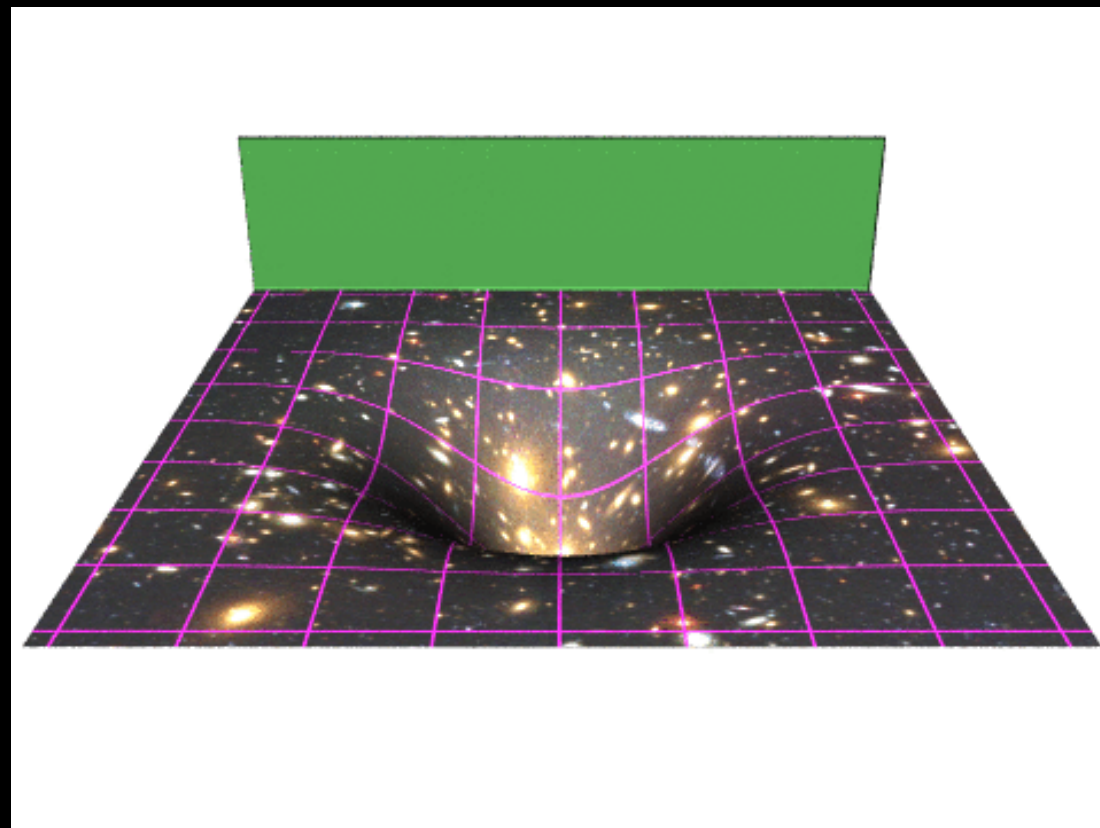
*Low mass (DE-like) case:
late Integrated Sachs-Wolfe Effect*



CMB temperature anisotropies from potential decay

$$\Delta T_{\text{ISW}} = -2 \int_0^{\eta_{\text{dec}}} d\eta \dot{\Phi}(\eta, \hat{n}\eta)$$

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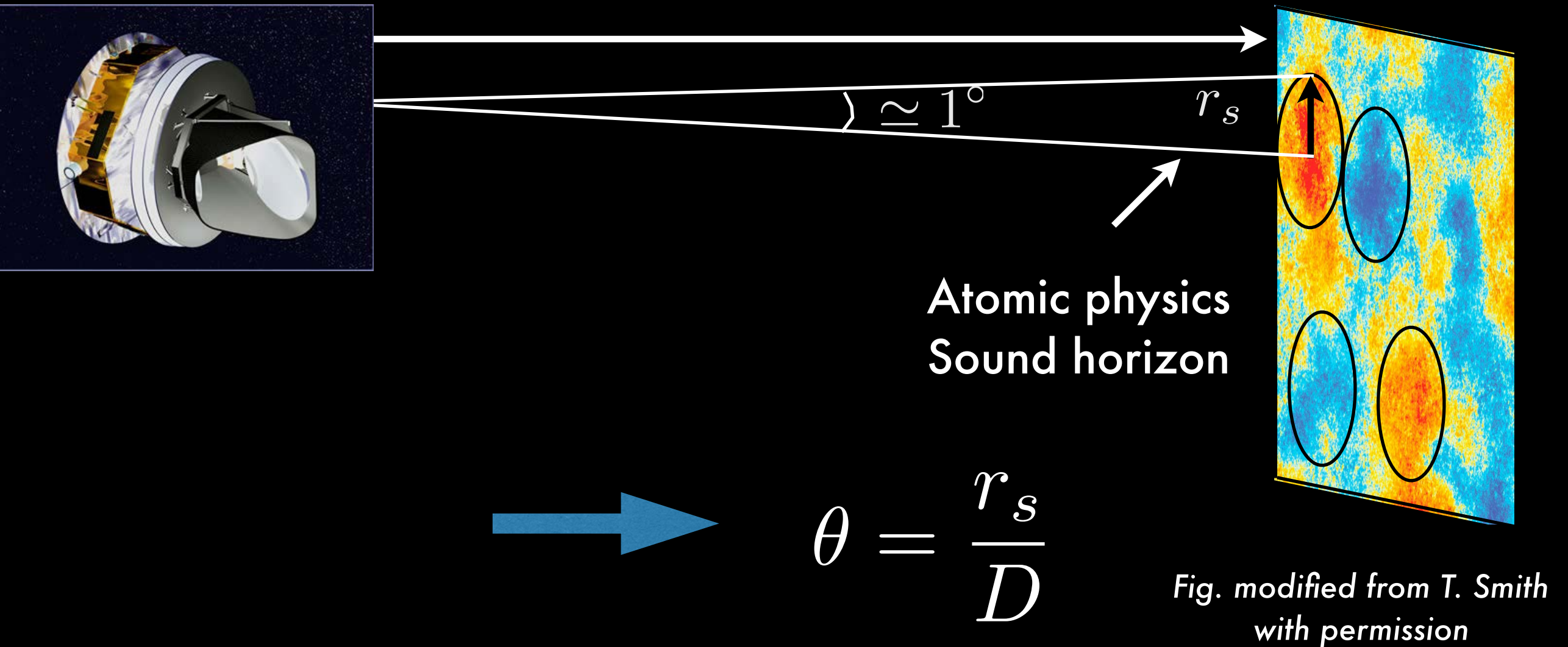


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ULAS AS DARK ENERGY AND THE ANGULAR SOUND HORIZON

D (sensitive to any energy source)



Faster early expansion brings LSS closer

ULAS AS DARK ENERGY AND THE ANGULAR SOUND HORIZON

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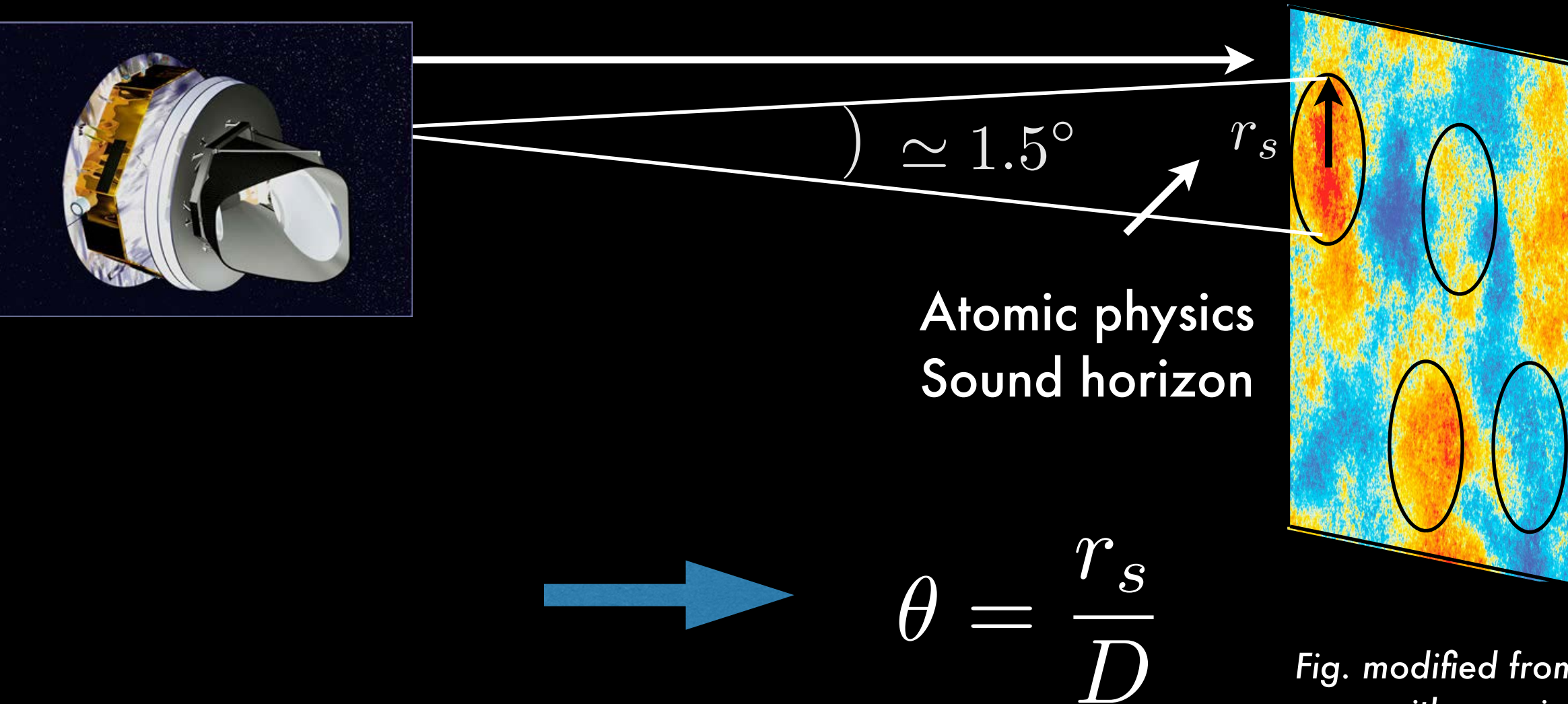
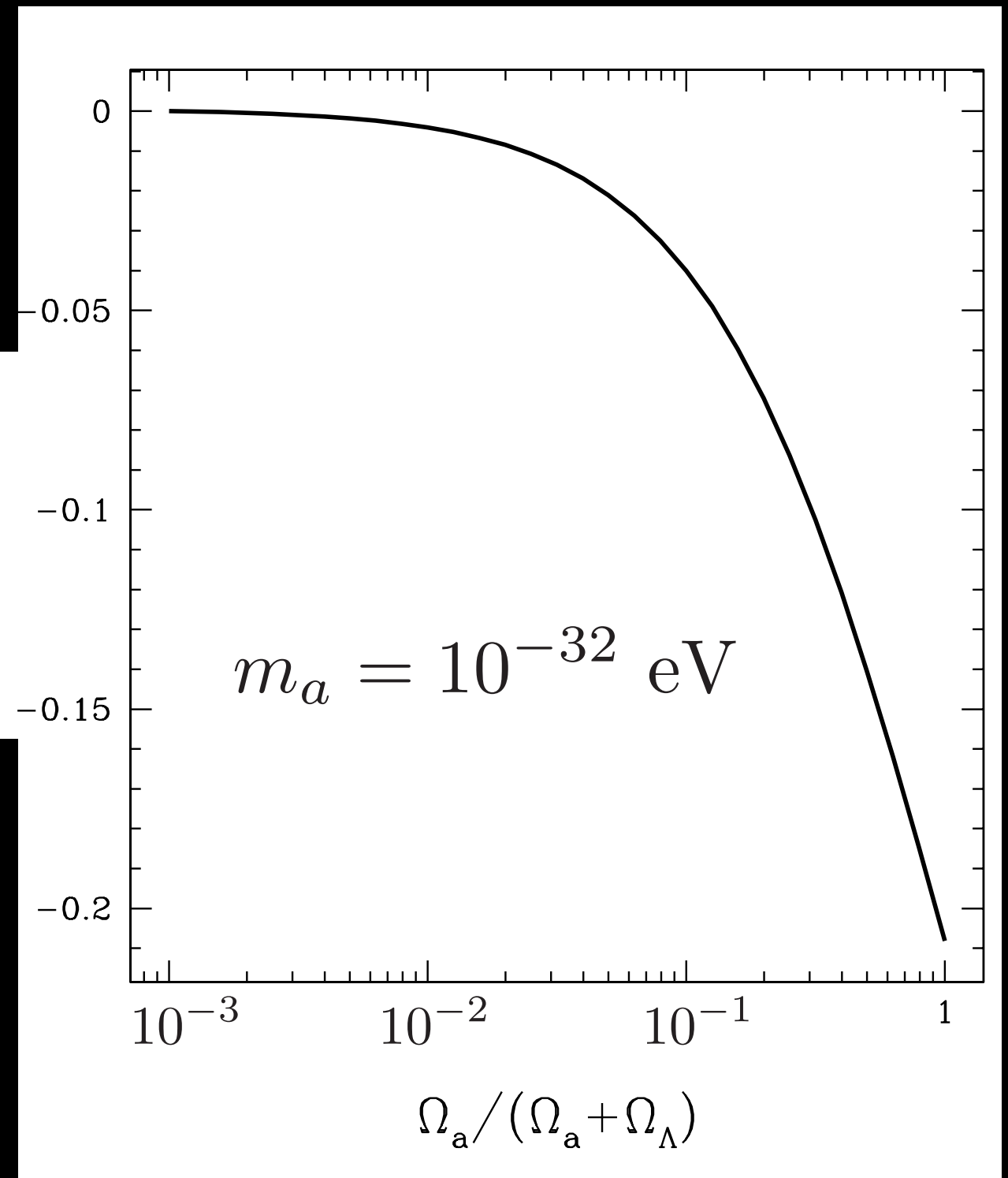


Fig. modified from T. Smith
with permission

Faster early expansion brings LSS closer

ULAS AS DARK ENERGY AND THE ANGULAR SOUND HORIZON

$$\frac{D(z_{\text{decoupling}}) - D^{\text{axion}}(z_{\text{decoupling}}^{\text{axion}})}{D(z_{\text{decoupling}})}$$

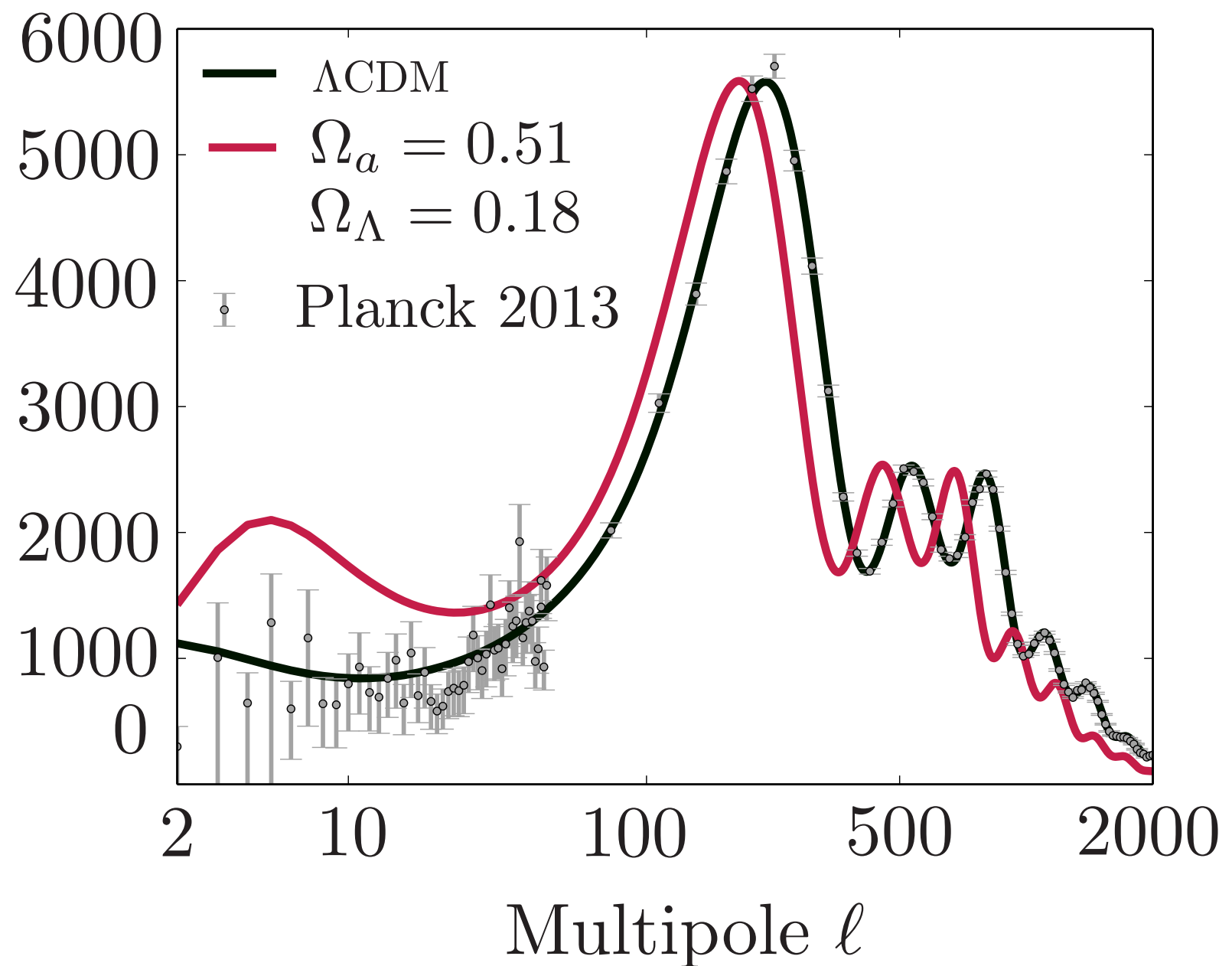


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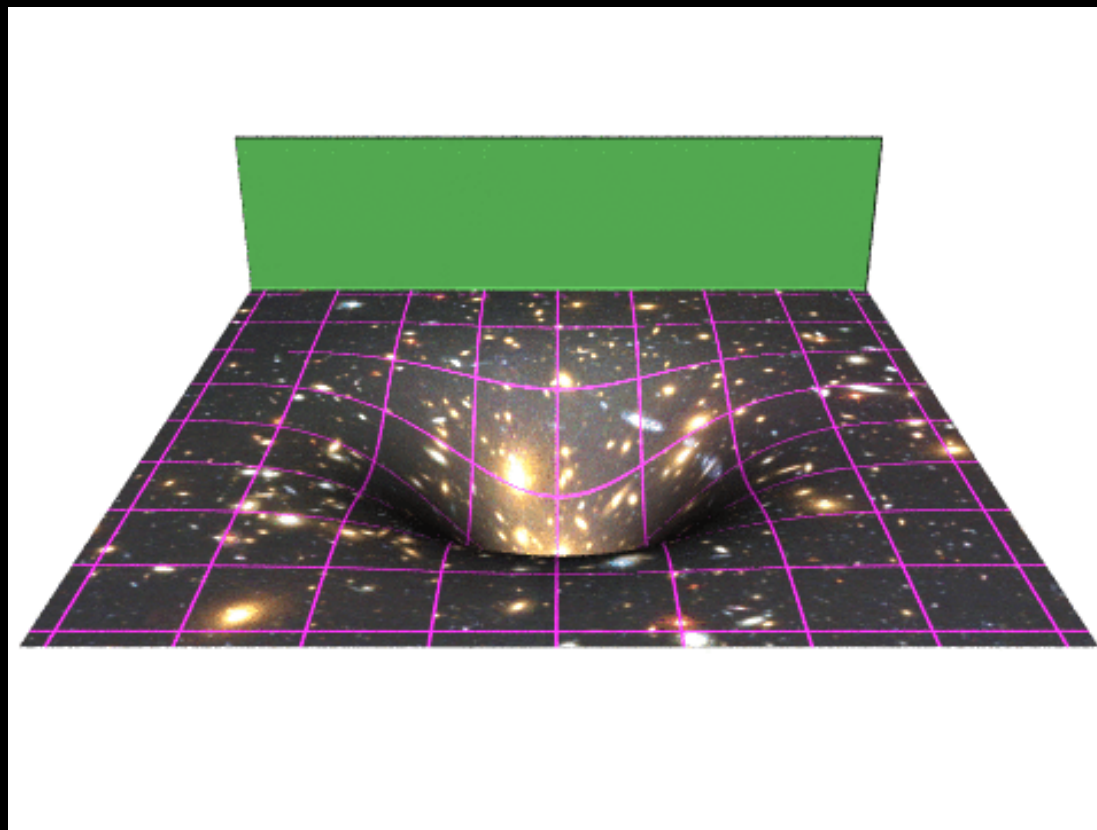
Temperature Variance

$$\frac{\mu\text{K}^2}{2\pi} \frac{\ell(\ell+1)C_\ell^{\text{TT}}}{\ell(\ell+1)C_\ell^{\text{TT}}}$$



ULAS AS DARK ENERGY AND PERTURBATIONS IN OTHER FLUIDS

*Low mass (DE-like) case:
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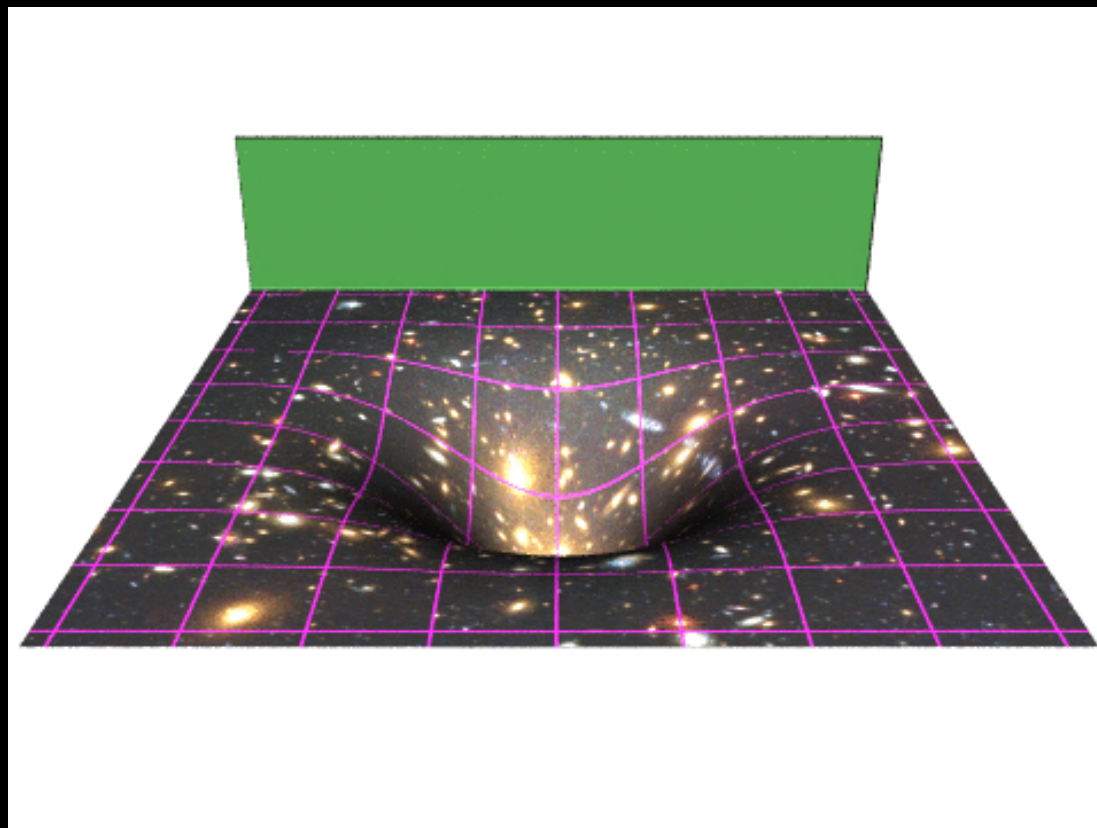


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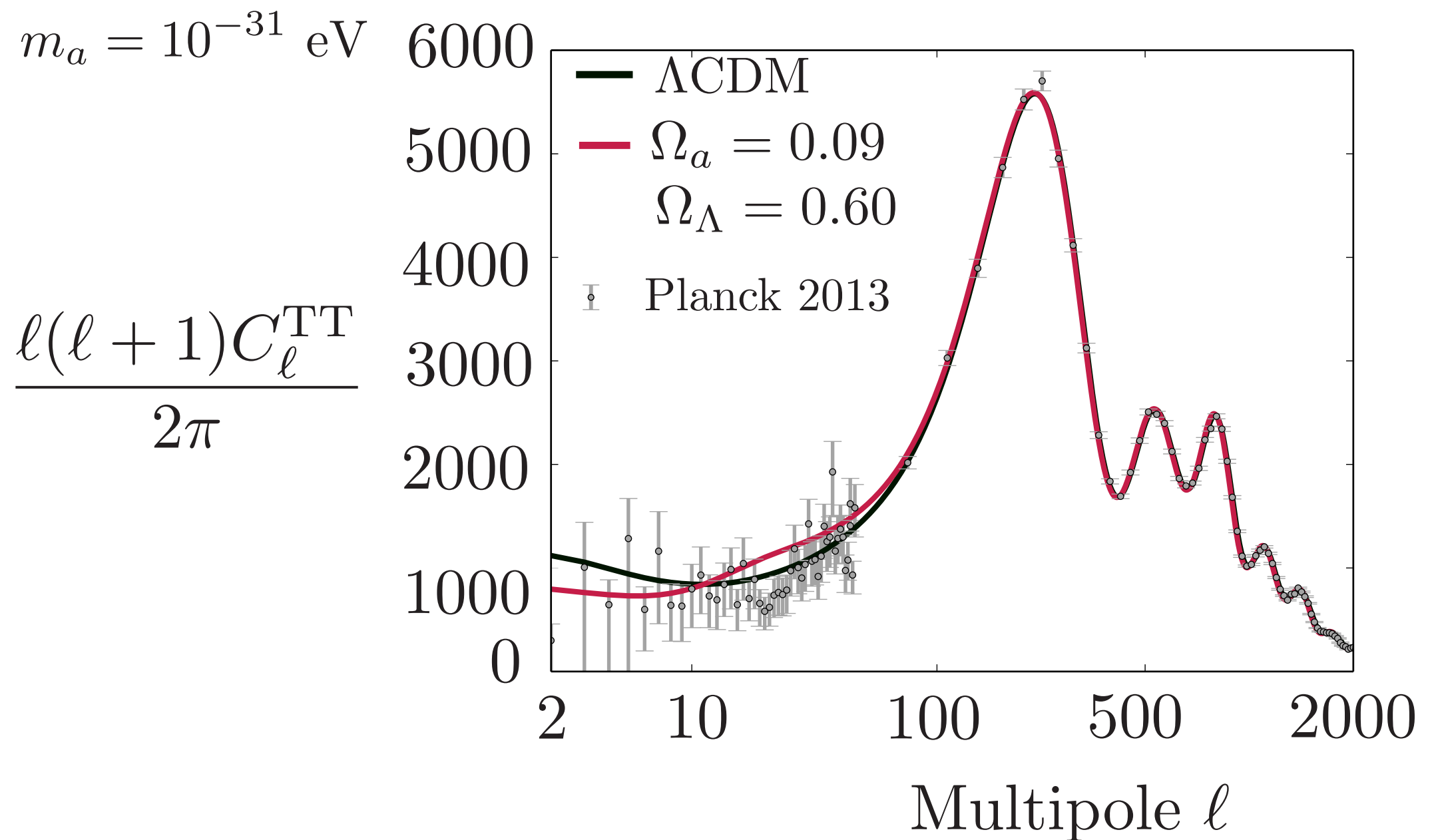


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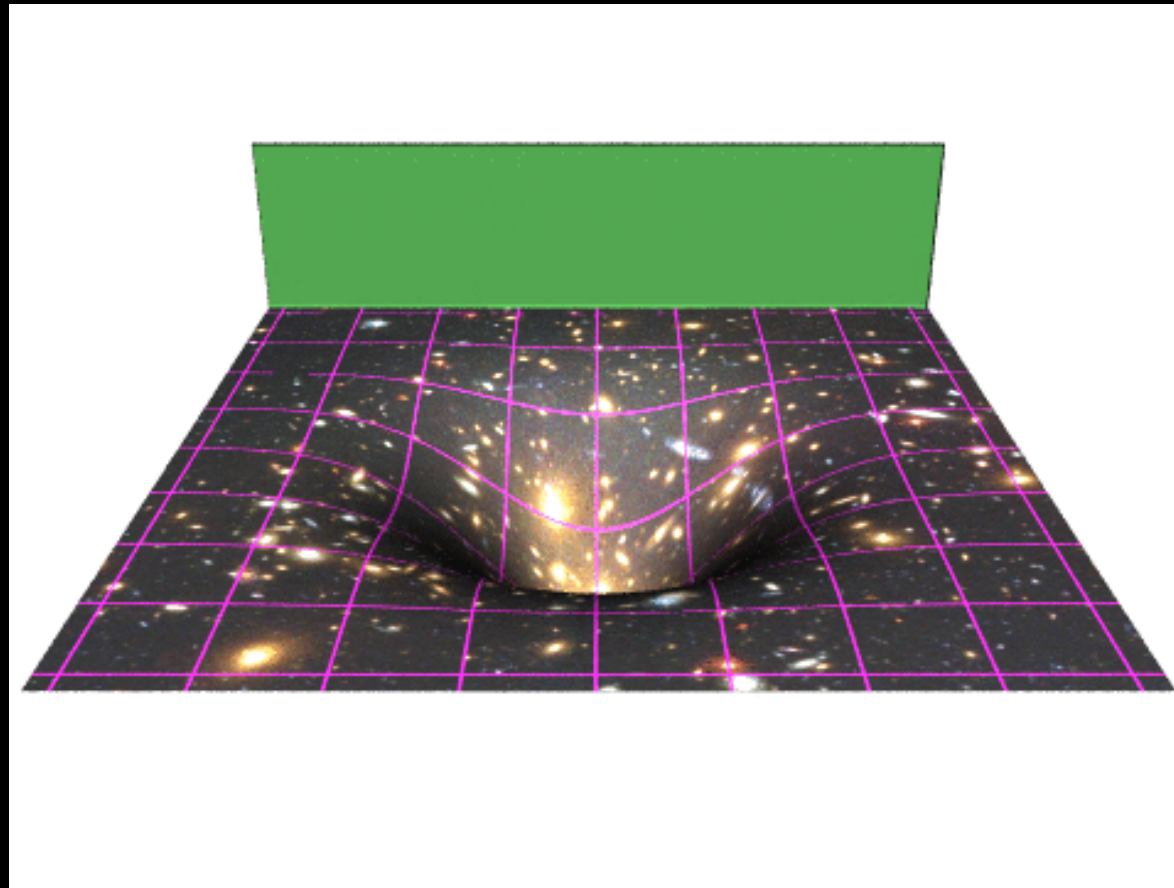
ULAS AS DARK ENERGY AND PERTURBATIONS IN OTHER FLUIDS

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ULAs and the CMB: high mass and early ISW

Higher mass (DM-like) case: high- l ISW

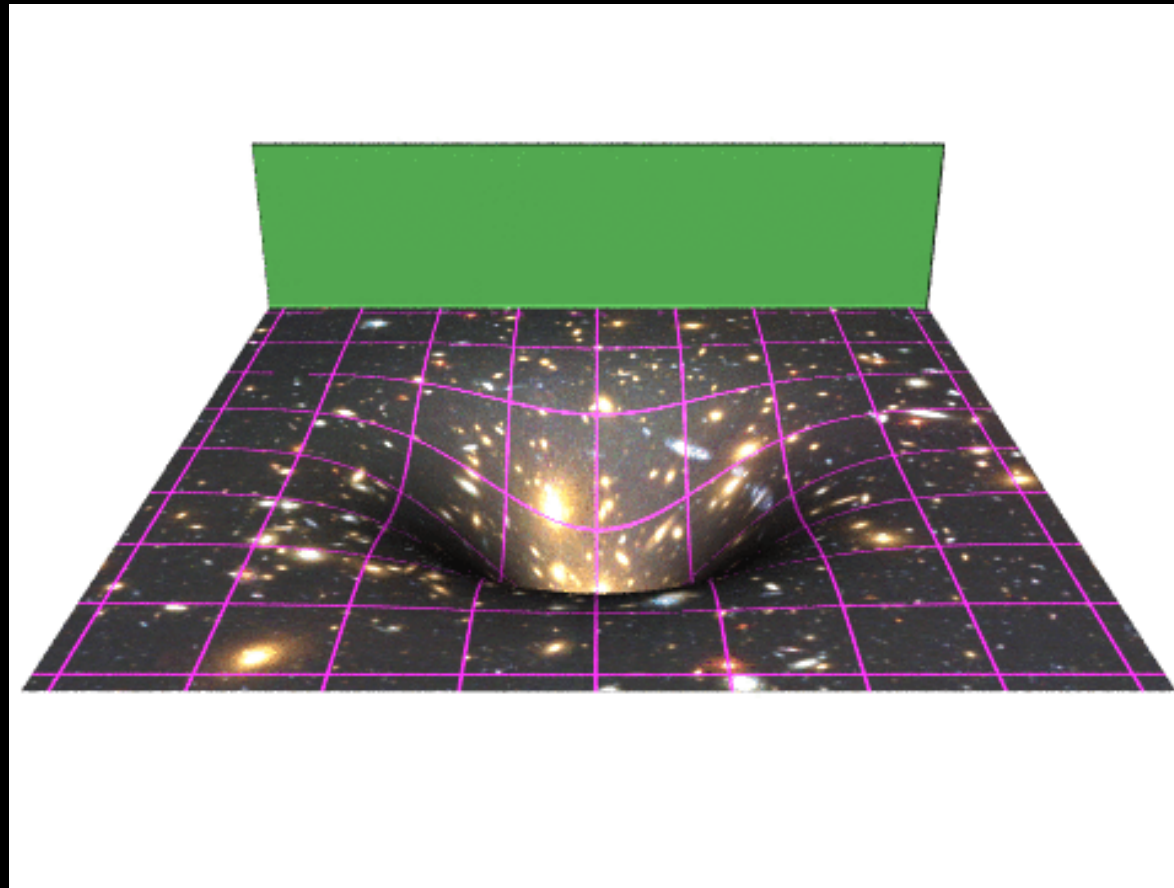


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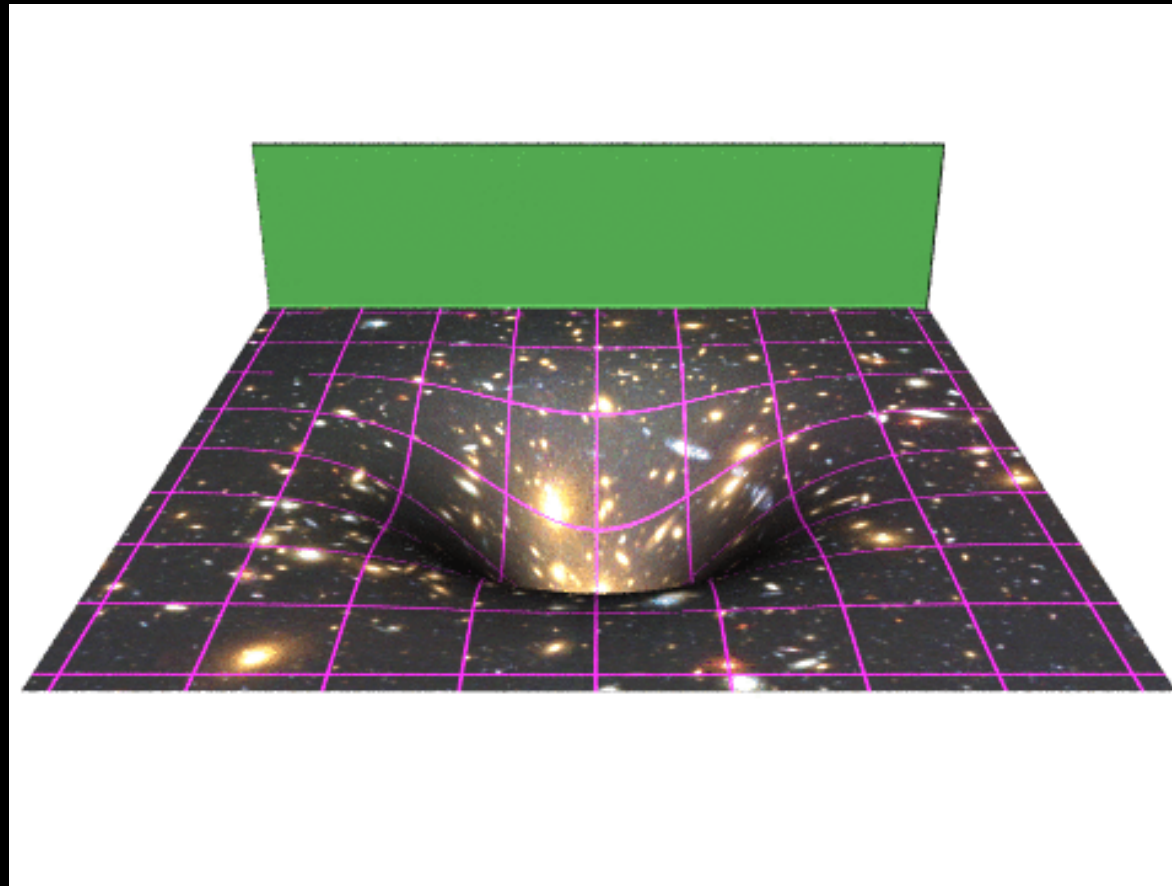


CMB temperature anisotropies from potential decay

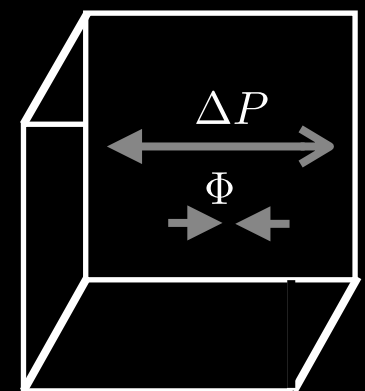
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ULAs and the CMB: high mass and early ISW

Higher mass (DM-like) case: high- l ISW



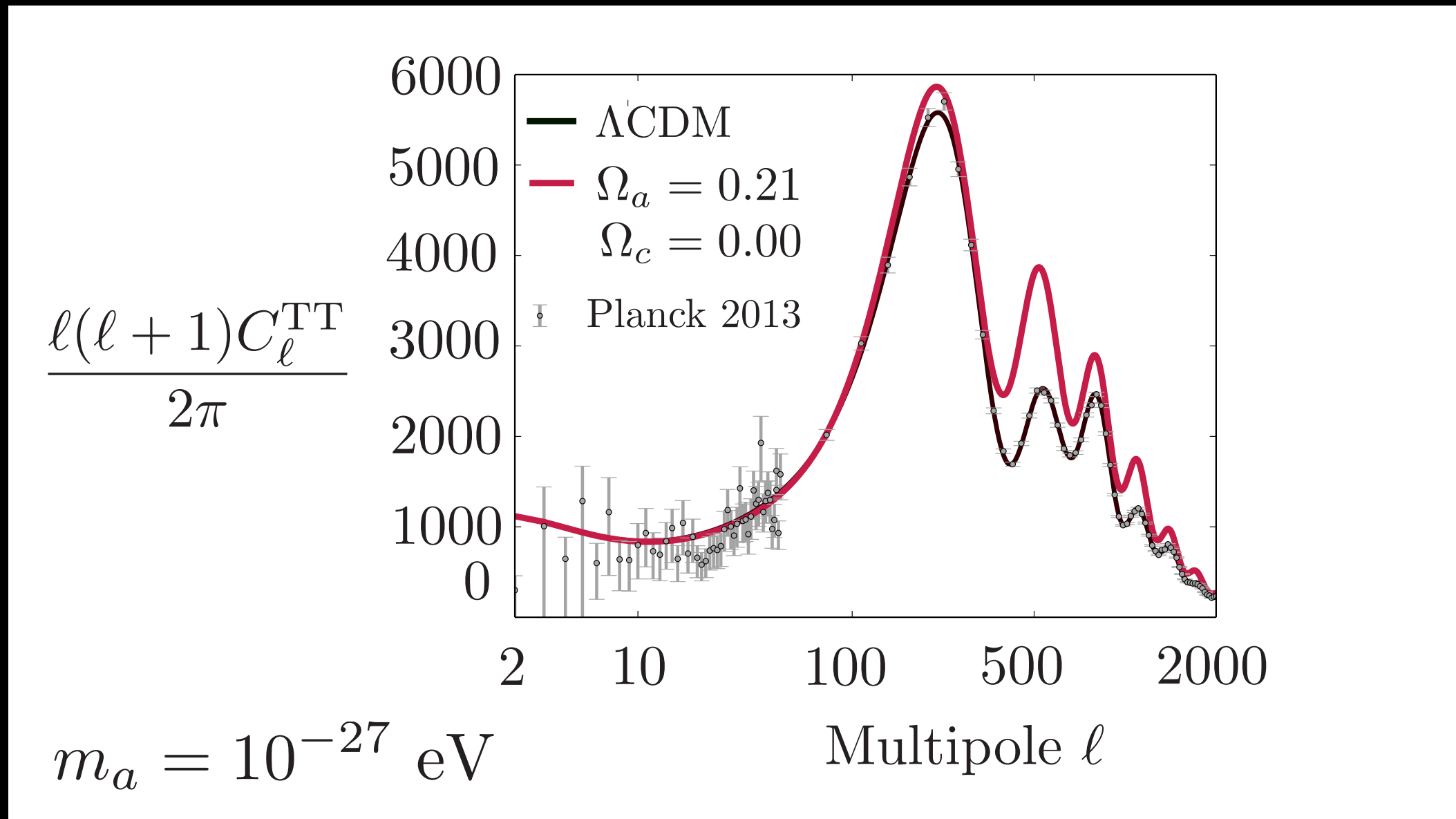
Radiation pressure causes potential decay



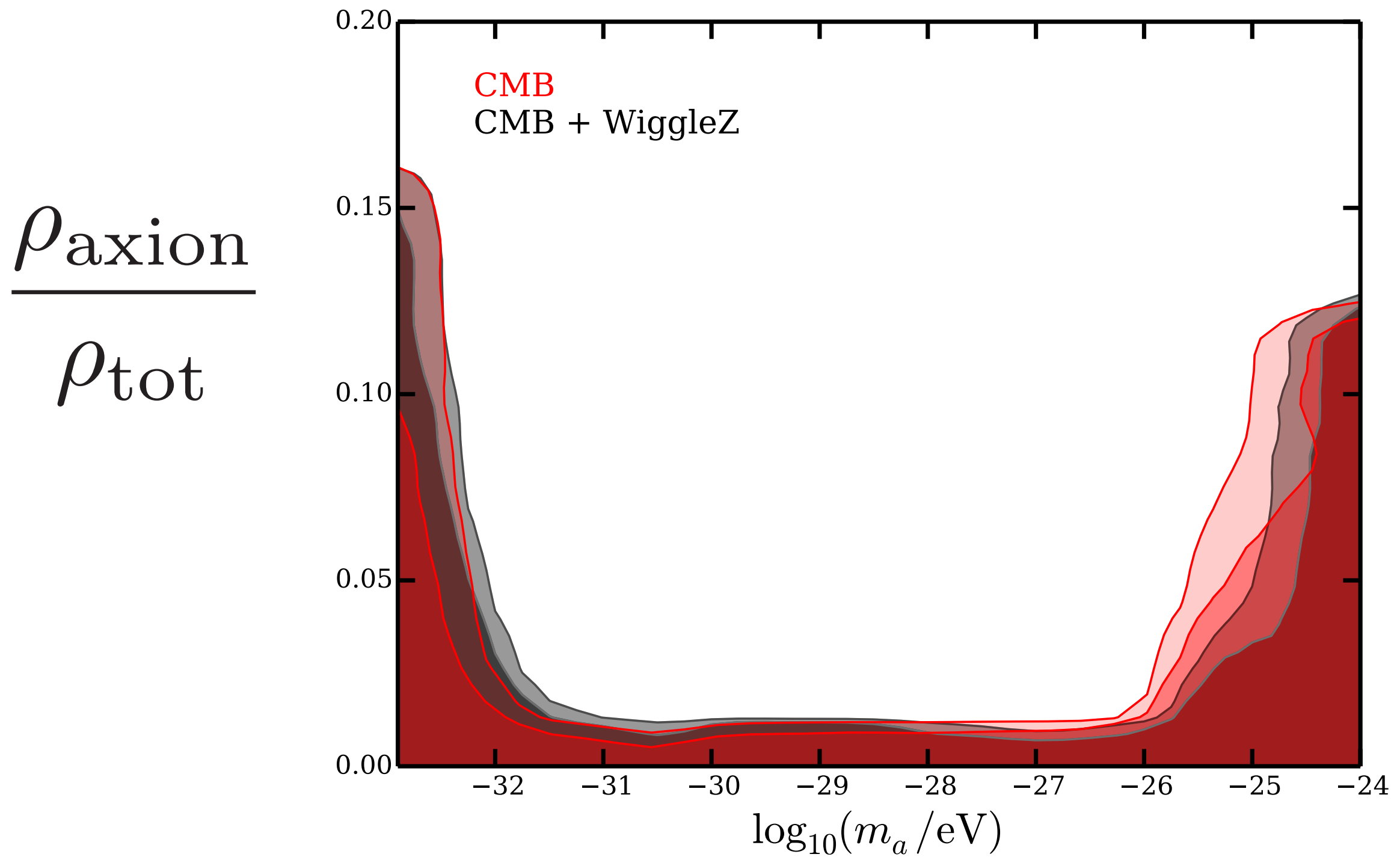
$$\Delta P \Delta A > \rho \delta V \nabla \Phi$$

ULAs and the CMB: high mass and early ISW

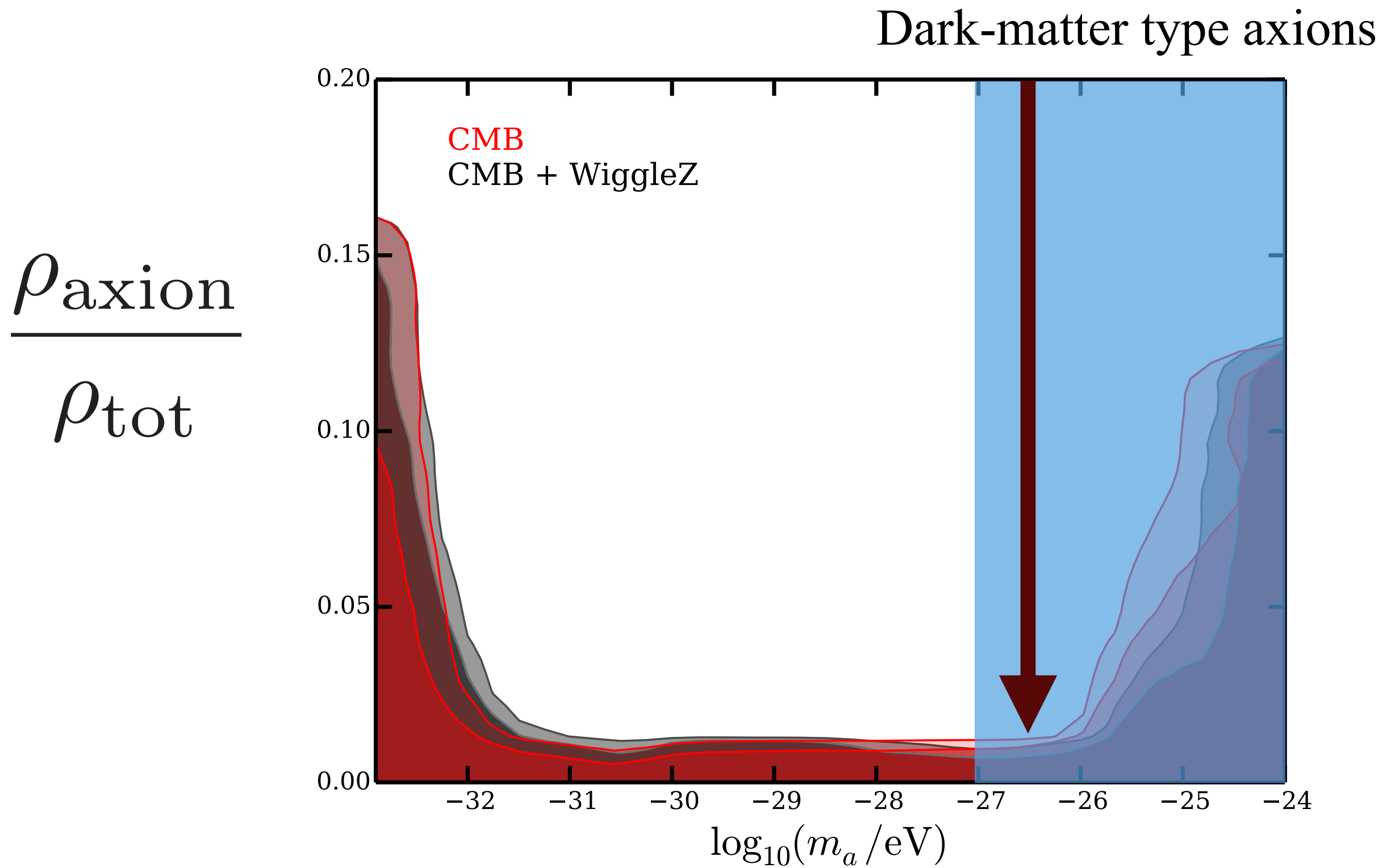
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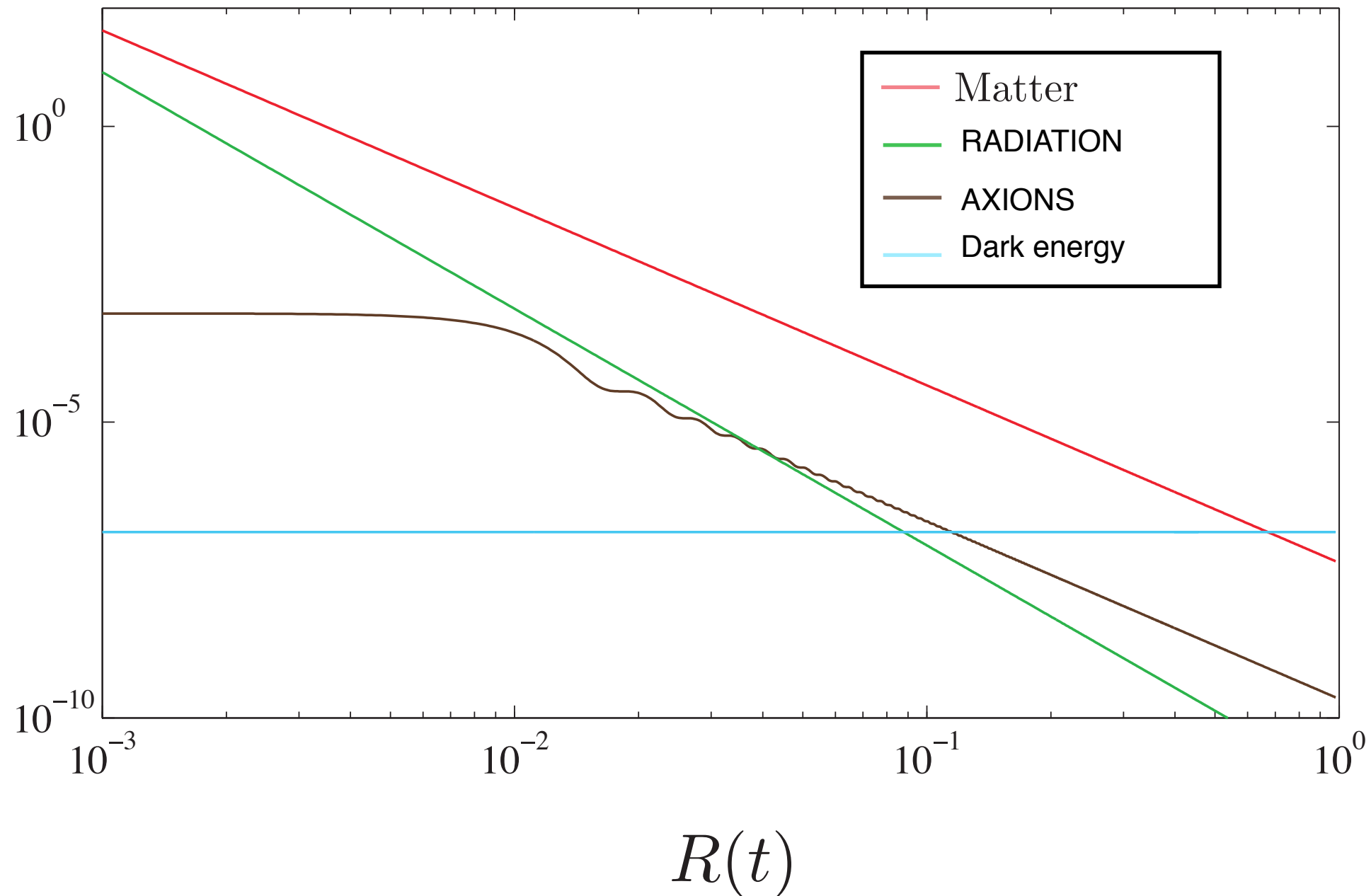
PHYSICS BEHIND THE CONSTRAINTS



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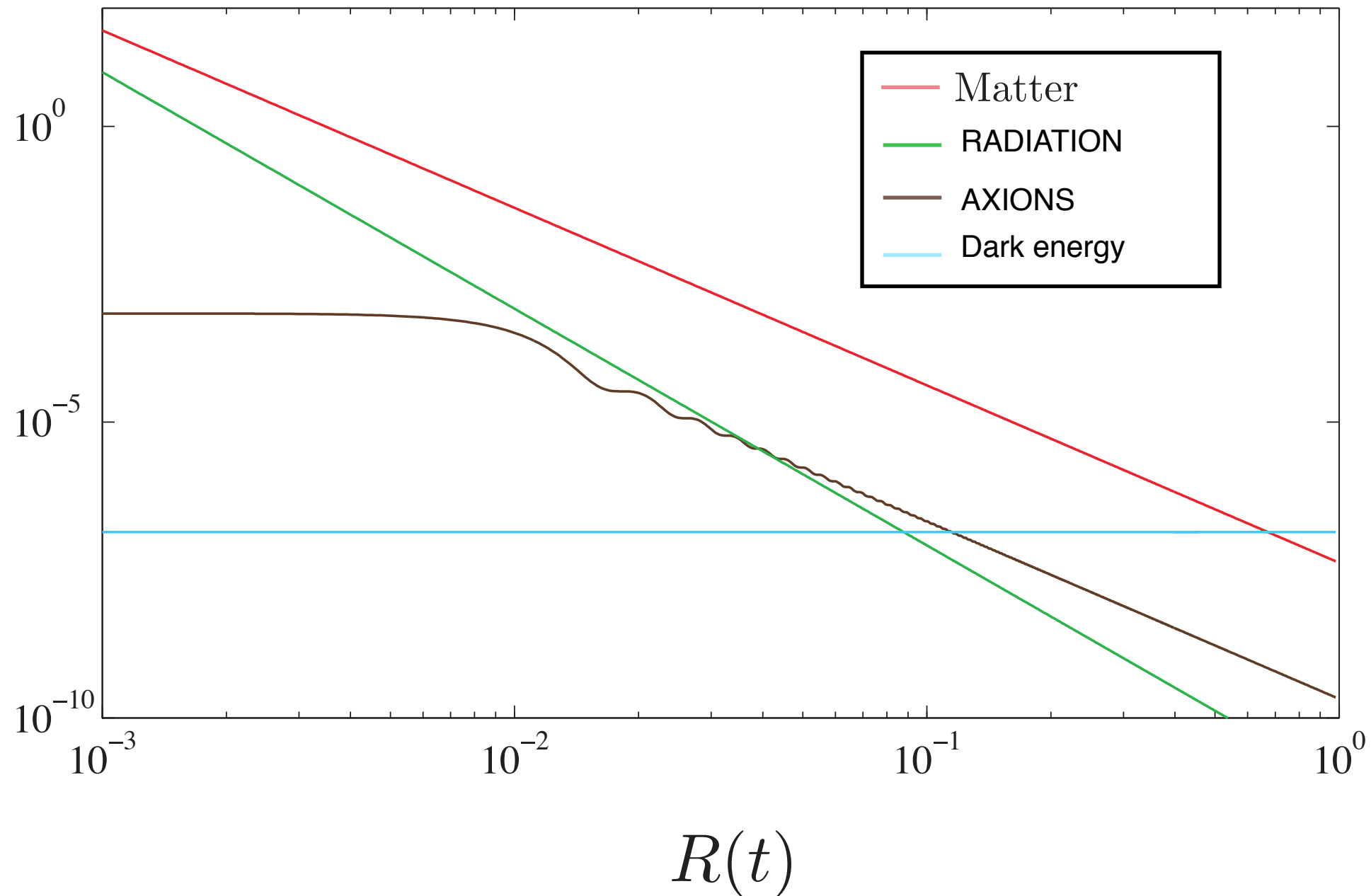


ULAs and the CMB: high mass and early ISW



Matter-radiation balance changed at $z \sim 3400$

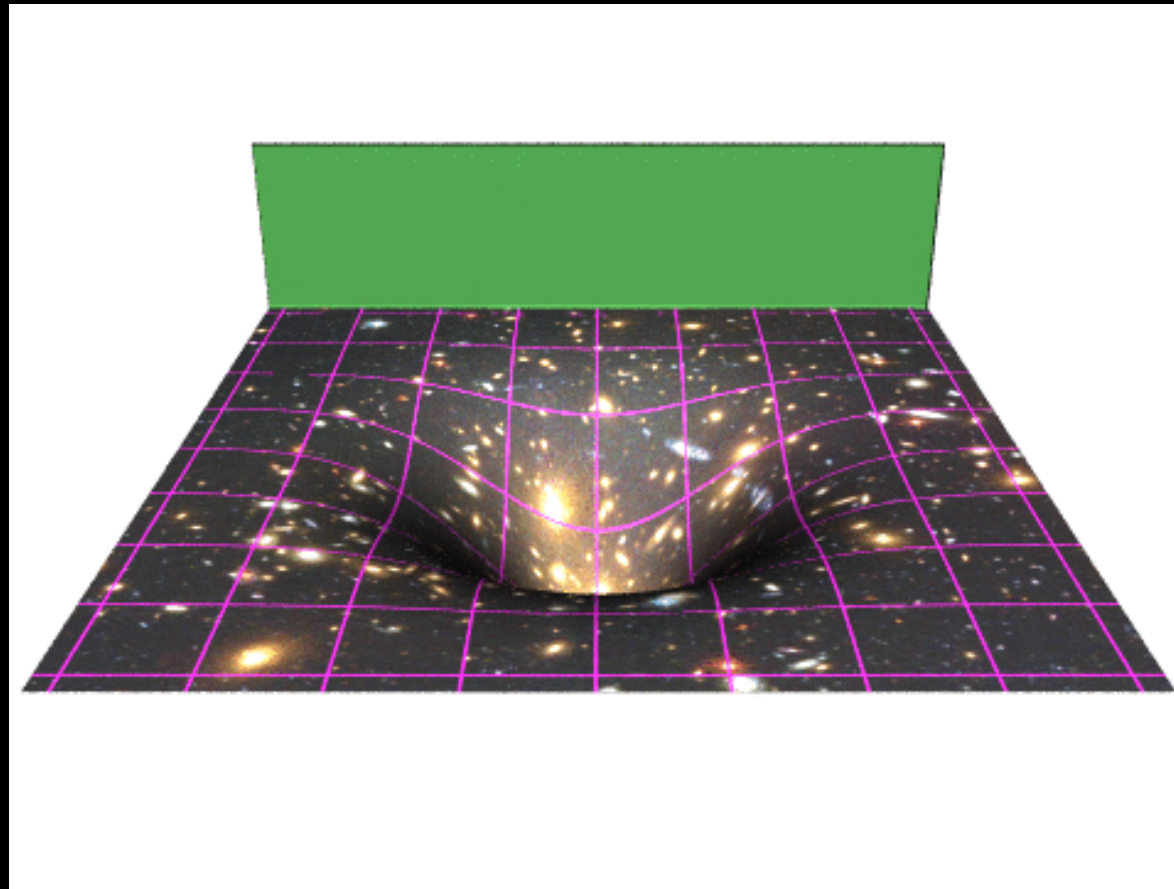
ULAs and the CMB: high mass and early ISW



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ULAs and the CMB: high mass and early ISW

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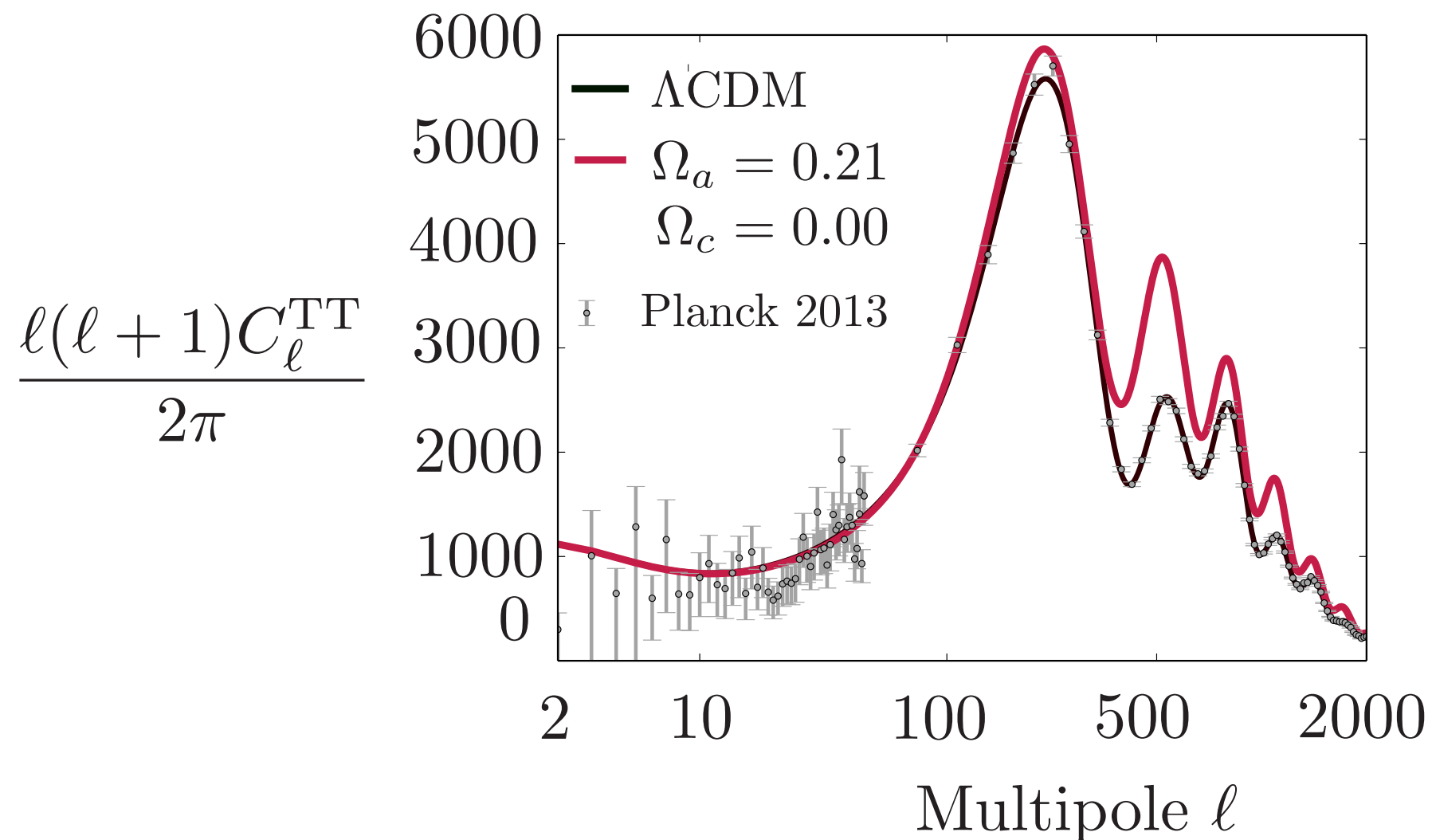


CMB temperature anisotropies from potential decay

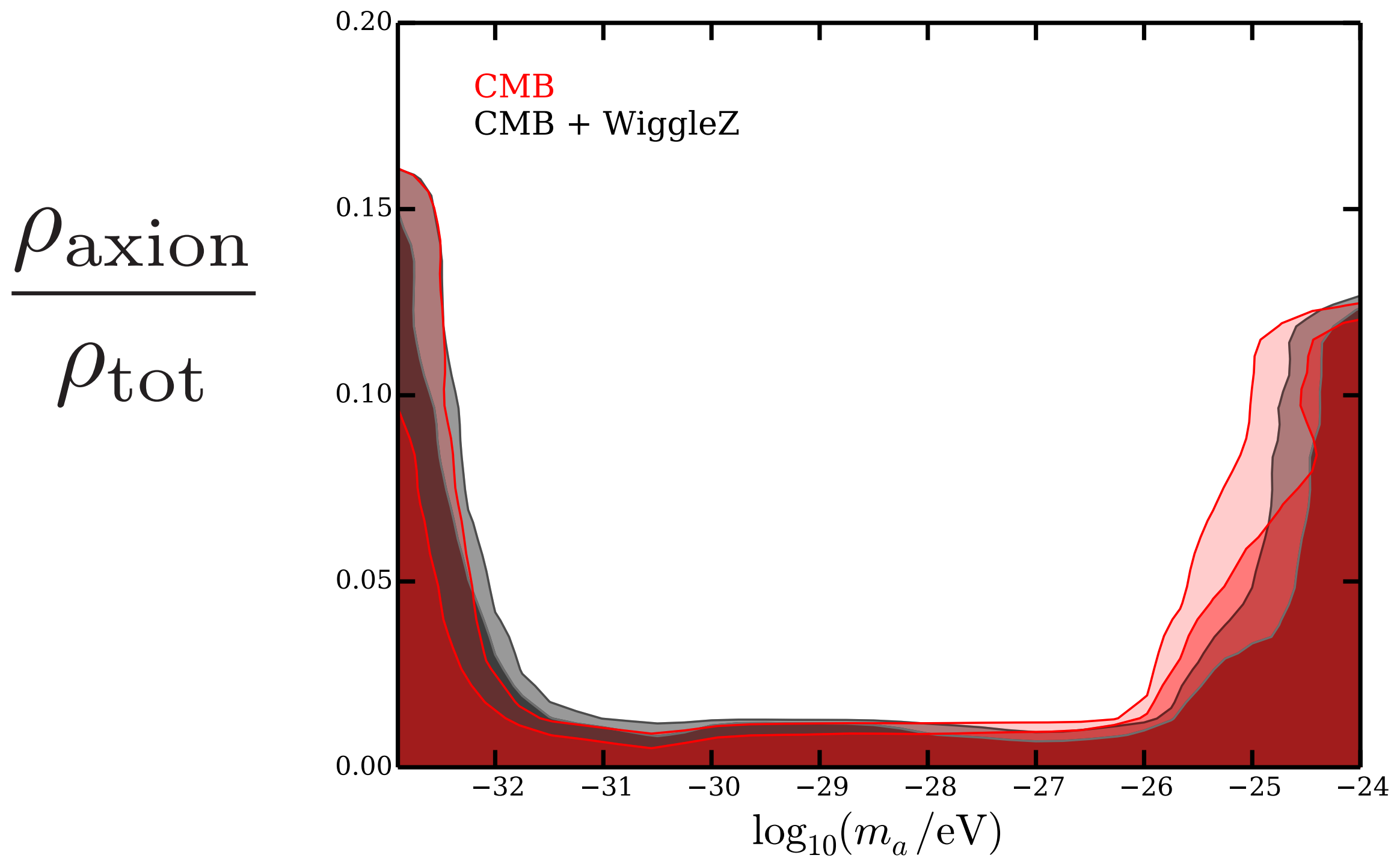
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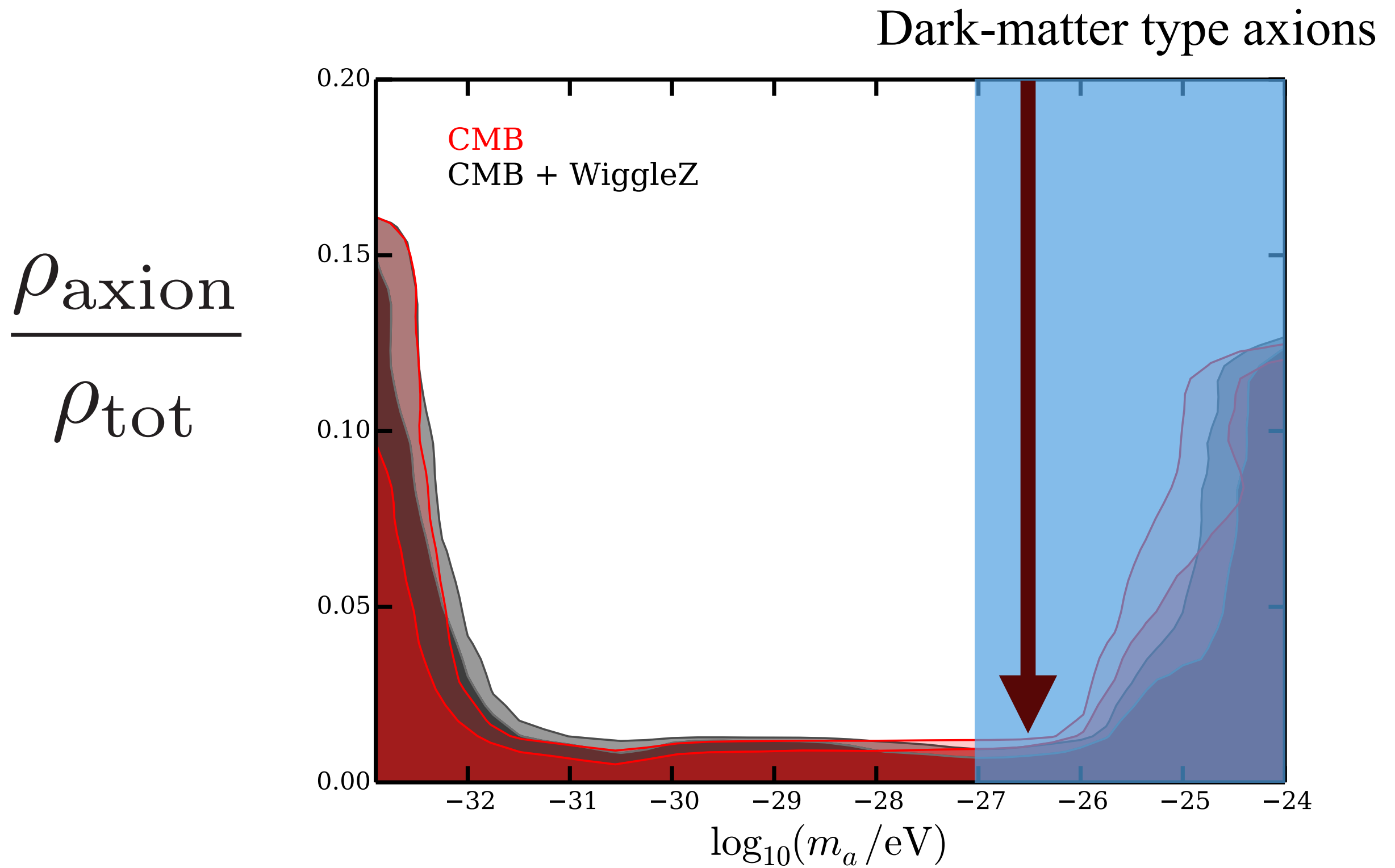
Higher mass (DM-like) case: high- l ISW



PHYSICS BEHIND THE CONSTRAINTS

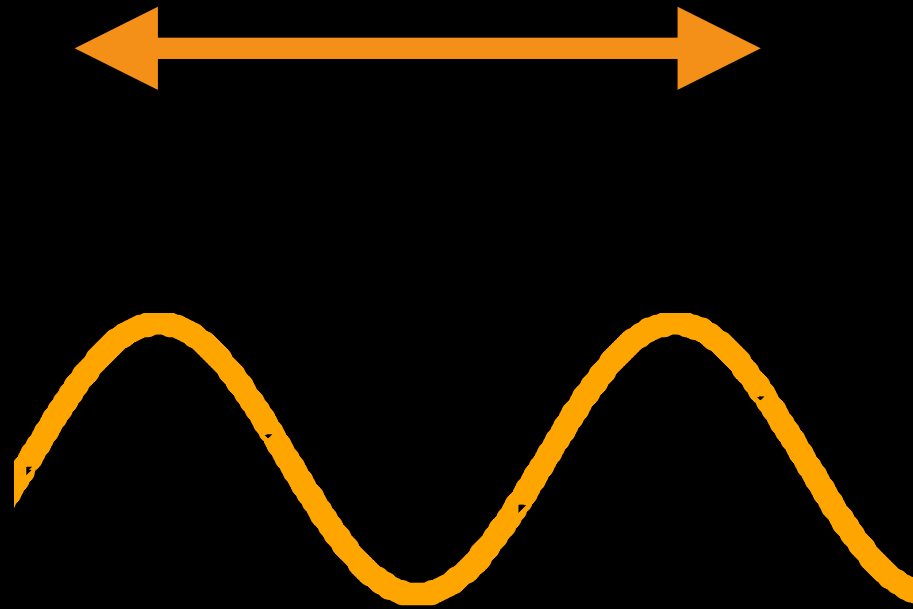


PHYSICS BEHIND THE CONSTRAINTS

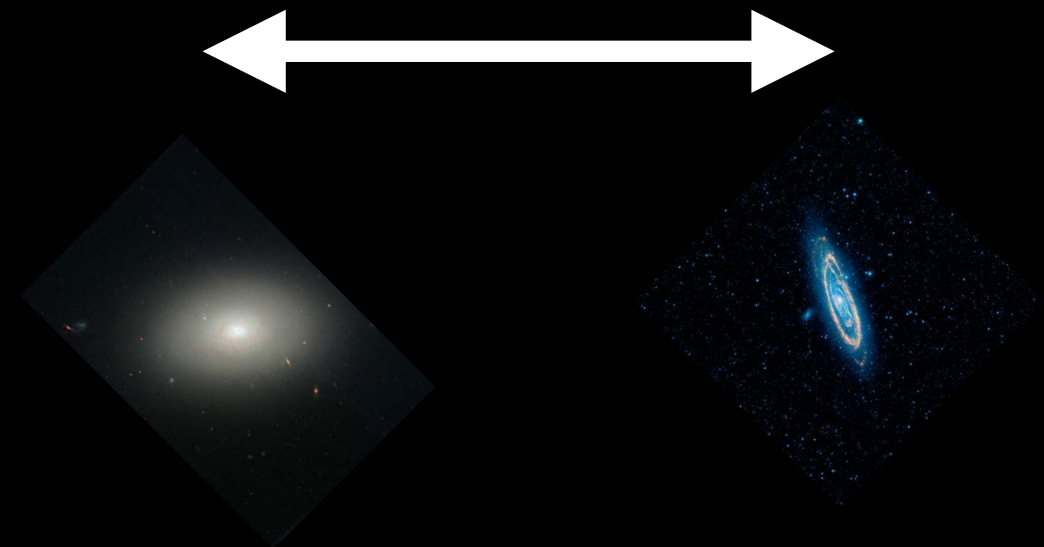


LOOK FOR ULTRA-LIGHT AXIONS IN THE COSMOS

Axion deBroglie wavelength



*Astronomical length scale
kilo-lightyear – giga-lightyear!*



GROWTH OF ULA PERTURBATIONS

✳ Perturbed Klein-Gordon + Gravity

$$\ddot{\delta\phi} + 2\mathcal{H}\delta\dot{\phi} + (k^2 + m_a^2 a^2)\delta\phi = 4\dot{\Psi}\dot{\phi}_0 - \Psi a^2 m_a^2 \phi_0$$

✳ Axionic Jeans Scale is macroscopic [in contrast to QCD axion]:

$$\lambda_J = 2.4h^{-1/2} \left(\frac{m}{10^{-25} \text{ eV}} \right)^{-1/2} \text{ Mpc}$$

✳ Computing observables is expensive for $m \gg 3\mathcal{H}$:

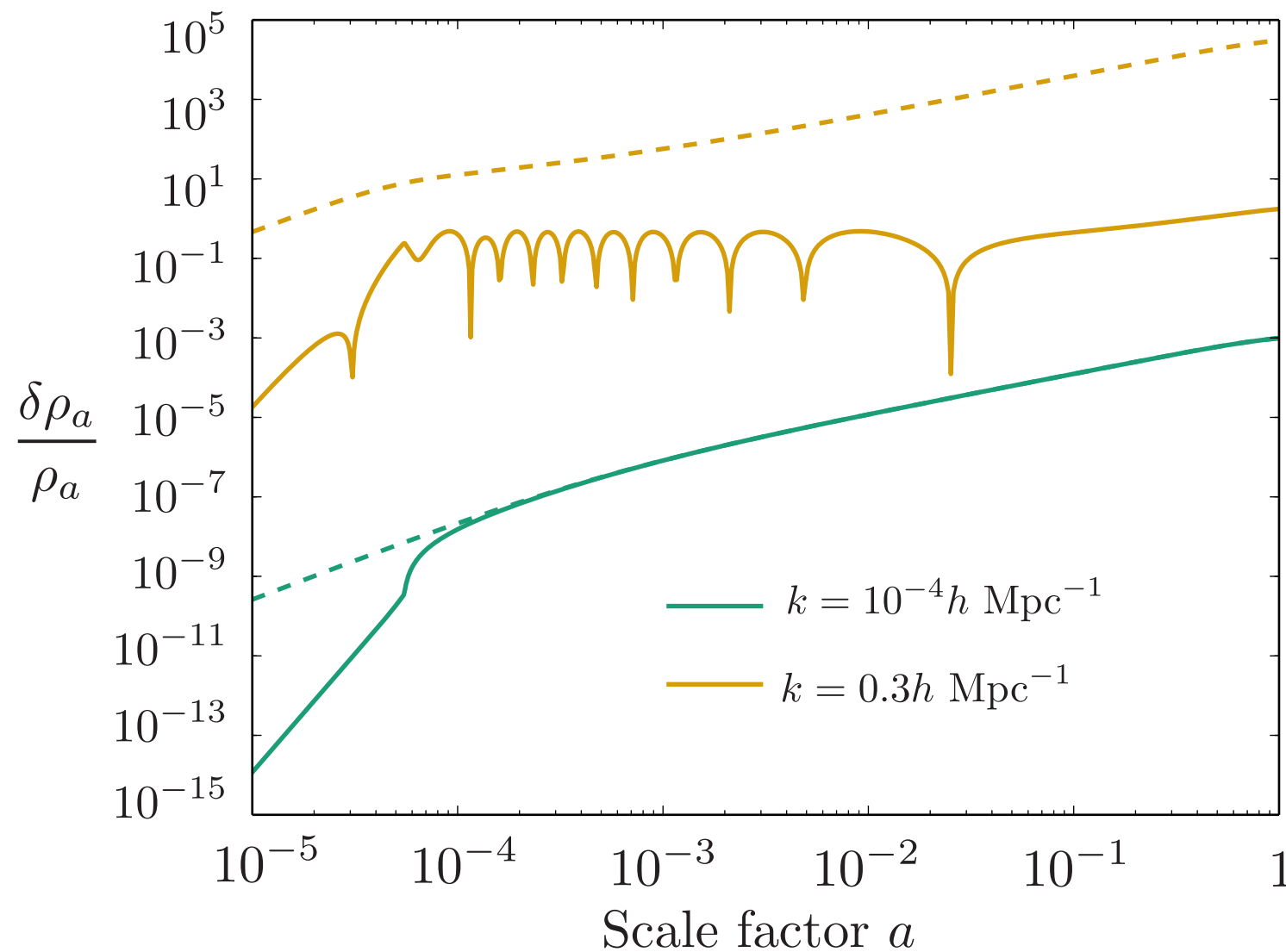
✳ Coherent oscillation time scale $\Delta\eta \sim (ma)^{-1} \ll \Delta\eta_{\text{CAMB}}$

✳ WKB approximation

$$\delta\phi = A_c \Delta_c(k, \eta) \cos(m\eta) + A_s \Delta(k, \eta) \sin(m\eta)$$

$$c_a^2 = \frac{\delta P}{\delta \rho} = \frac{k^2 / (4m^2 a^2)}{1 + k^2 / (4m^2 a^2)}$$

GROWTH OF **ULA** PERTURBATIONS



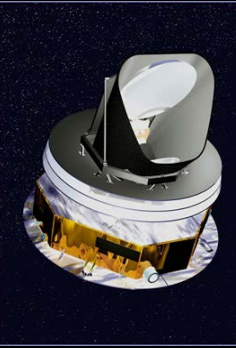
- * Modes with $k \gg k_J \sim \sqrt{m\mathcal{H}}$ oscillate instead of growing
- * “Pressure” stabilization

DATA

- * Planck 2013 temperature anisotropy power spectra (+SPT+ACT+BAO)

- * Cosmic variance limited to $\ell \sim 1500$

- * Power spectrum already shown



- * WiggleZ galaxy survey (linear scales only $k \lesssim 0.2h \text{ Mpc}^{-1}$)

- * Galaxy bias marginalized over

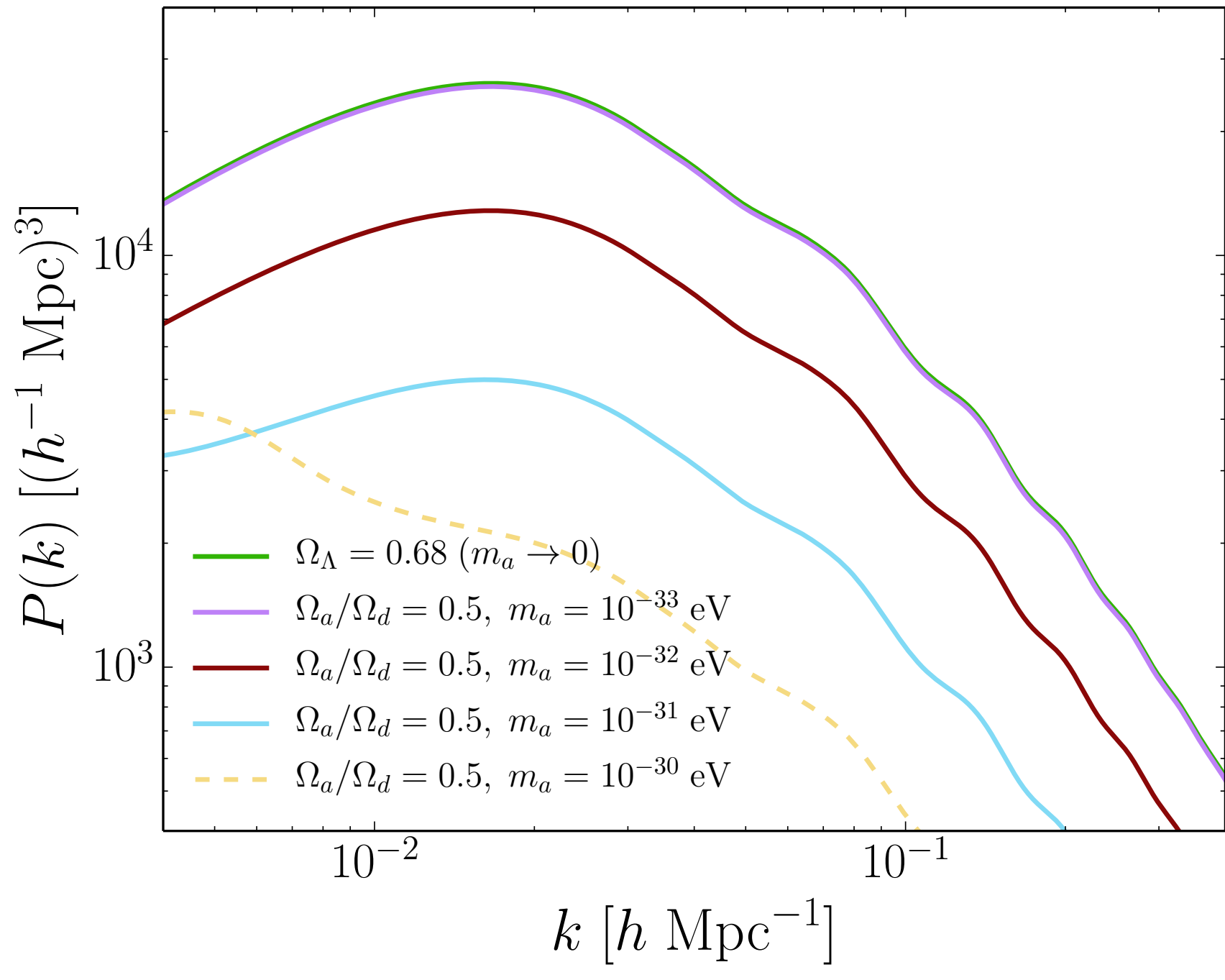
- * Theory $P(k)$ convolved with survey window function

- * 240,000 emission line galaxies at $z < 1$

- * 3.9 m Anglo-Australian Telescope (AAT)



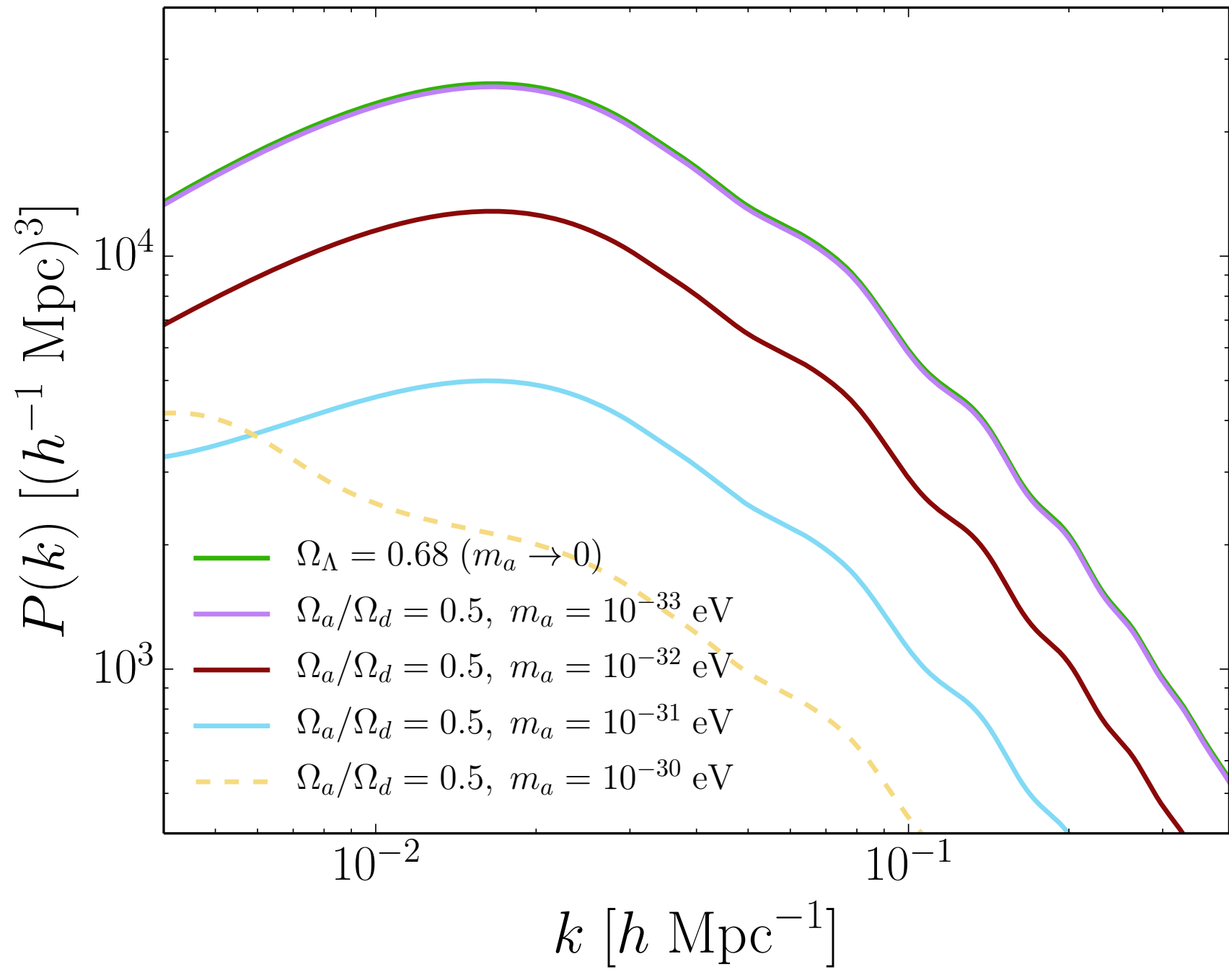
Matter power spectrum for ULA (in DE regime)



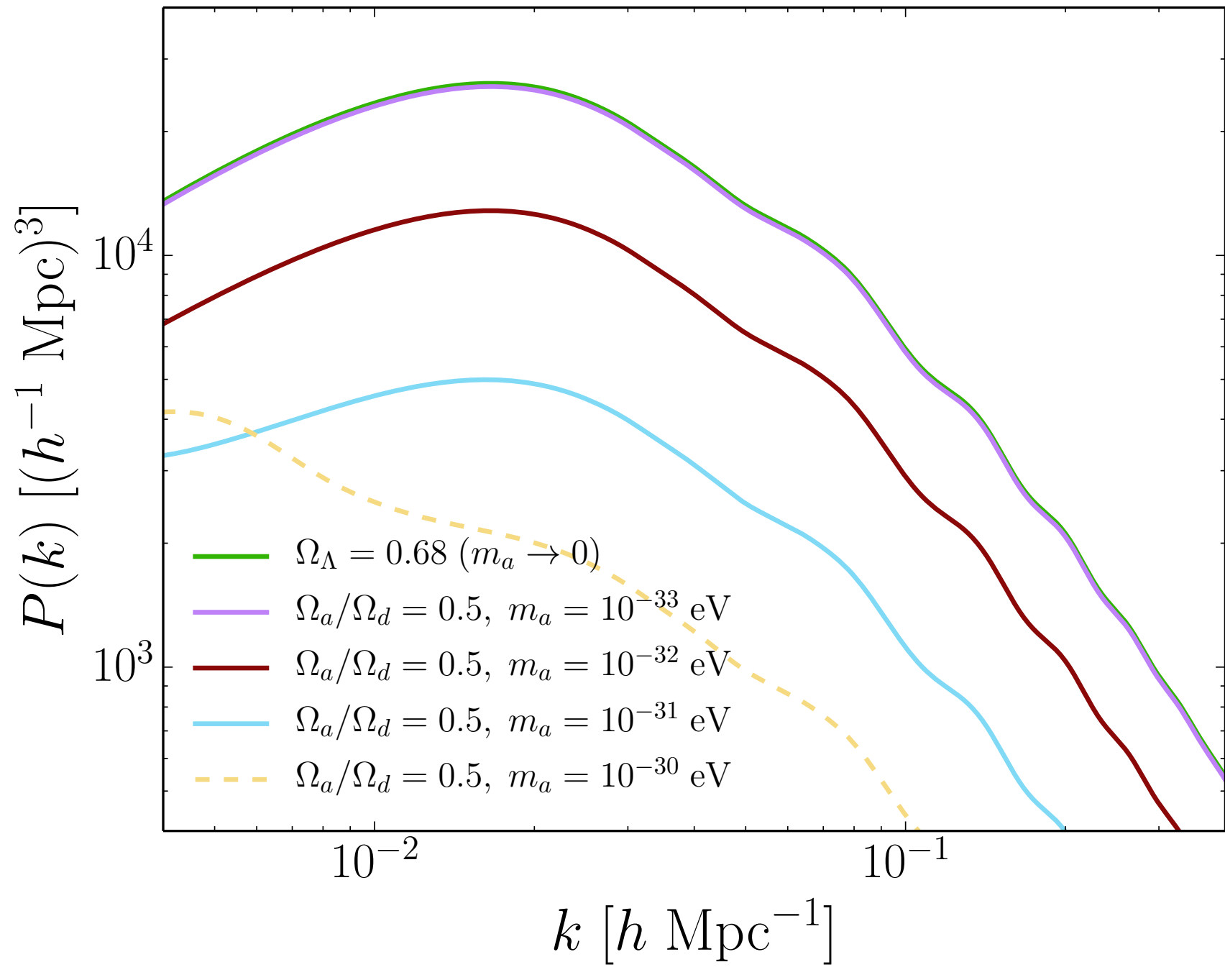
θ_s

Matter power spectrum for ULA (in DE regime)

θ_s fixed to lock CMB



Matter power spectrum for ULA (in DE regime)



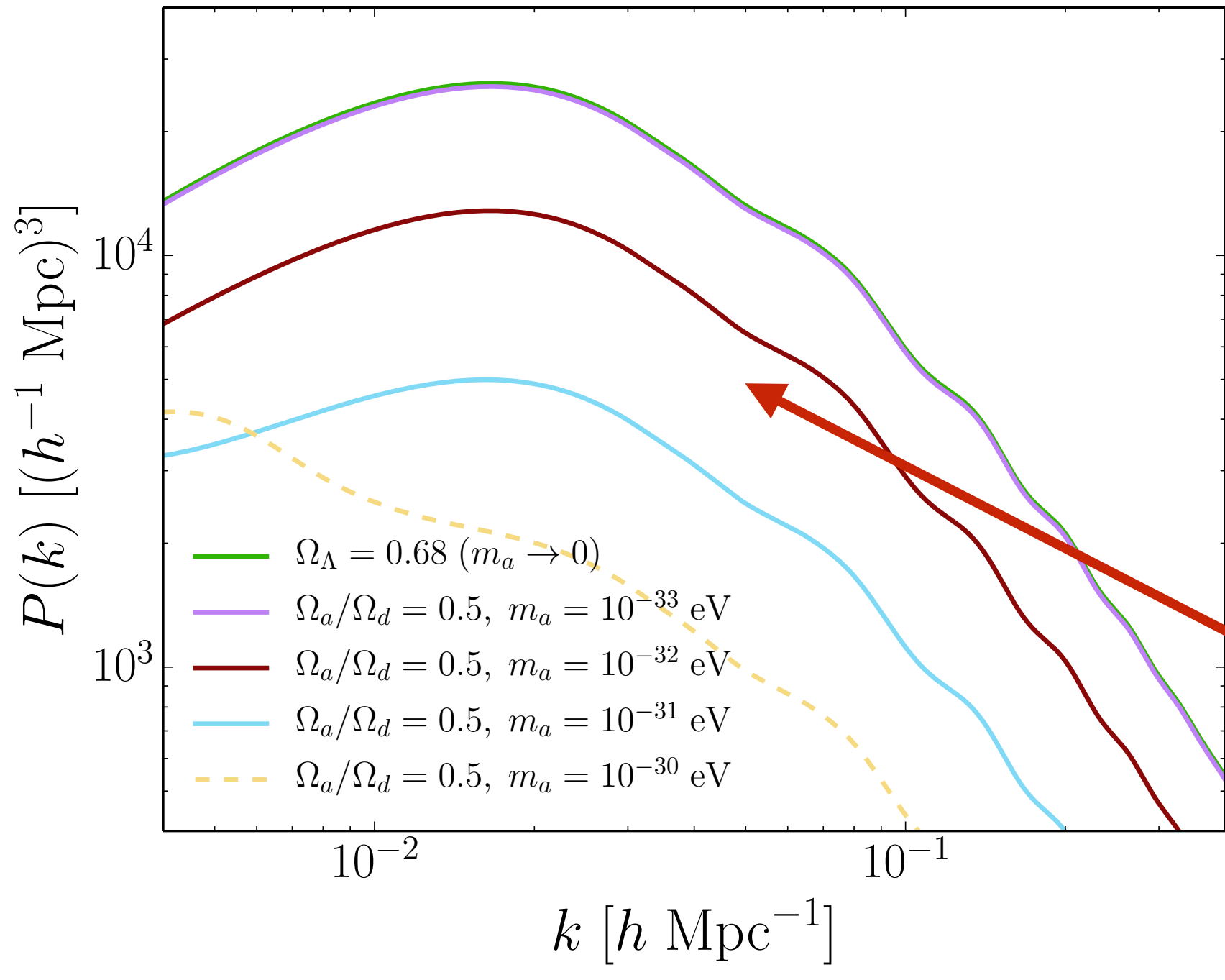
θ_s fixed to lock CMB

$H_0 \downarrow$

$$1 + z_{eq} = \frac{\Omega_m h^2}{\rho_{\text{rad}}}$$

Matter-radiation equality delayed

Matter power spectrum for ULA (in DE regime)



θ_s fixed to lock CMB

$H_0 \downarrow$

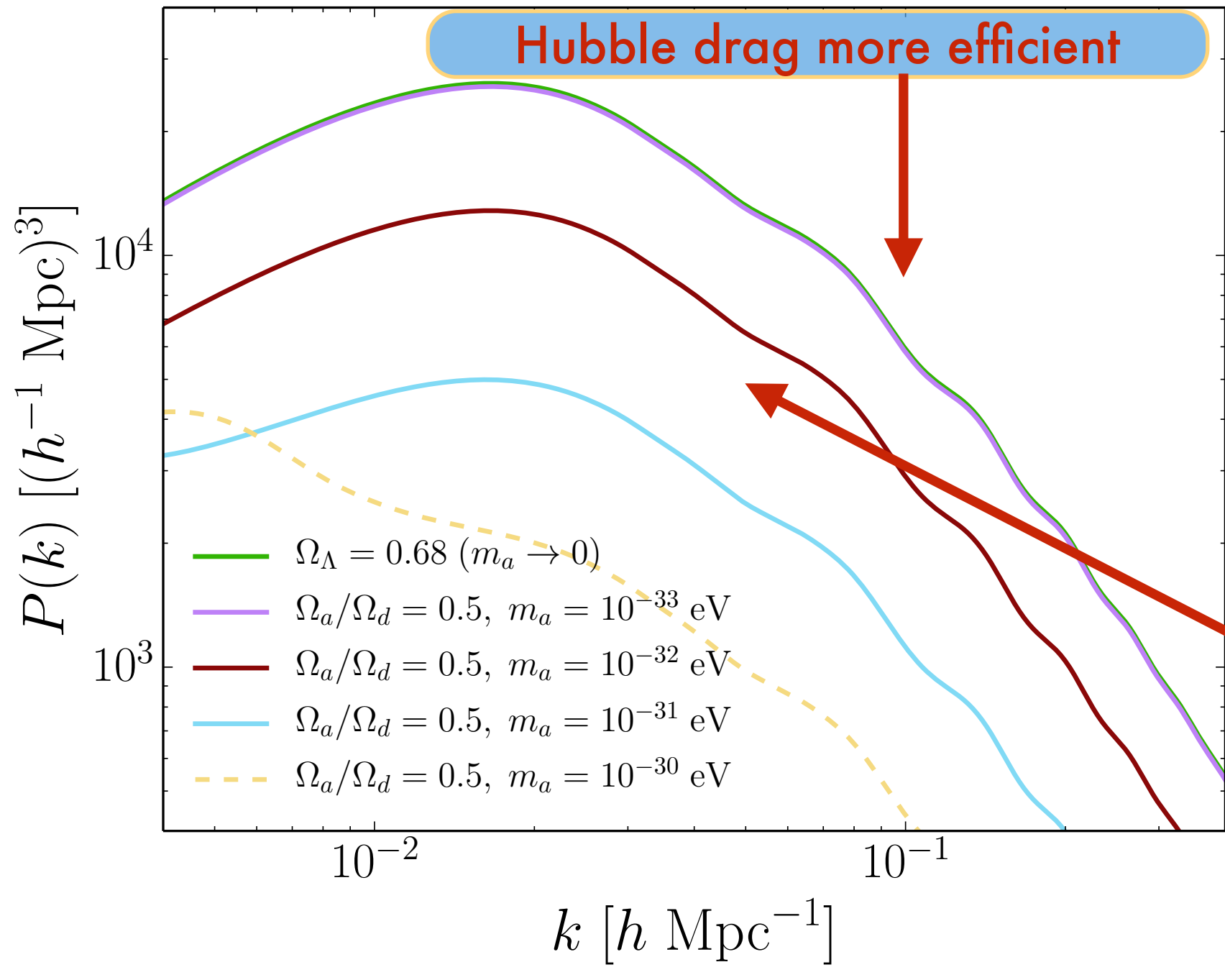
$$k_{eq} = \lambda_{\text{horizon,eq}}^{-1} \downarrow$$

Peak of $P(k)$ to lower k

$$1 + z_{eq} = \frac{\Omega_m h^2}{\rho_{\text{rad}}}$$

Matter-radiation equality delayed

Matter power spectrum for ULA (in DE regime)



θ_s fixed to lock CMB

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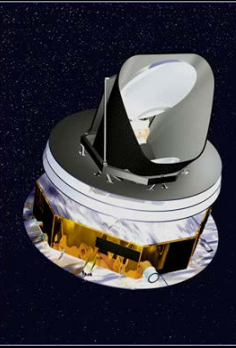
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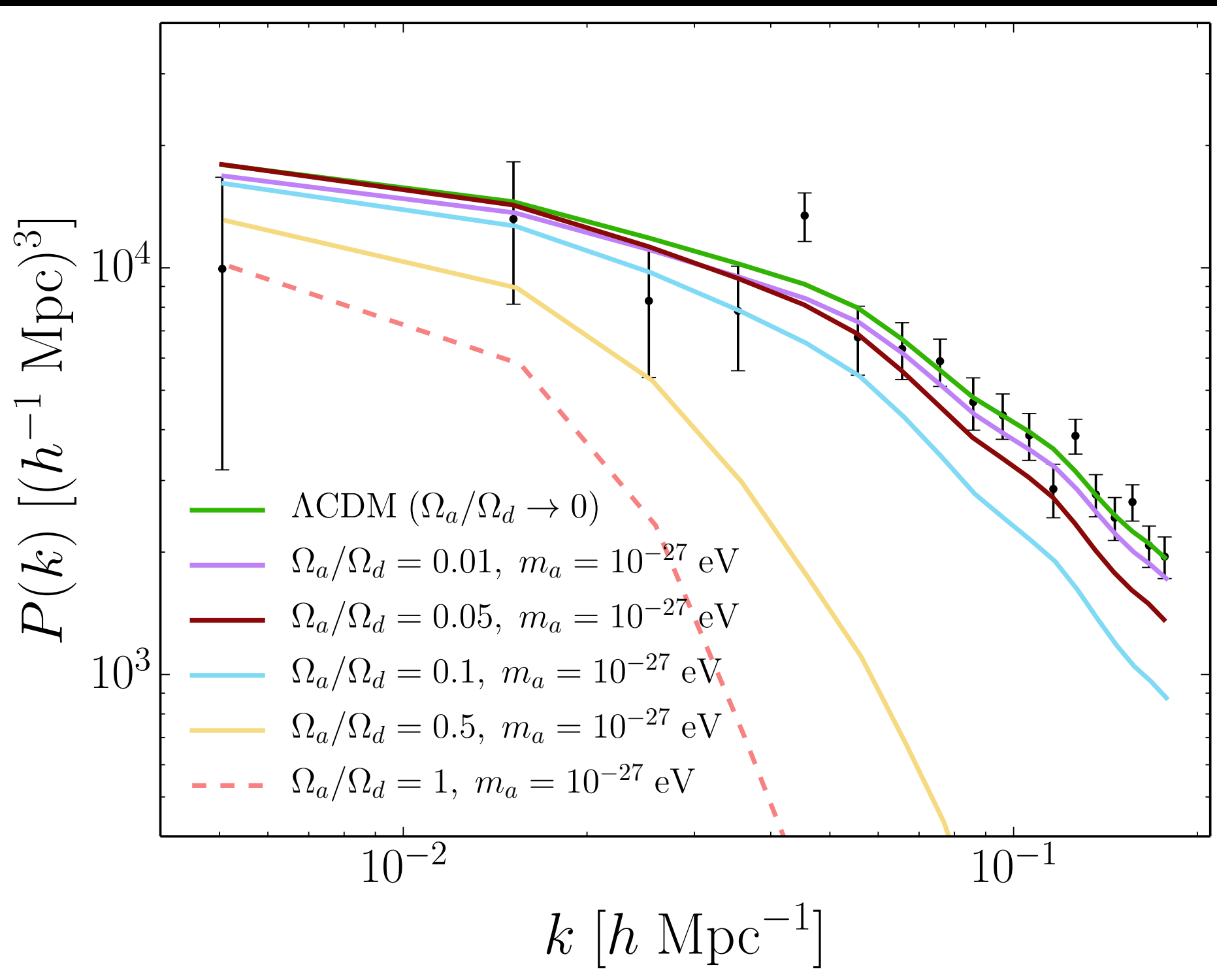
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Data



Difficult parameter space

$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$

— —

Difficult parameter space

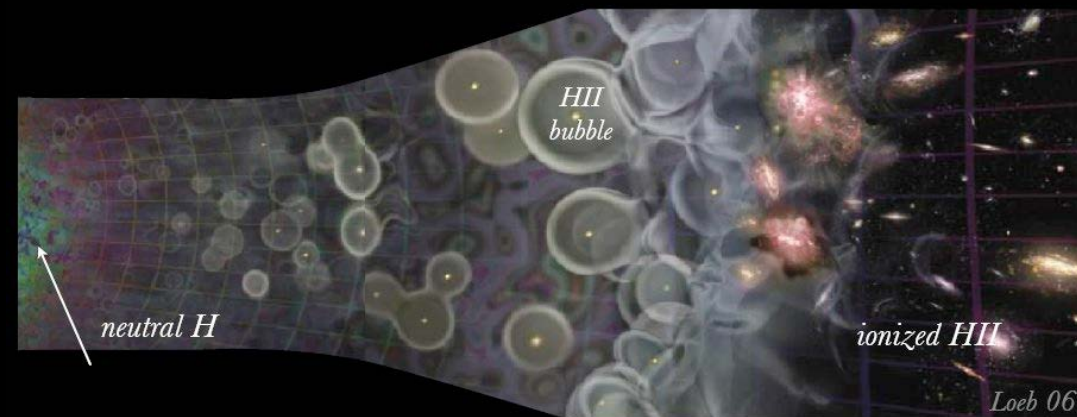
$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$

$$\Delta_{\mathcal{R}}^2(k) \equiv A_s \left(\frac{k}{k_0} \right)^{n_s - 1} \quad \text{Initial conditions}$$

Difficult parameter space

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$$\tau_{\text{reion}} \equiv \int dl n_e \sigma_T$$



Difficult parameter space

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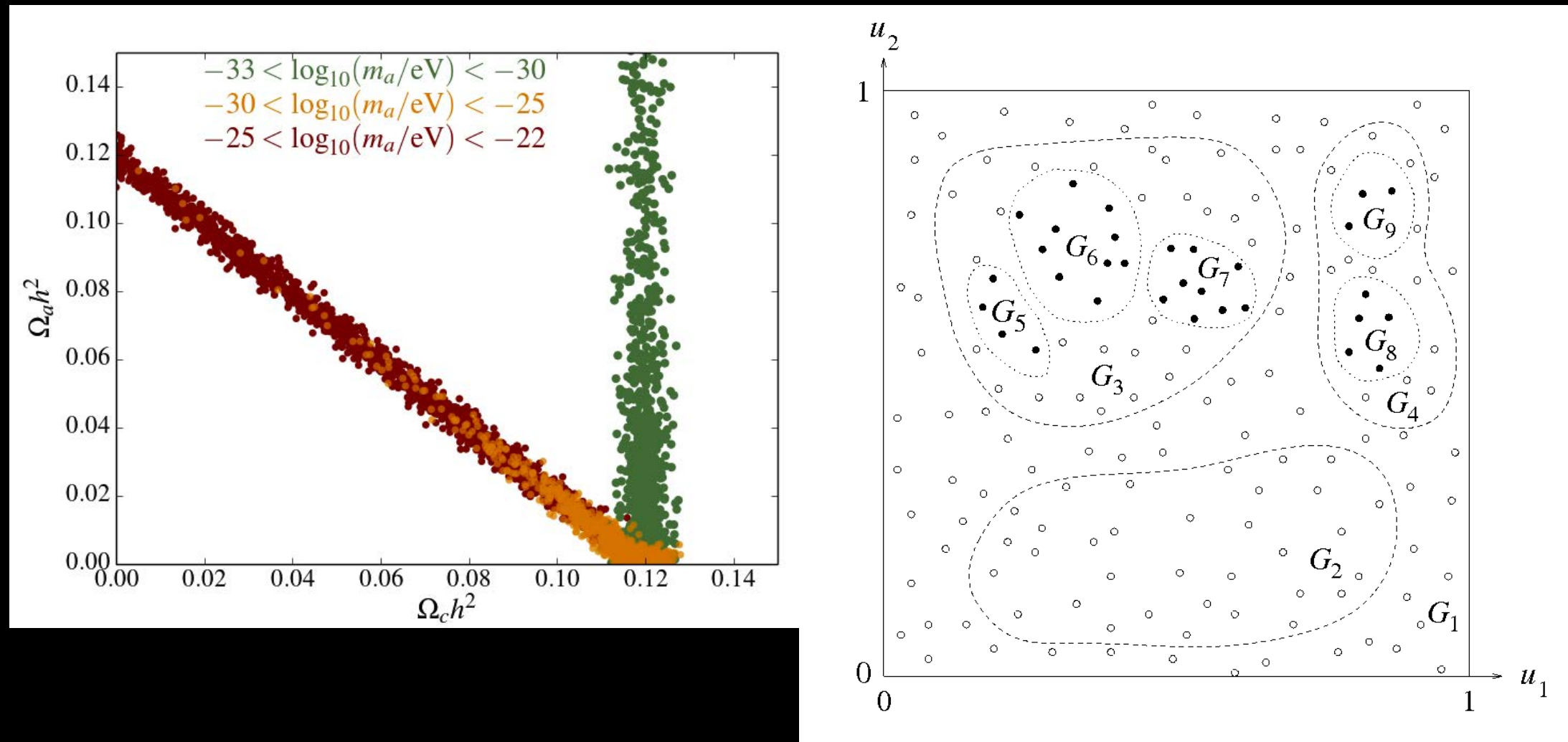
AxiCAMB



Compare with data
Explore posterior using Monte Carlo
Markov Chain (MCMC)

Difficult parameter space

$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$



Addressed using nested sampling
MULTINEST (Hobson, Feroz, others 2008)

Parameter space

$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$

— —

Parameter space

$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$



ULA parameters

Parameter space

$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$



Densities of standard species

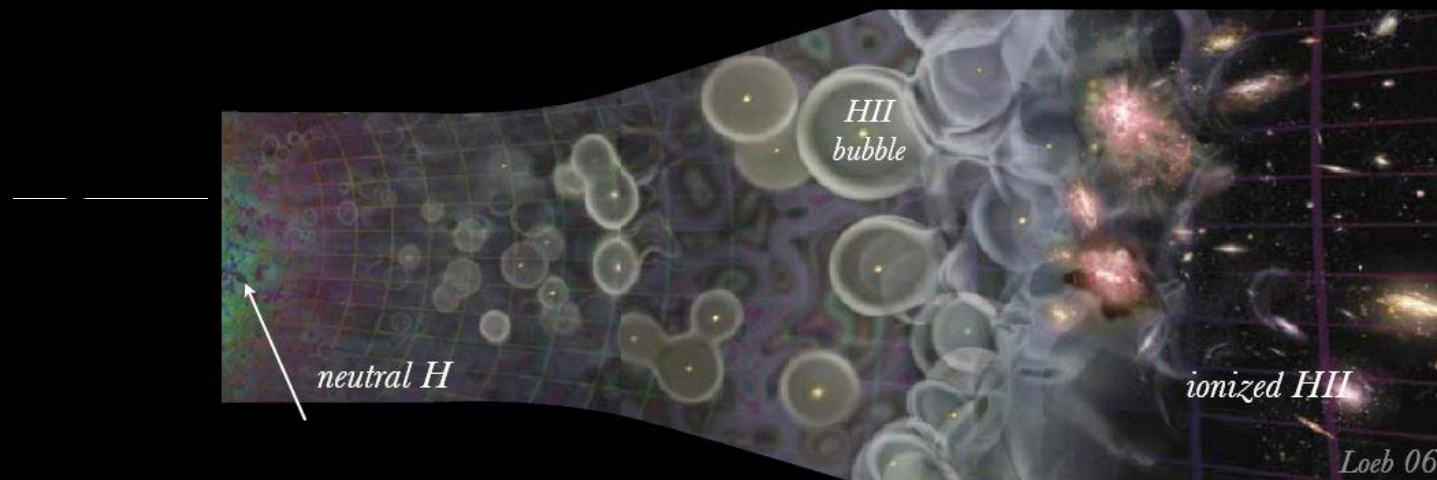
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Parameter space

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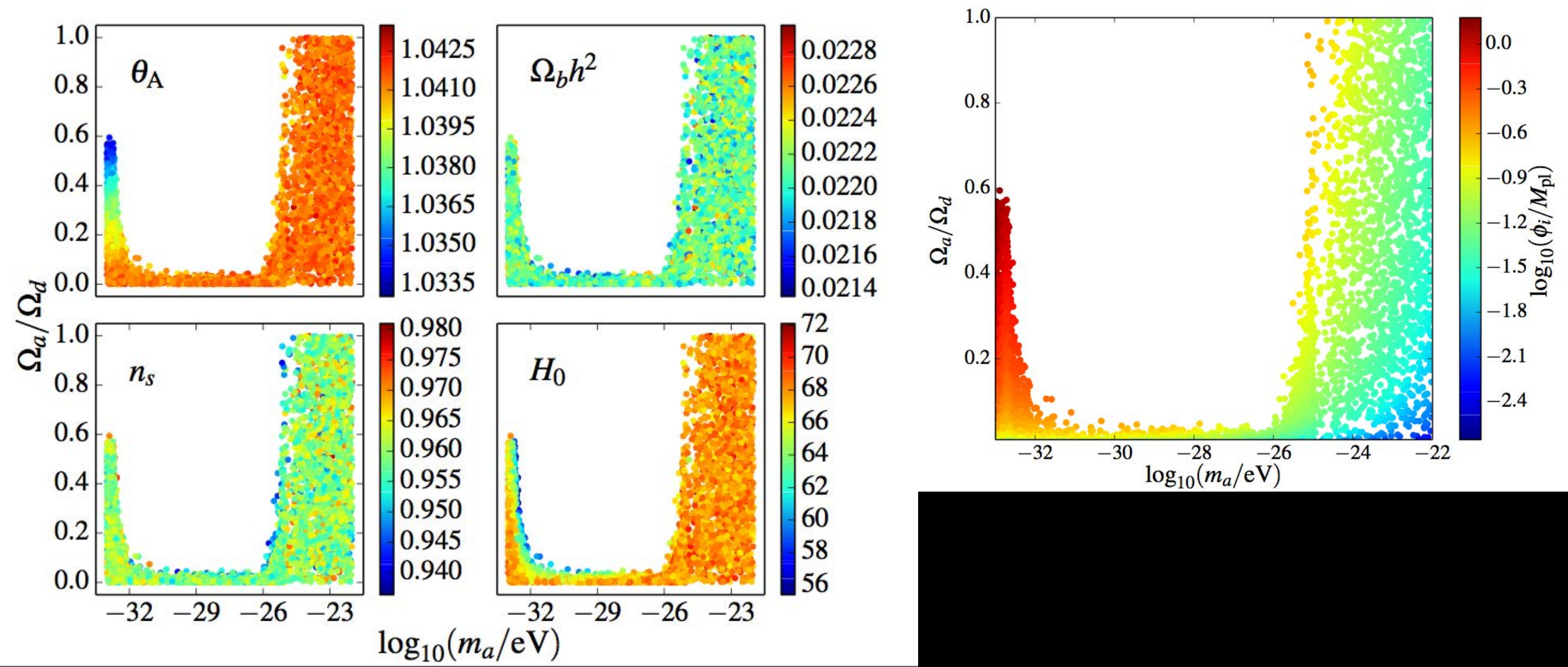
AxionCAMB



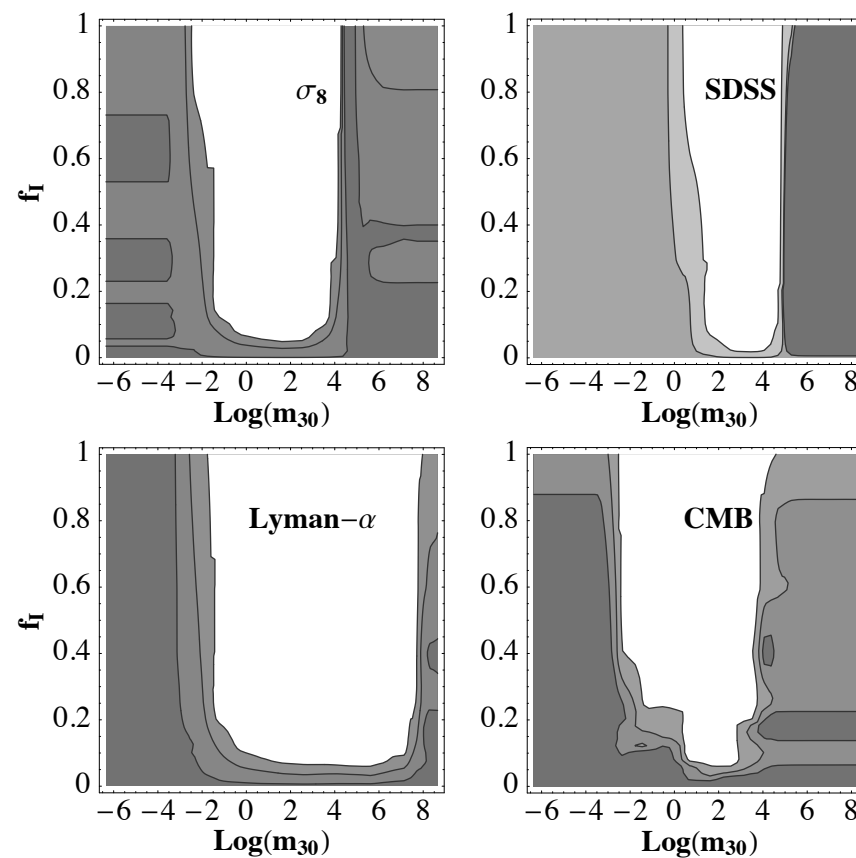
Compare with data

Explore posterior using Nested sampling

Degeneracies/Weak gravity conjecture



Amendola and Barbieri



Old power spectrum constraints from Amendola and Barbieri, arXiv:hep-ph/0509257

- 1) Grid search
- 2) No isocurvature
- 3) No marginalization over foregrounds
- 4) No lensing, no polarization
- 5) No real Boltzmann code [step in power spectrum, or unclustered DE at low m]

Difficult parameter space

$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$

— —

Difficult parameter space

$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$



ULA parameters

Difficult parameter space

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Densities of standard species

Difficult parameter space

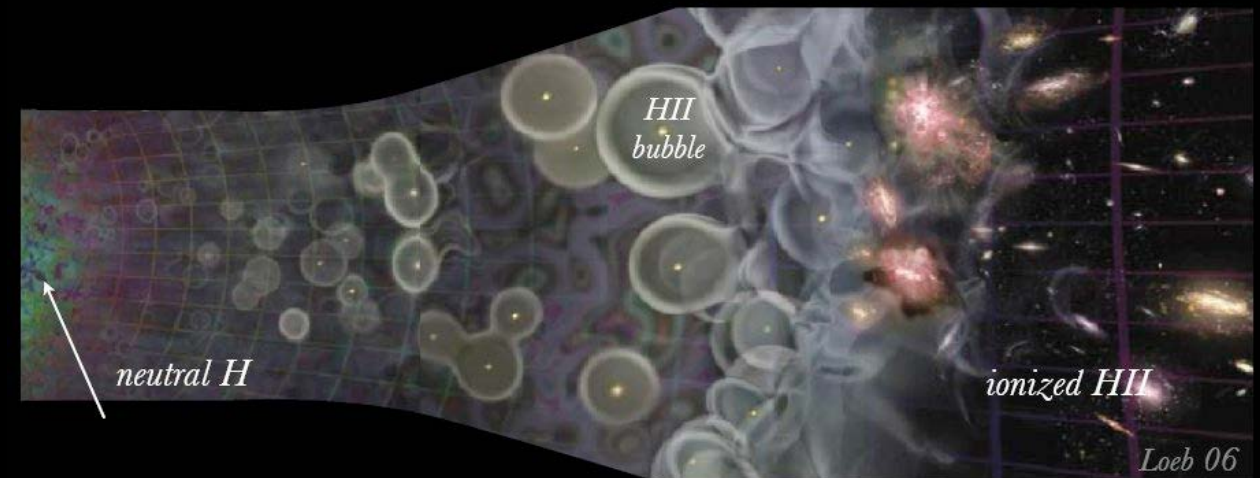
$$m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$$

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Difficult parameter space

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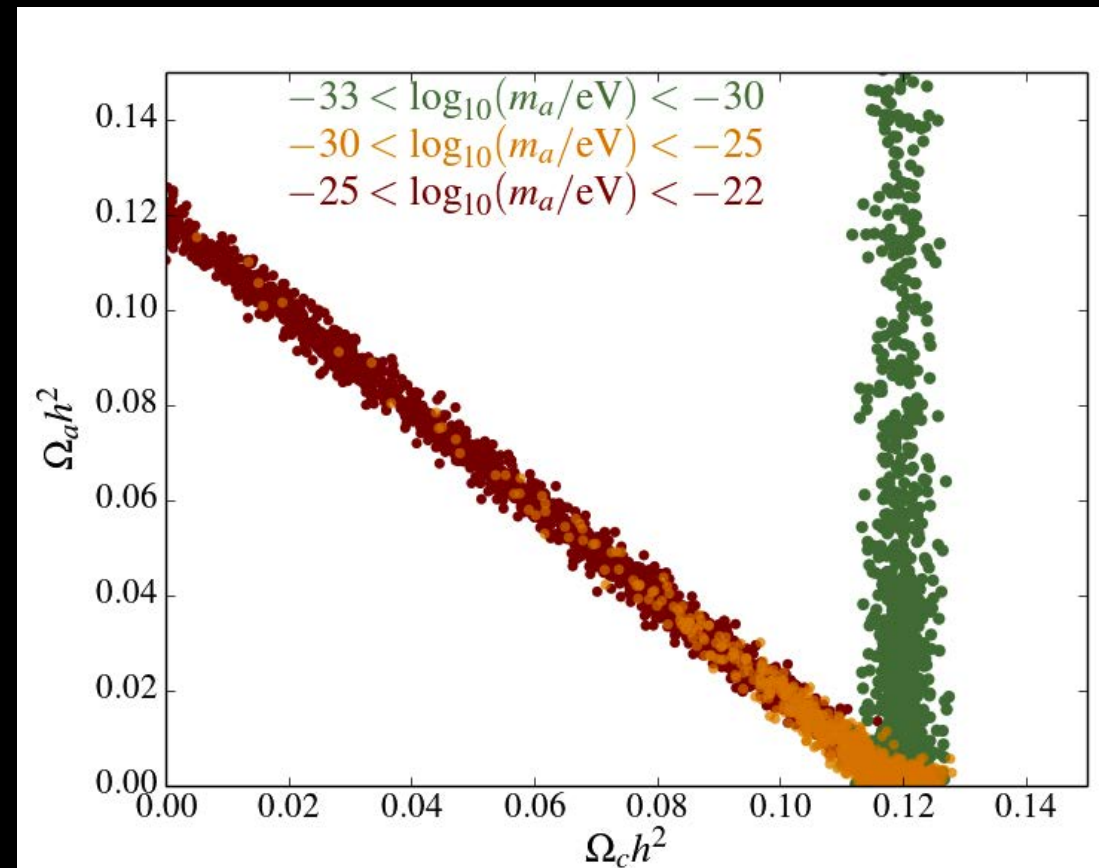
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Compare with data
Explore posterior using Monte Carlo
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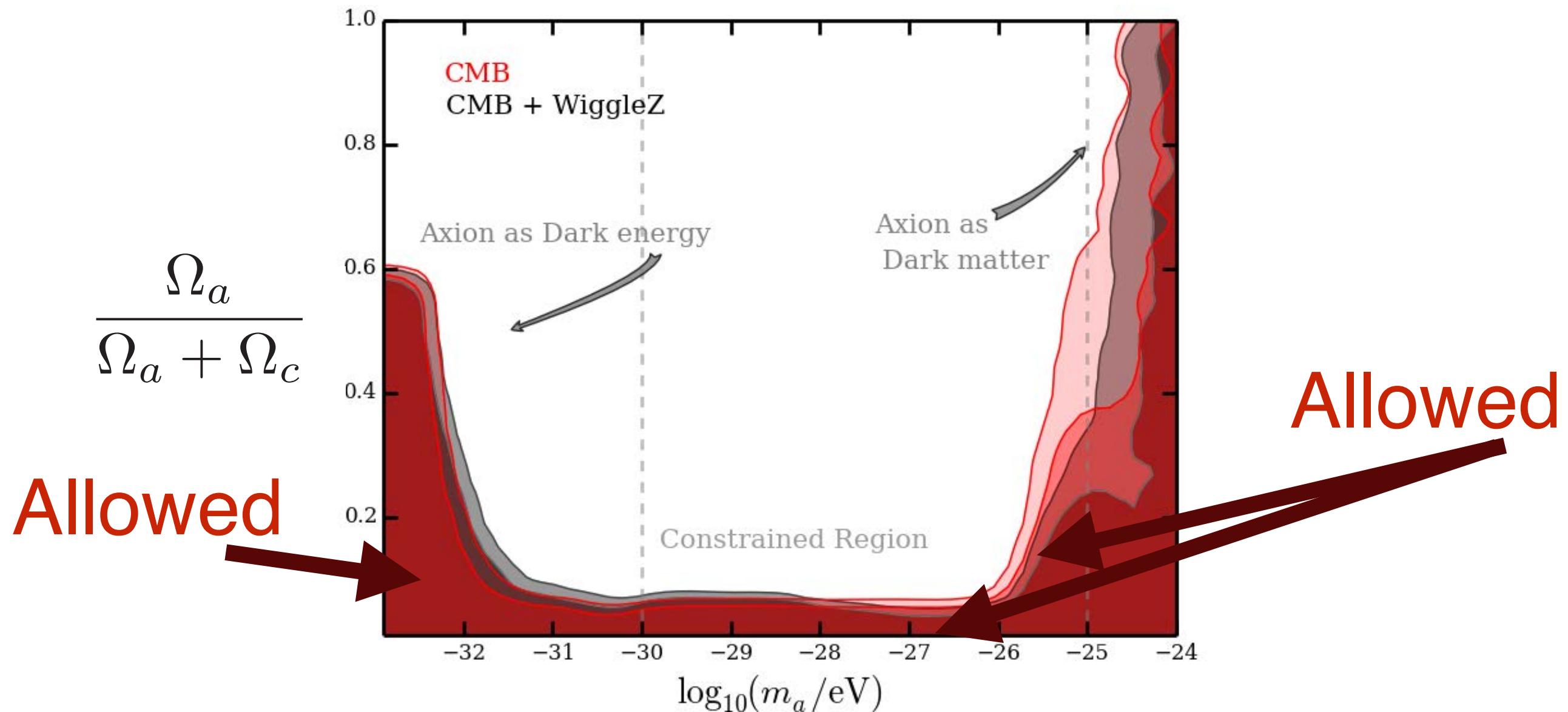
Difficult parameter space

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Addressed using nested sampling
MULTINEST (Hobson, Feroz, others 2008)

CONSTRAINTS



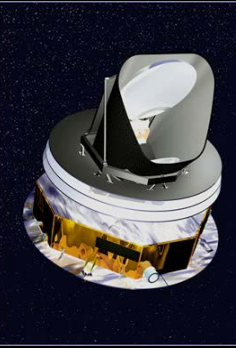
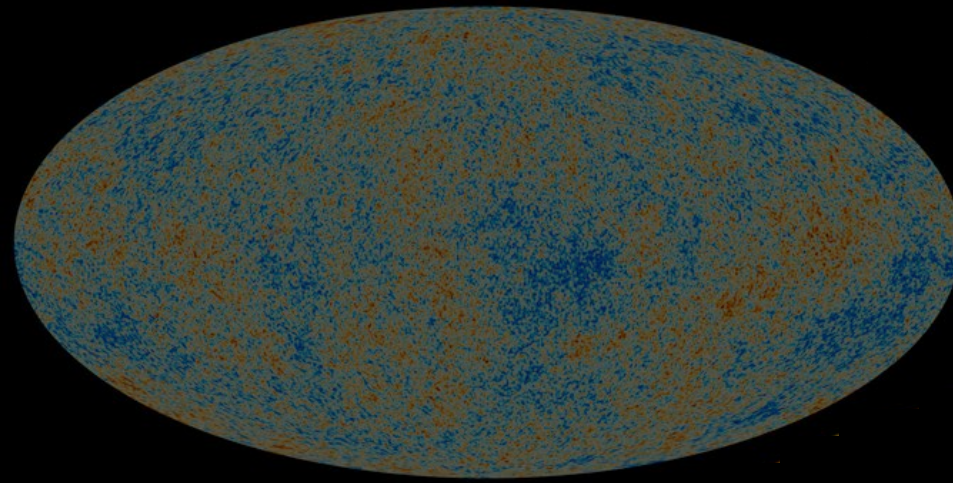
*Interesting constraints over 7 orders of magnitude in mass:

Thanks to **AXICAMB** and **MULTINEST**

*ULAs highly constrained if $10^{-32} \text{ eV} \lesssim m_a \lesssim 10^{-25.5} \text{ eV}$

*ULAs are viable DM/DE candidates in linear theory outside ``belly” 133

DATA + ANALYSIS



* Planck 2013 temperature anisotropy power spectra (+SPT+ACT)

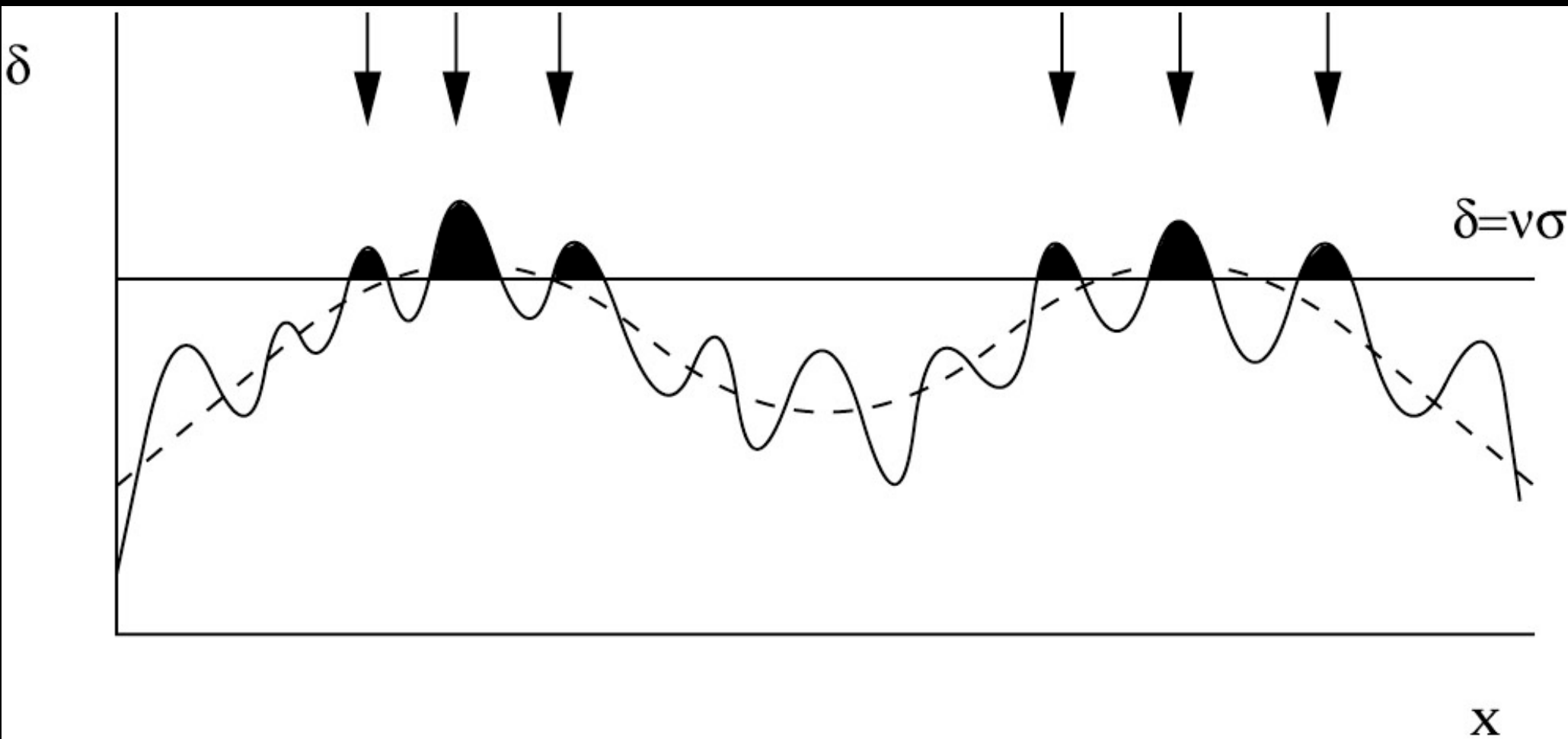
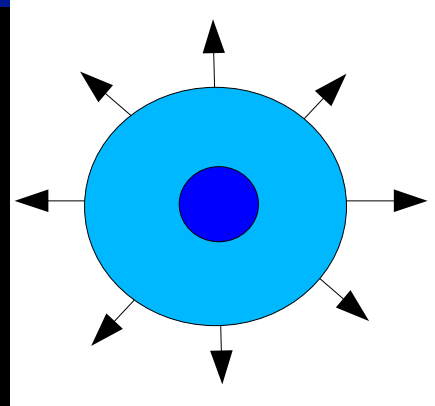
* Cosmic variance limited to $\ell \sim 1500$



* Nested sampling, MCMC, vary $m_a, \Omega_a h^2, \Omega_c h^2, \Omega_b h^2, \Omega_\Lambda, n_s, A_s, \tau_{\text{reion}}$

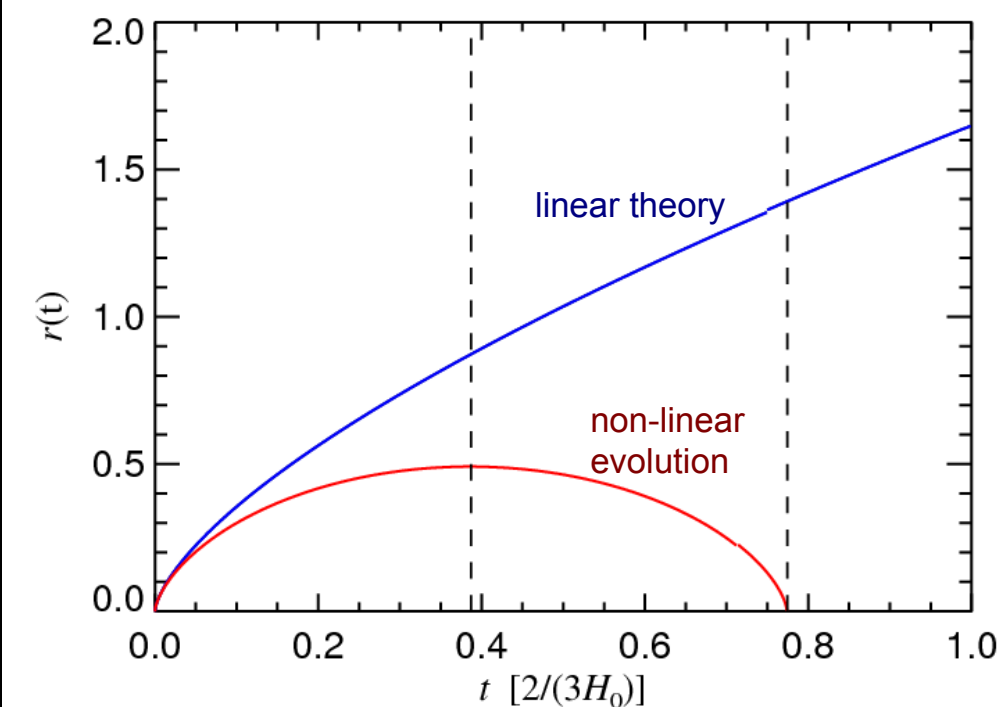
FUTURE WORK: ULAS AND GALAXIES

Collapse threshold for ULA DM unknown

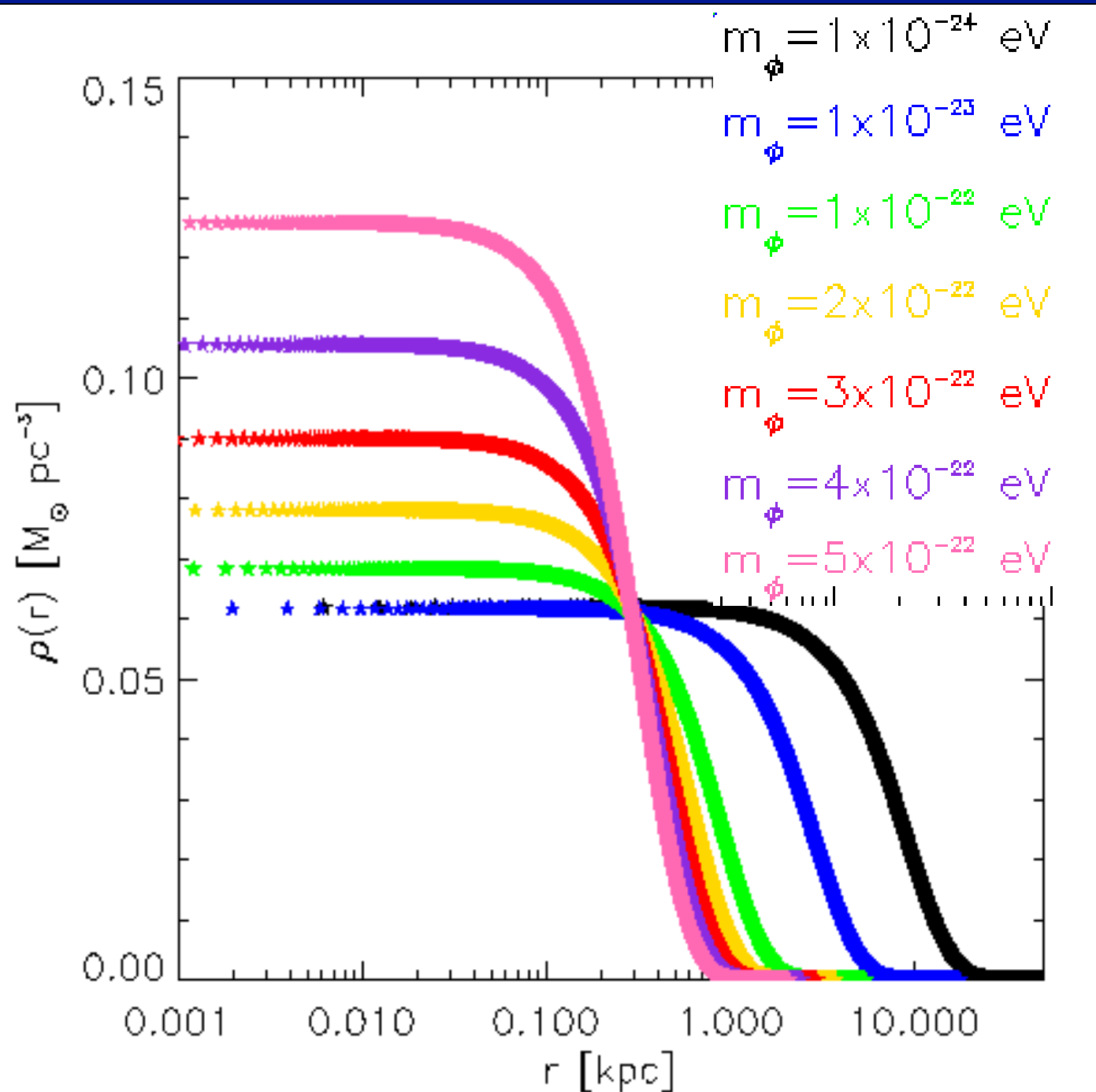


$$\delta_c^{\Lambda\text{CDM}} = 1.686$$

$$\delta_c^{\Lambda\text{ULA}} = \text{????}$$

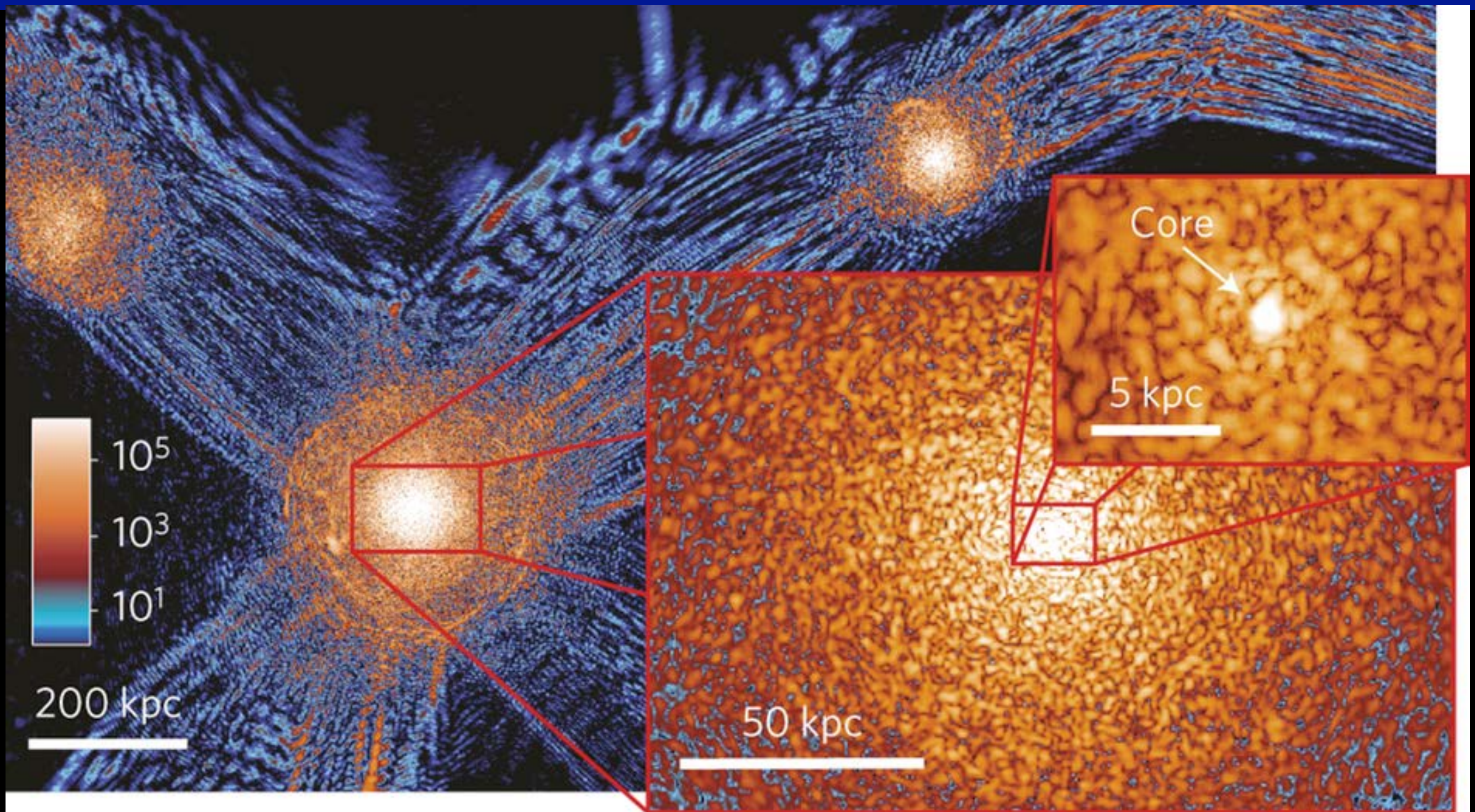


FUTURE WORK: ULAS CORES + CUSPS?



Cores! (Hu/Gruzinov/Barkana 2001, see also Marsh and Silk 2013, Marsh and Pop 2015, Matos 2012, Schive 2014, and others)

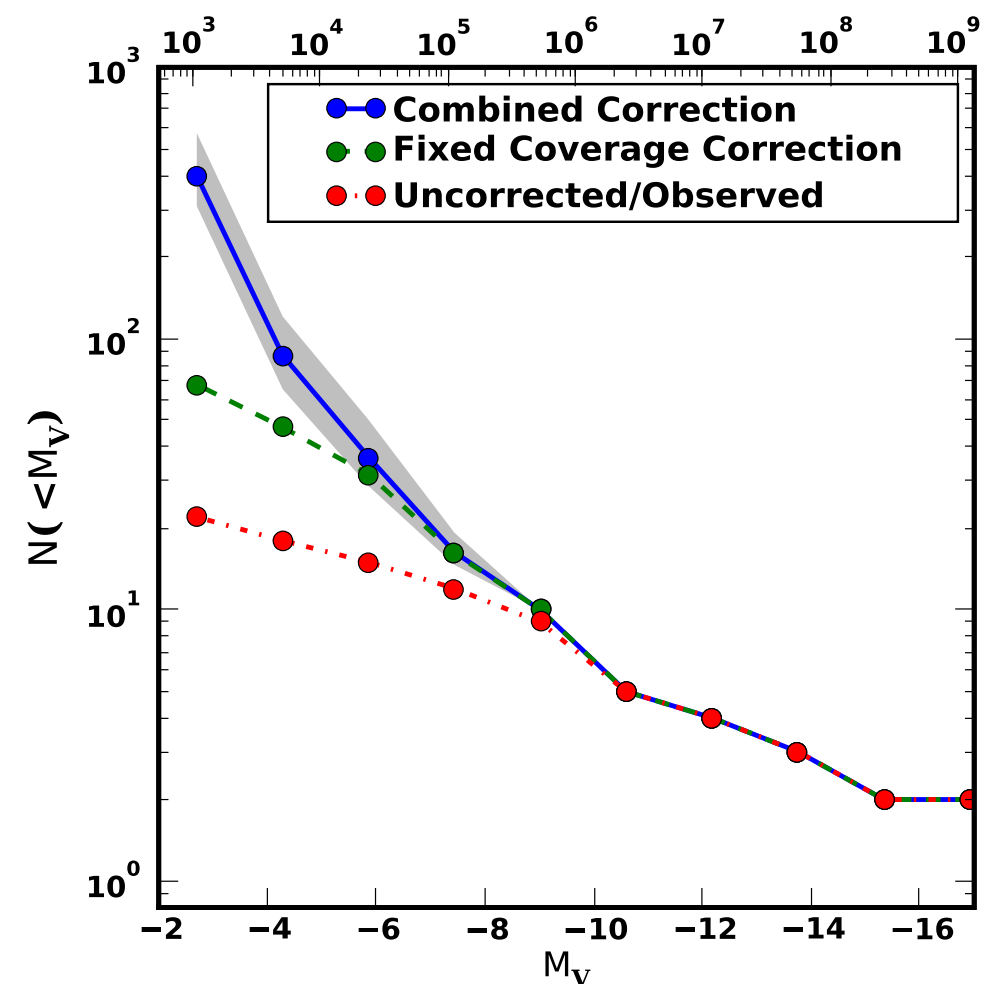
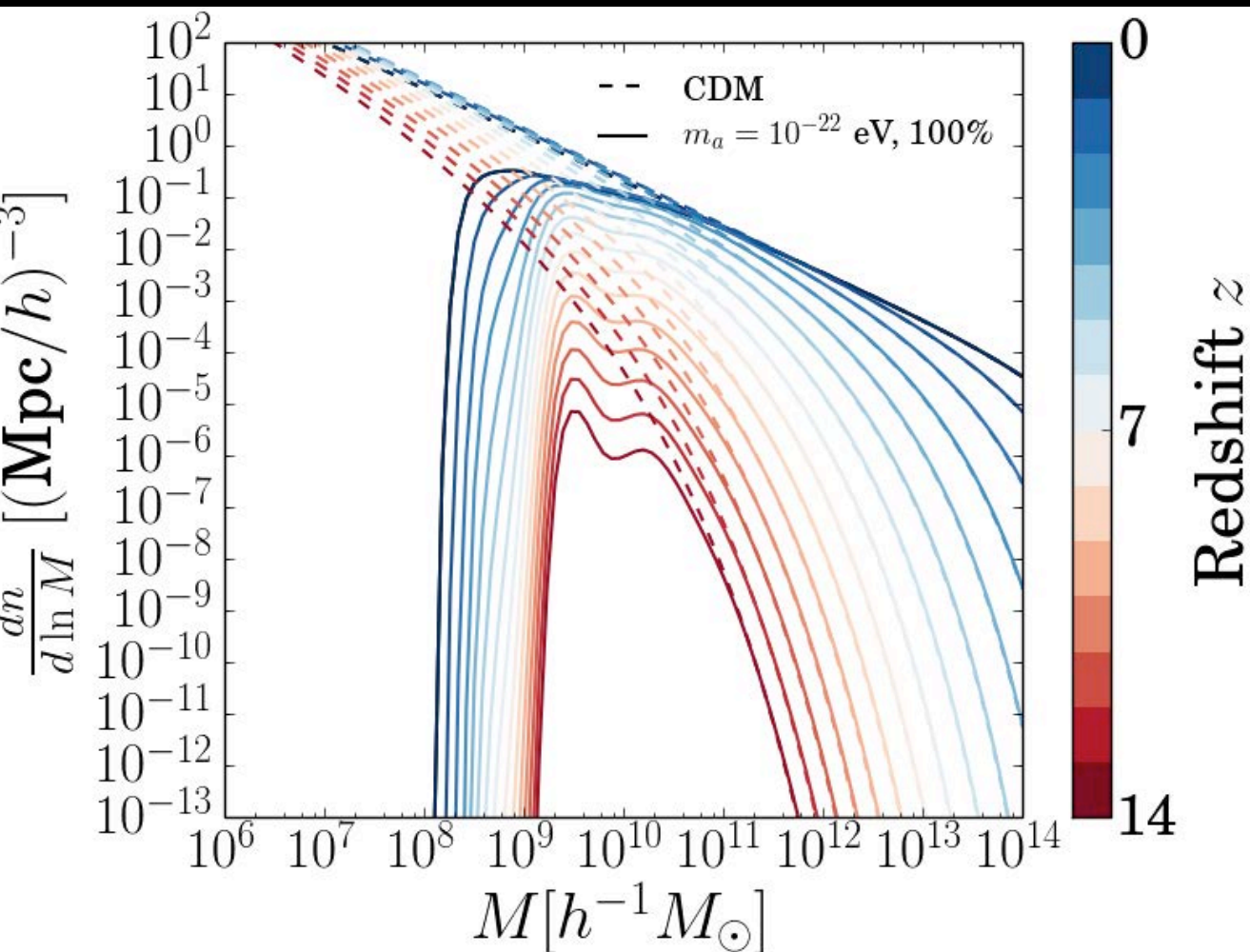
FUTURE WORK: ULAS CORES + CUSPS?



From Schive et al., more cosmological volume needed for statistics, baryons, etc...

FUTURE WORK: ULAS AND GALAXIES

Missing satellite problem?

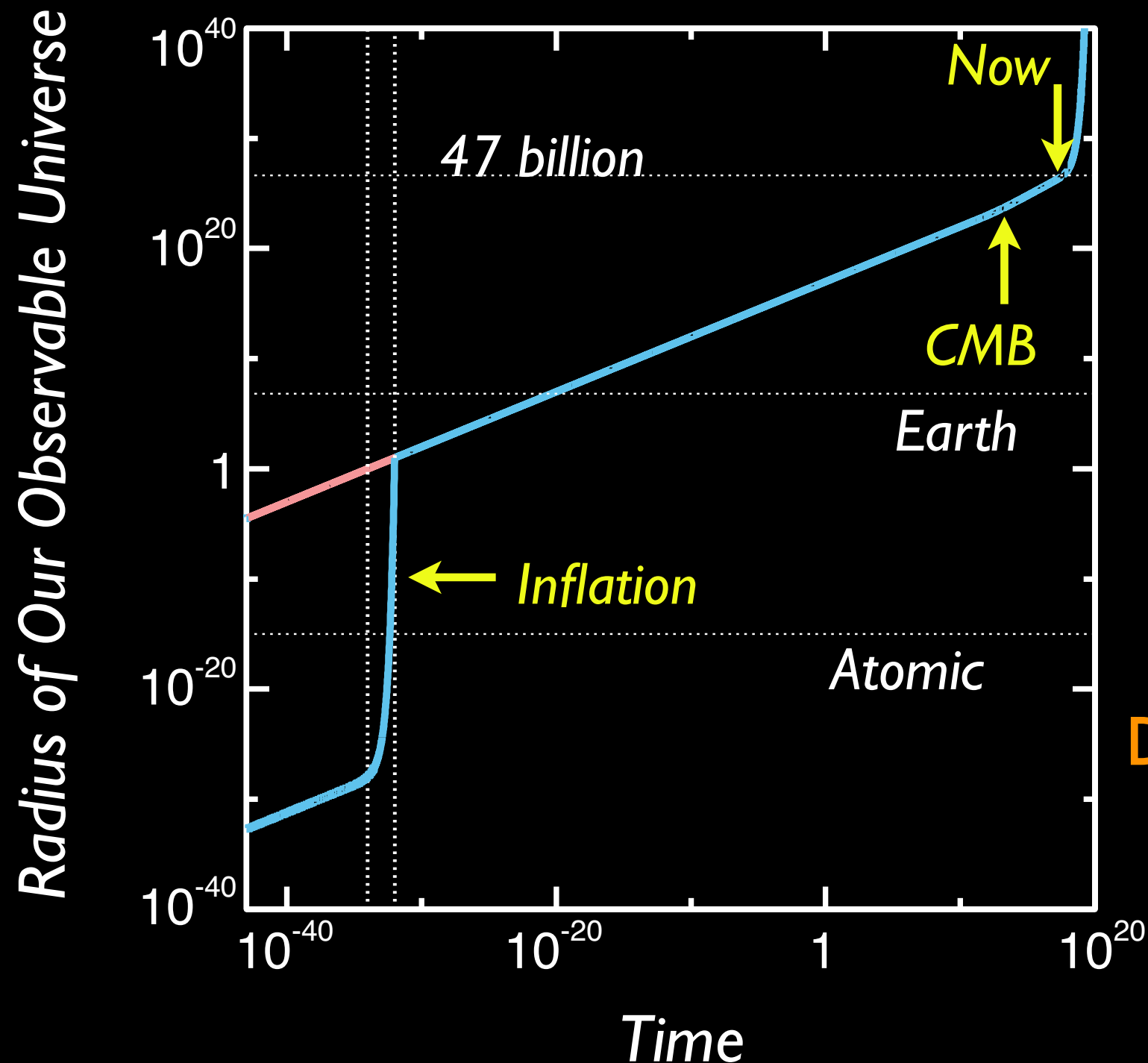


Marsh et al 2014, Klypin 1999, Bullock 2010

Dynamical friction, tidal disruption, substructure,
halo model, spherical collapse, better simulations
(much work to be done!)

AXIONS AND ISOCURVATURE FLUCTUATIONS

- * Inflation is an early epoch of accelerated expansion



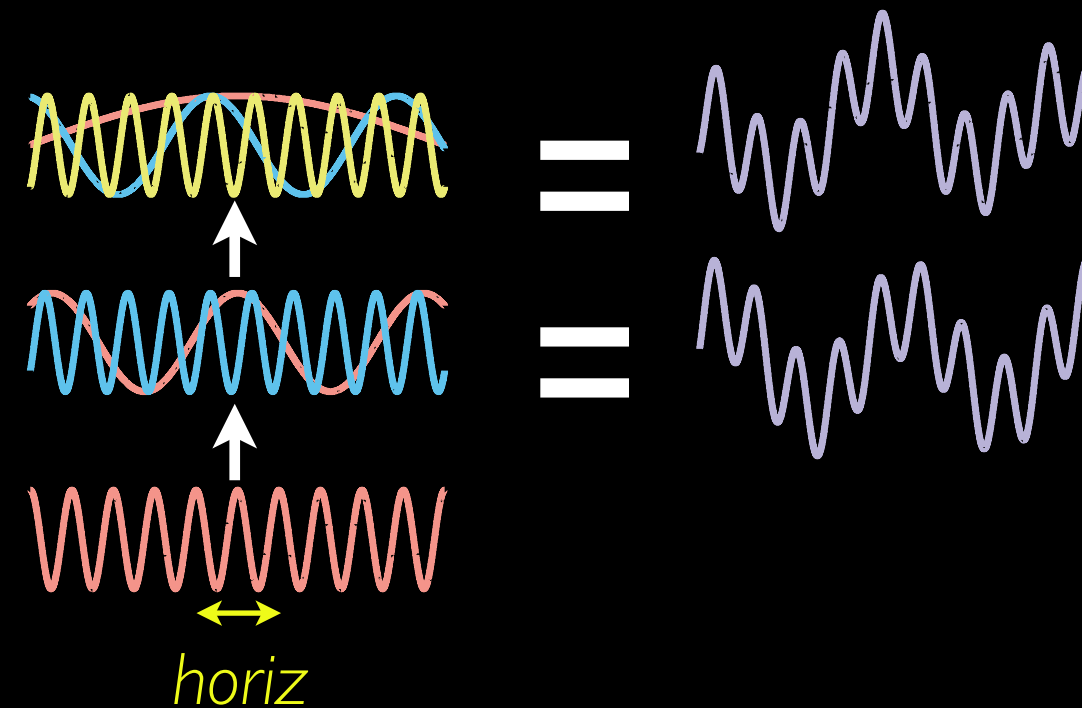
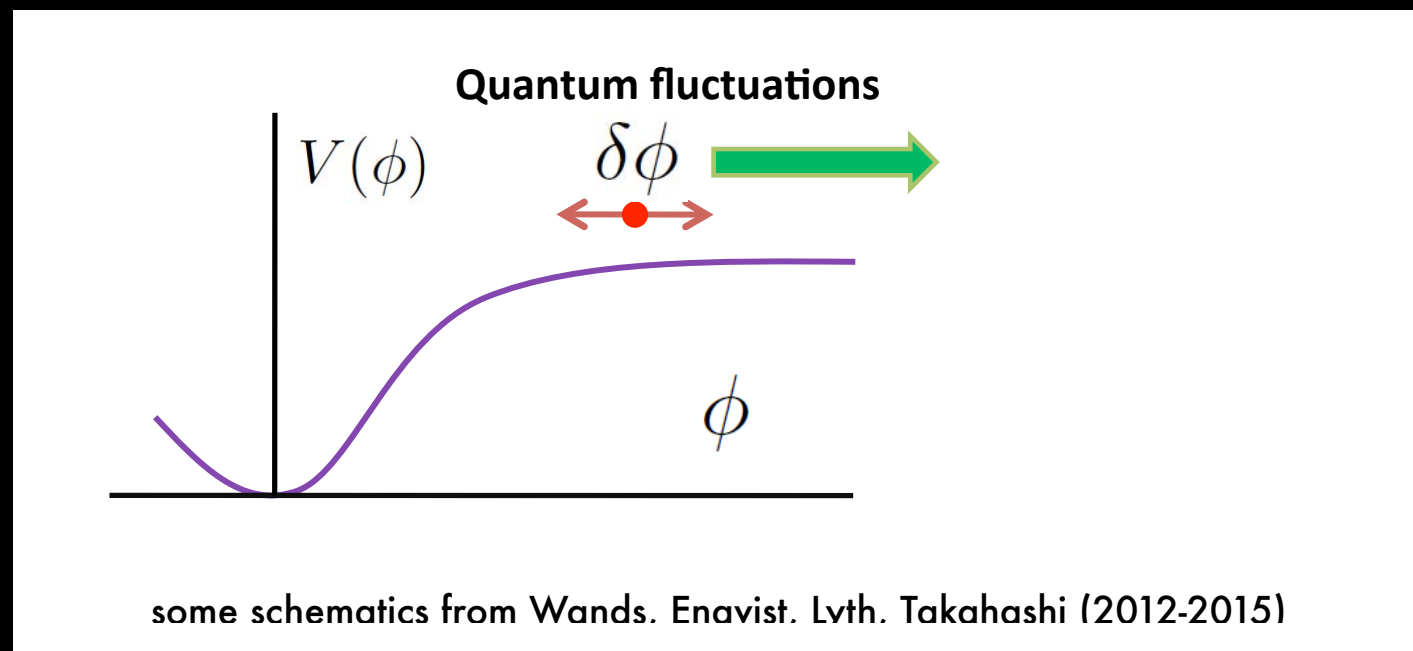
Hubble parameter

$$H_I = \text{?????}$$

Determined by energy scale

AXIONS AND ISOCURVATURE FLUCTUATIONS

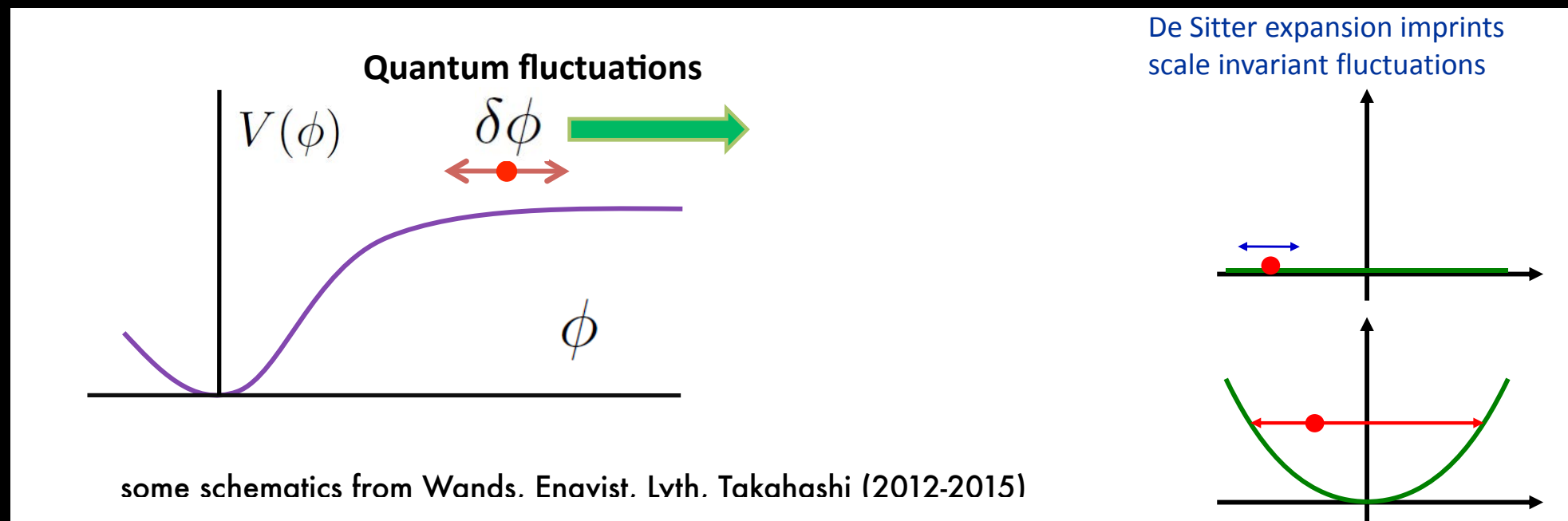
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Sets A_s and n_s

AXIONS AND ISOCURVATURE FLUCTUATIONS

✴ If $f_a > H_I$



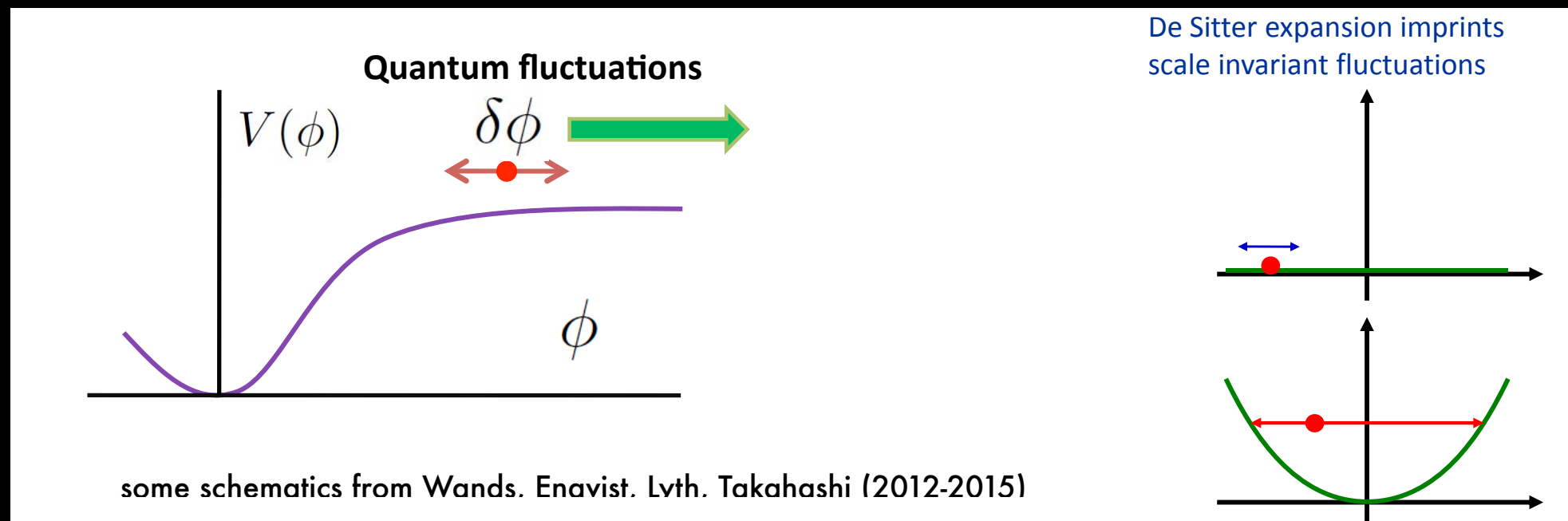
$$\sqrt{\langle a^2 \rangle} = \frac{H_I}{2\pi}$$

Quantum zero-point fluctuations!

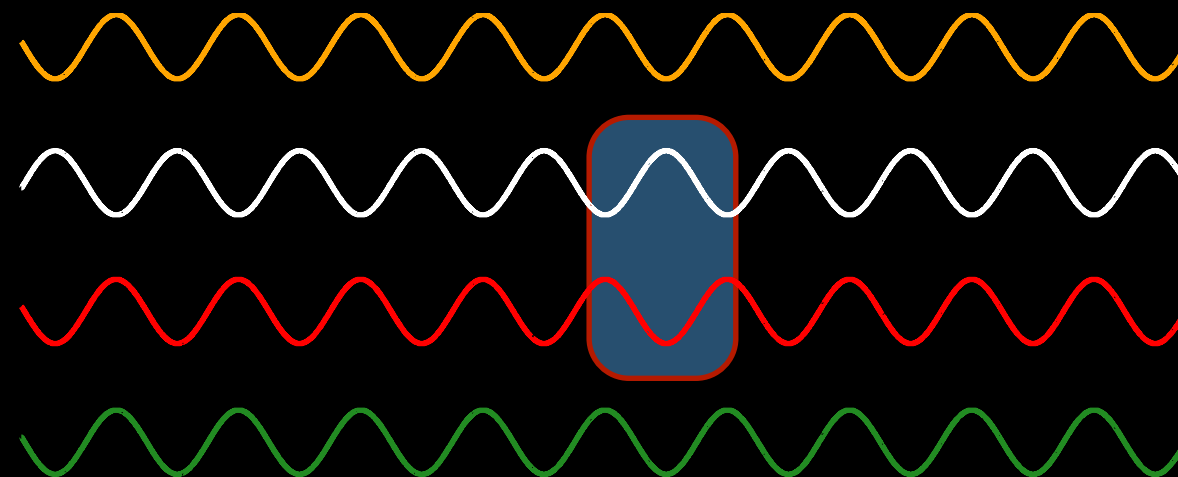
$$\rho_a \ll \rho_{\text{tot}} \rightarrow \Phi_a \ll 10^{-5}$$

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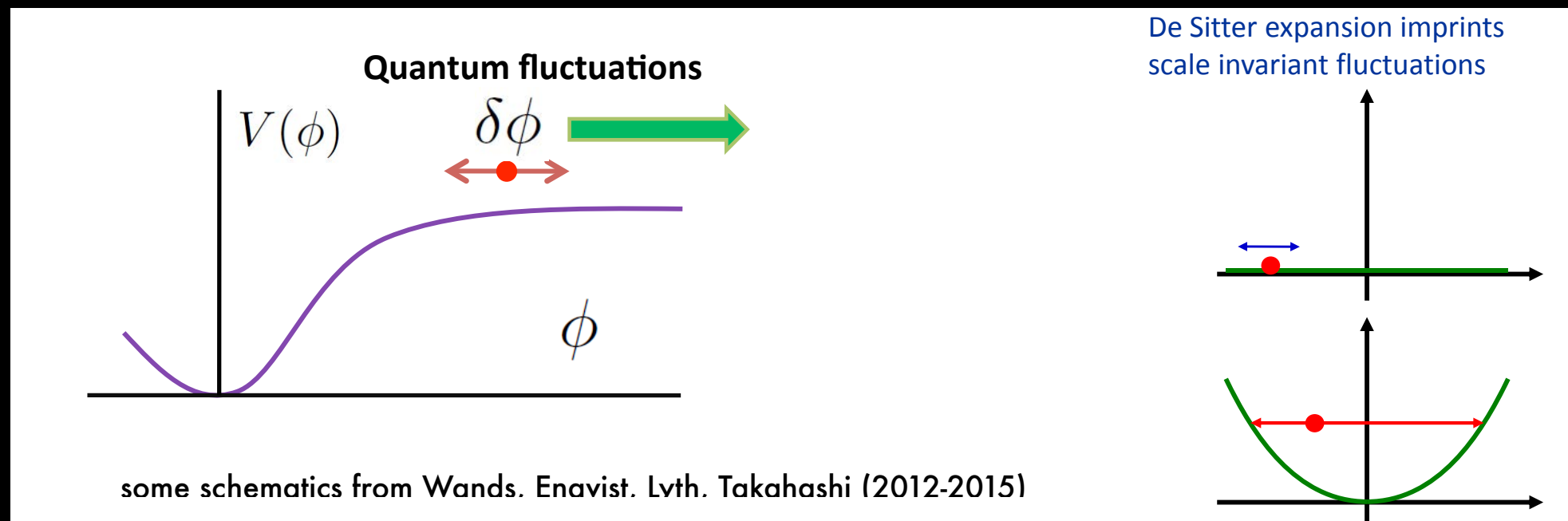
CDM
isocurvature



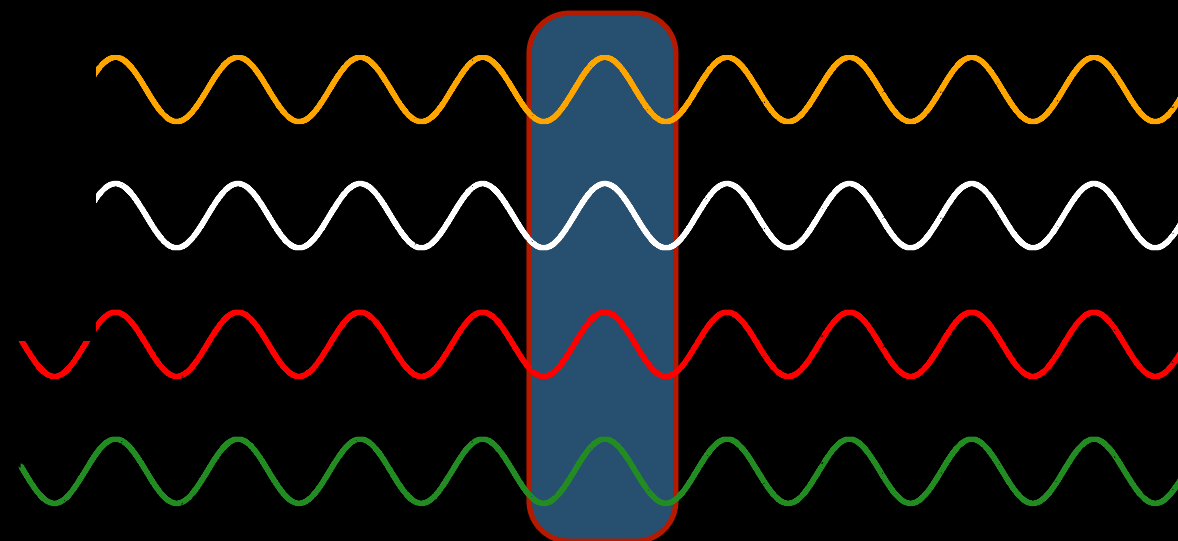
Neutrinos
CDM
Photons
Baryons

AXIONS AND ISOCURVATURE FLUCTUATIONS

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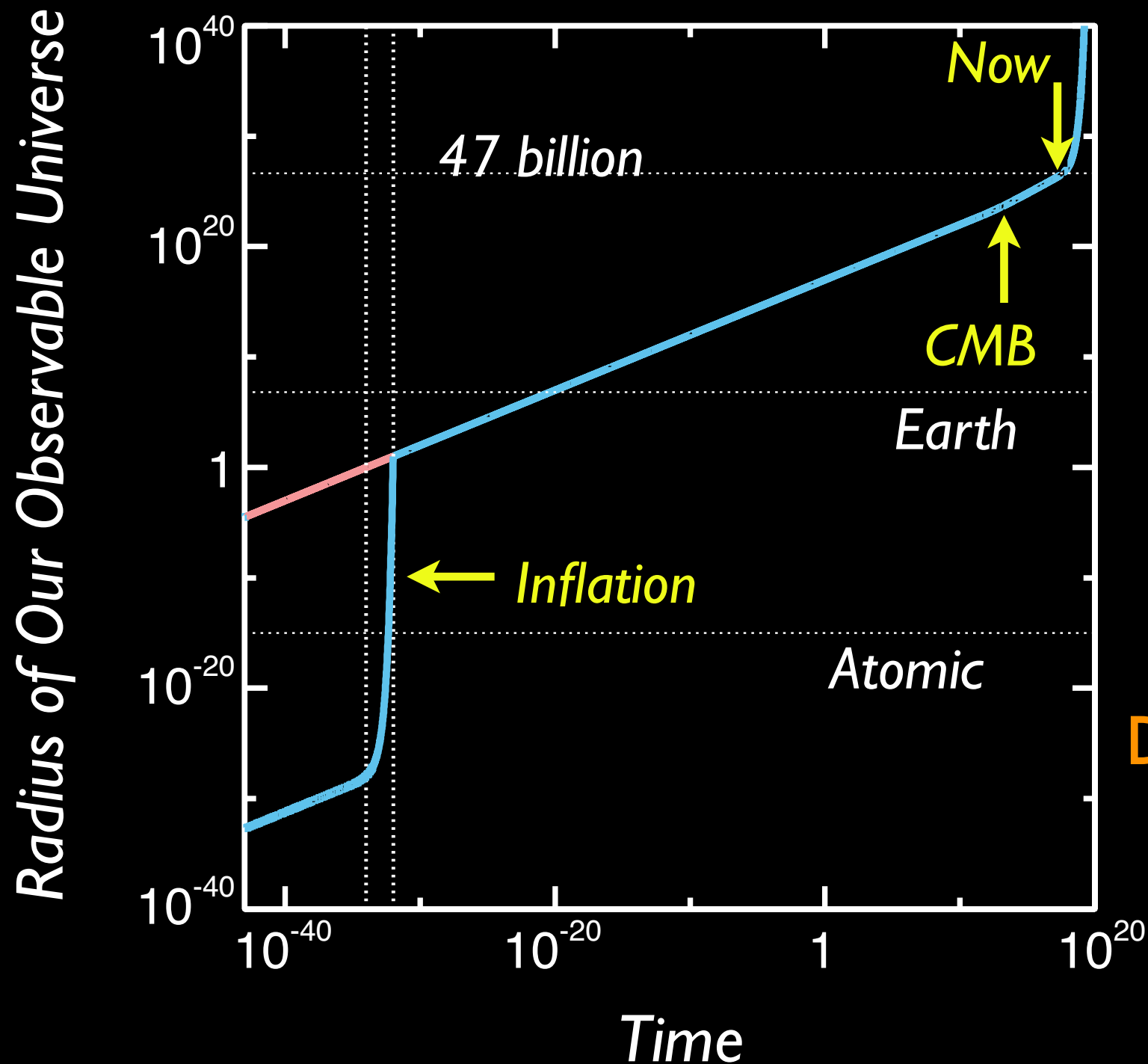


Total density
fluctuation



AXIONS AND ISOCURVATURE FLUCTUATIONS

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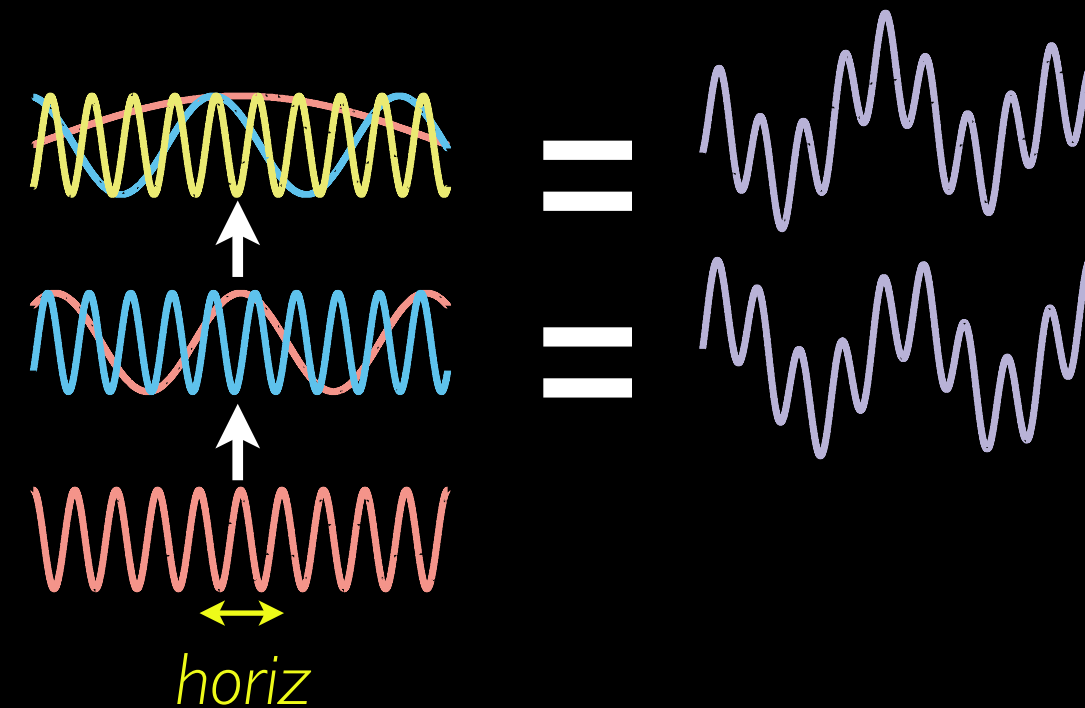
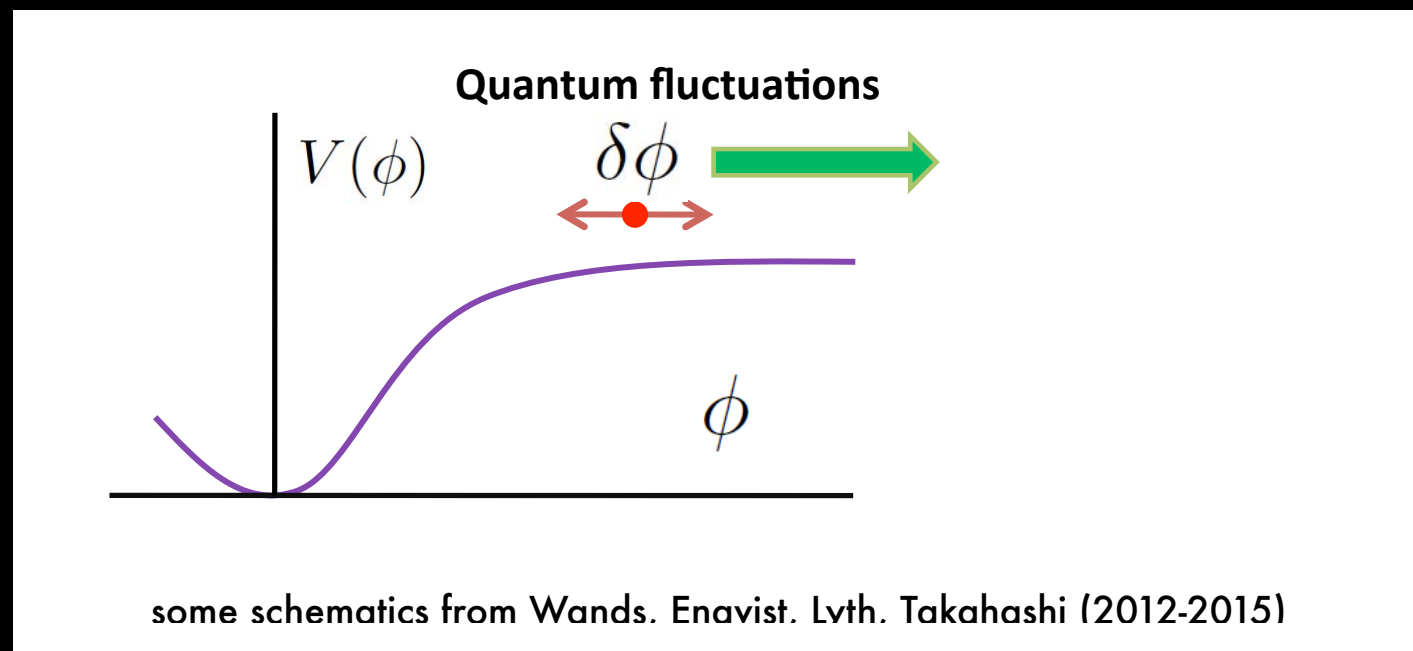
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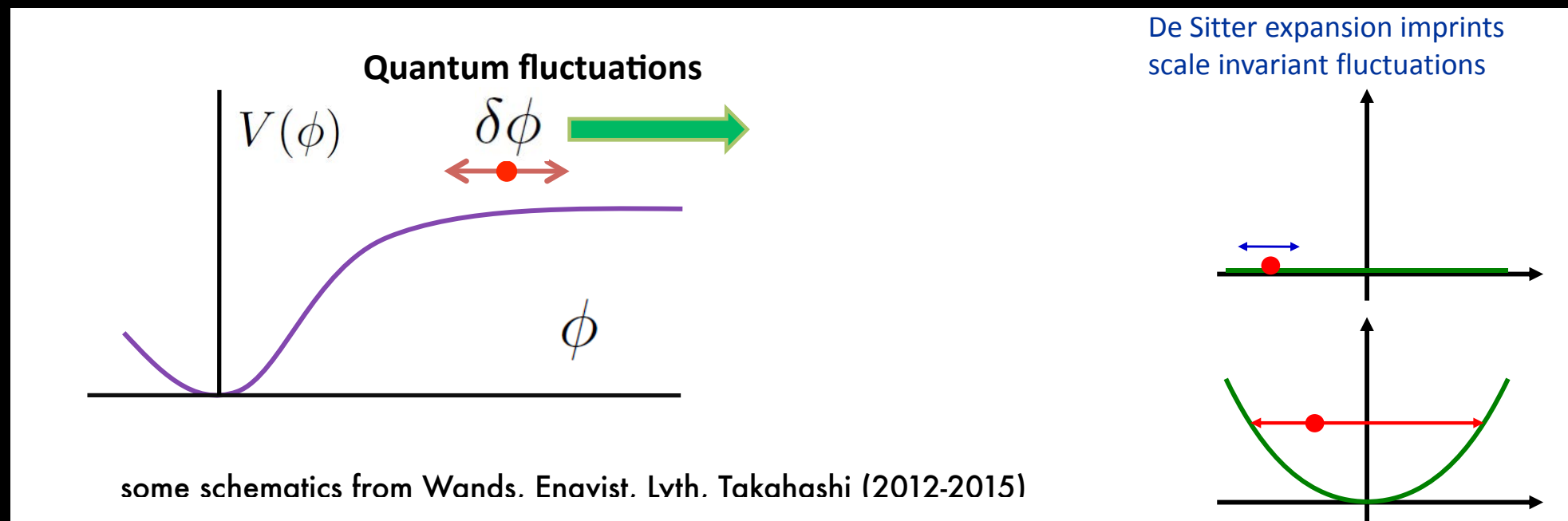
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Sets A_s and n_s

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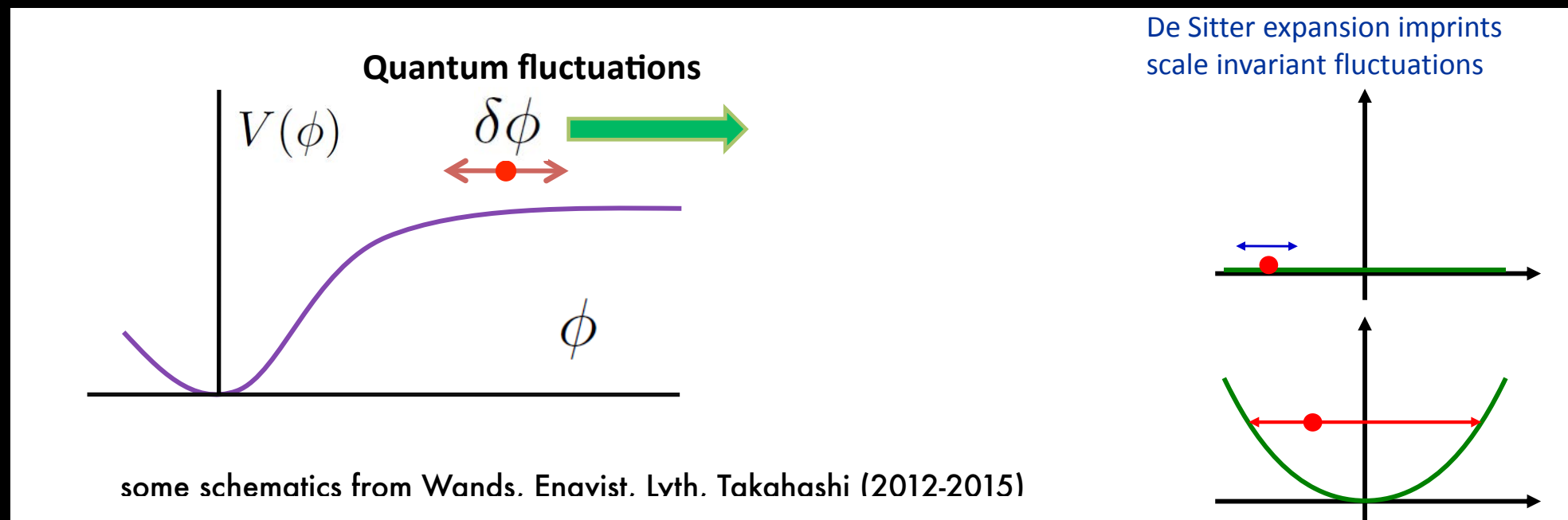
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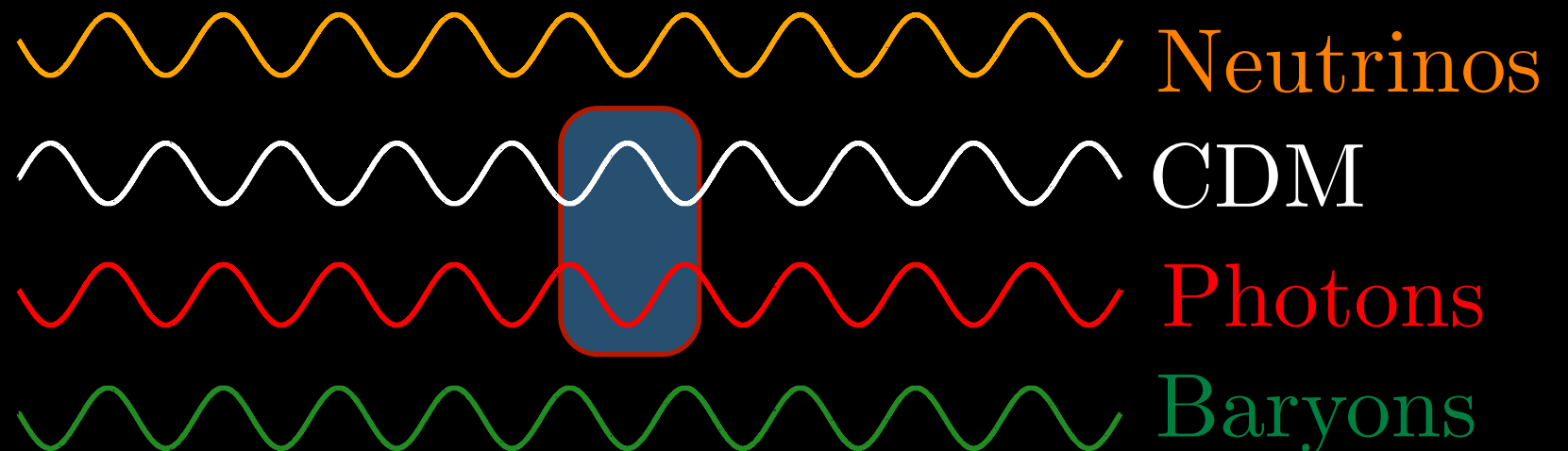
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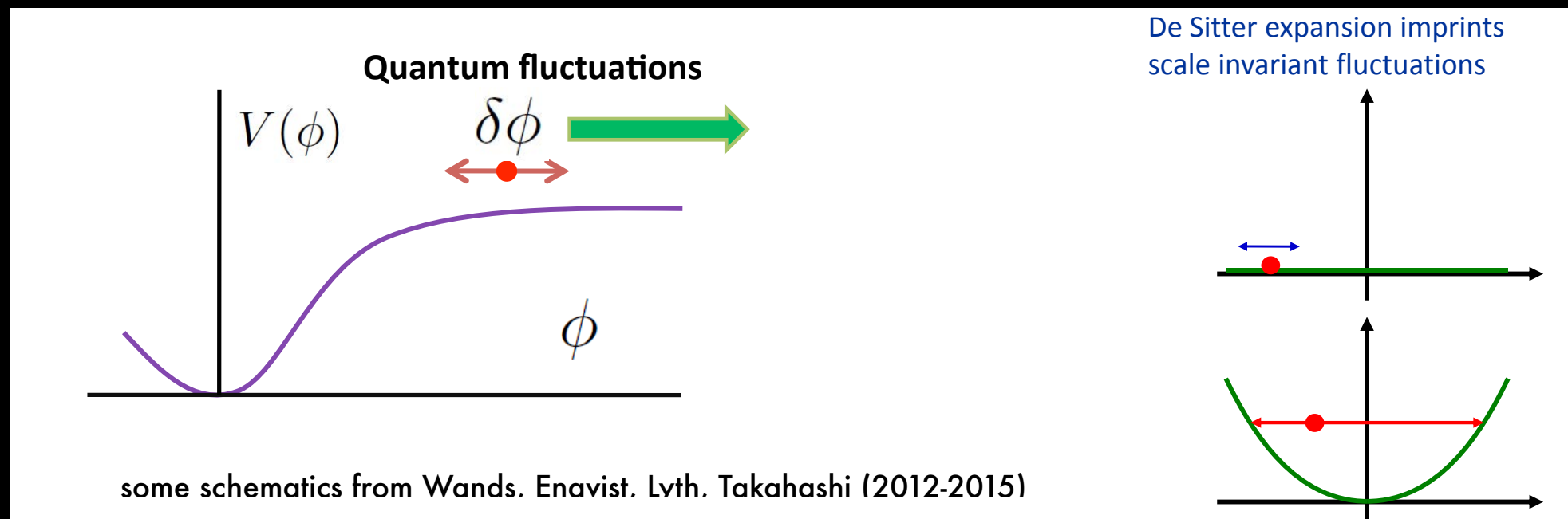


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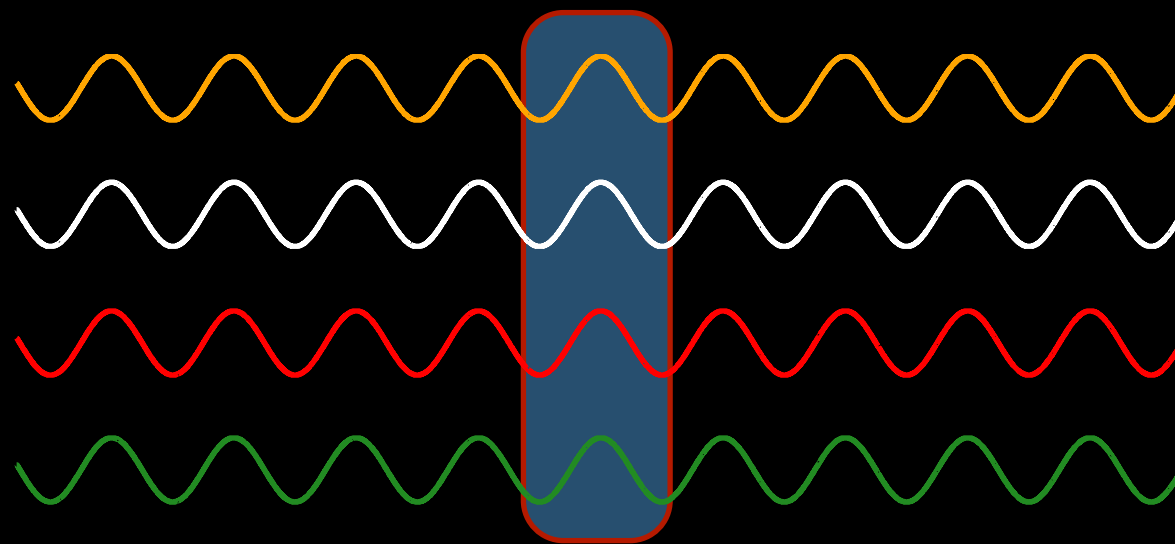


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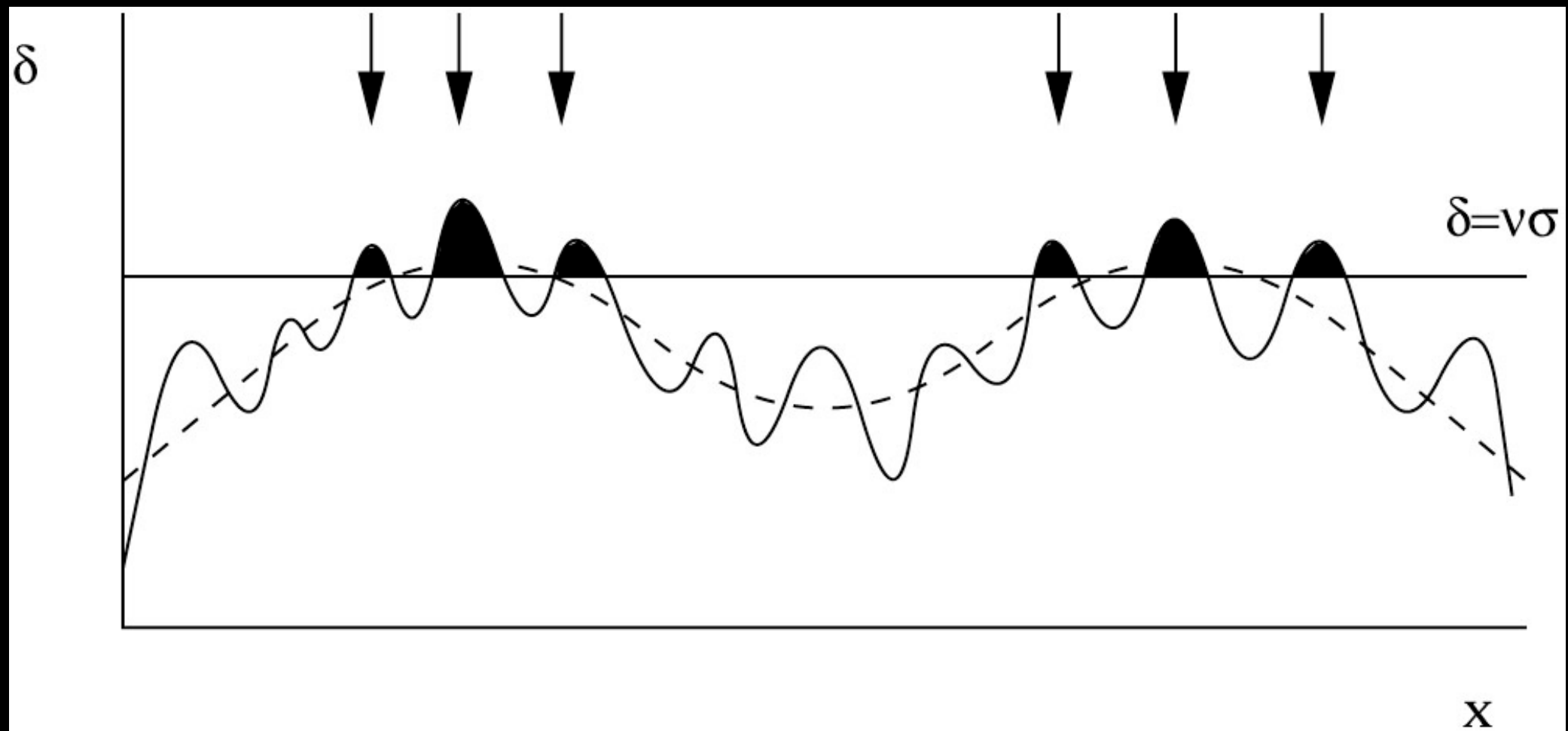
Adiabatic
Total density
fluctuation



Additional slides:
ULAs and galaxies

FUTURE WORK: ULAS AND GALAXIES

*Galaxies are biased tracers



*Galaxies are biased tracers

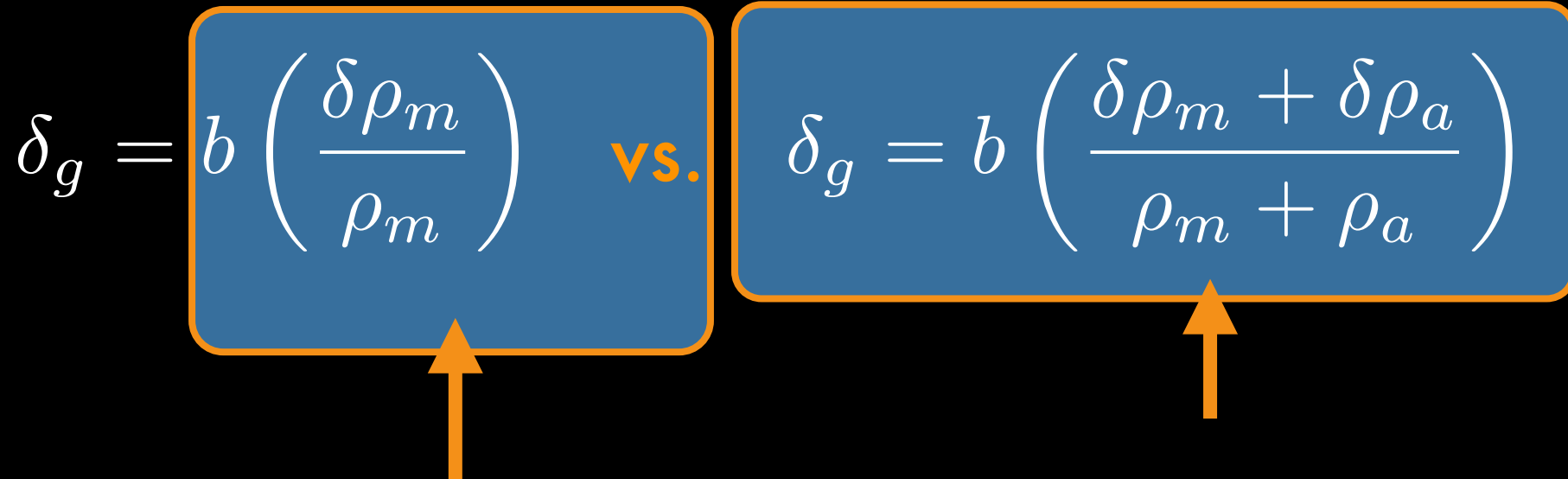
$$\delta_g = b \left(\frac{\delta\rho_m}{\rho_m} \right)$$

vs.

$$\delta_g = b \left(\frac{\delta\rho_m + \delta\rho_a}{\rho_m + \rho_a} \right)$$

↑
Unfair penalty on scales where
axions don't cluster

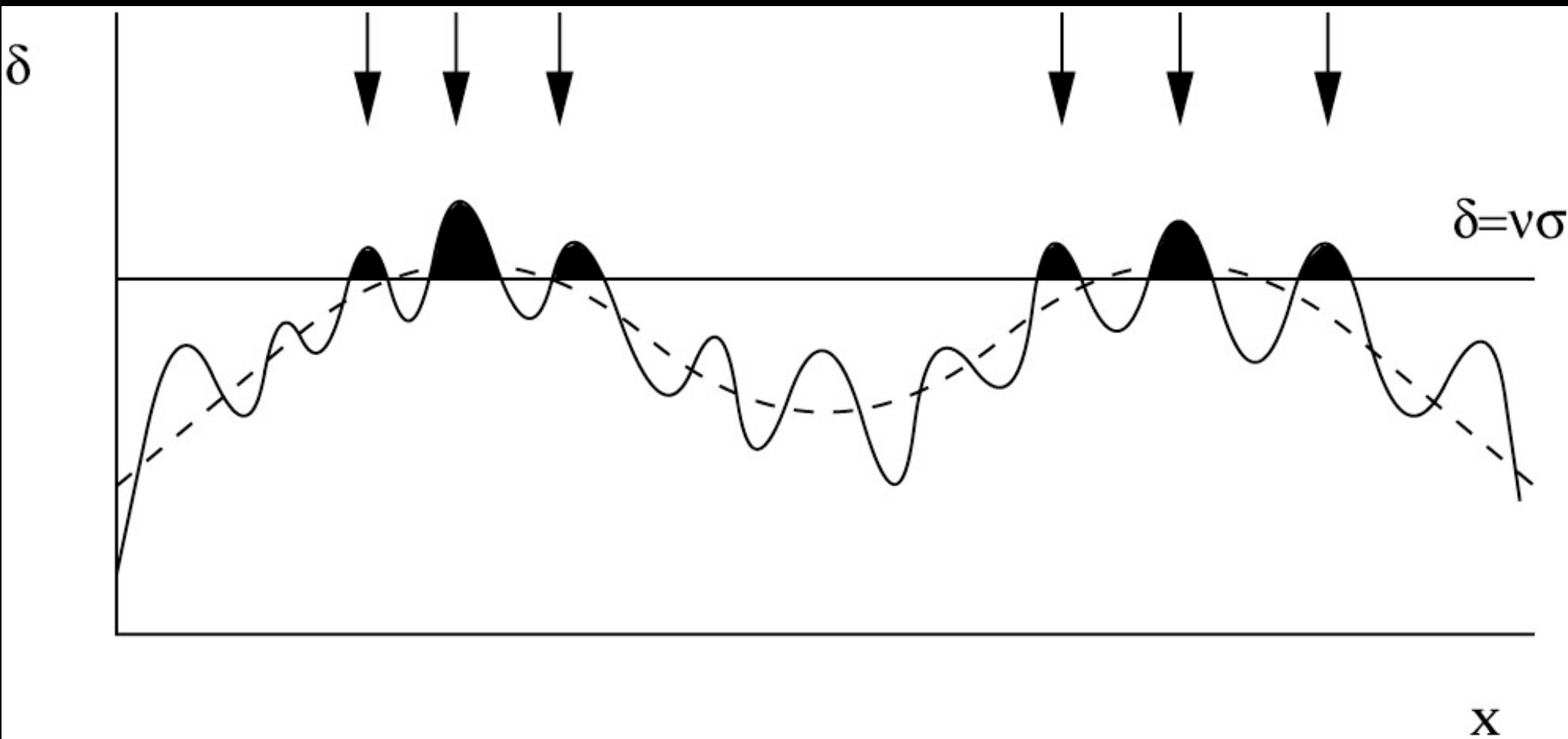
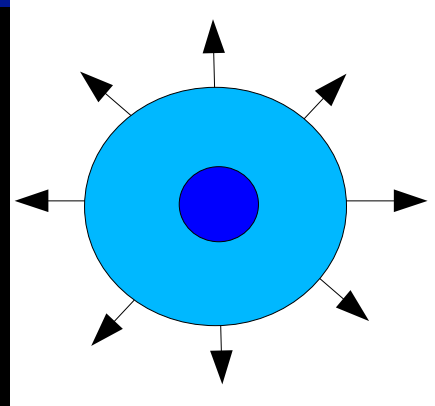
*Galaxies are biased tracers

$$\delta_g = b \left(\frac{\delta\rho_m}{\rho_m} \right) \quad \text{vs.} \quad \delta_g = b \left(\frac{\delta\rho_m + \delta\rho_a}{\rho_m + \rho_a} \right)$$


Doesn't include ULAs as matter component
on scales where they cluster

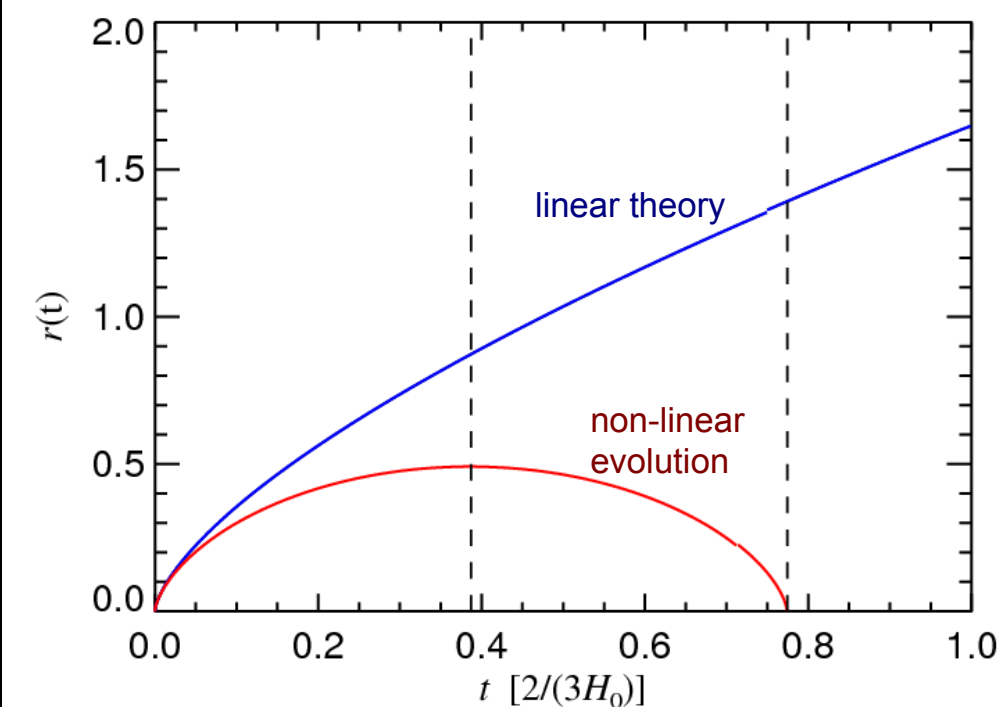
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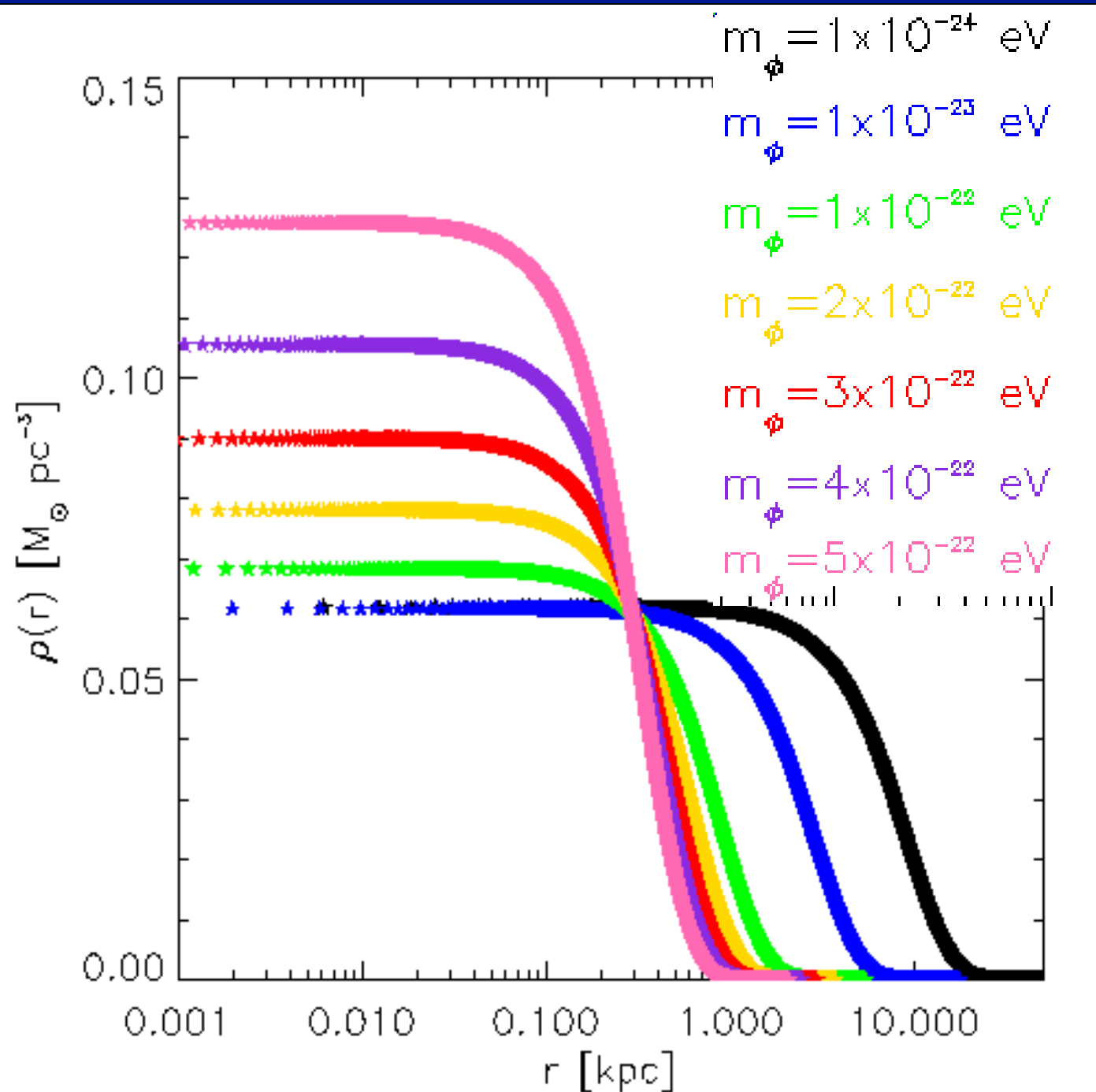


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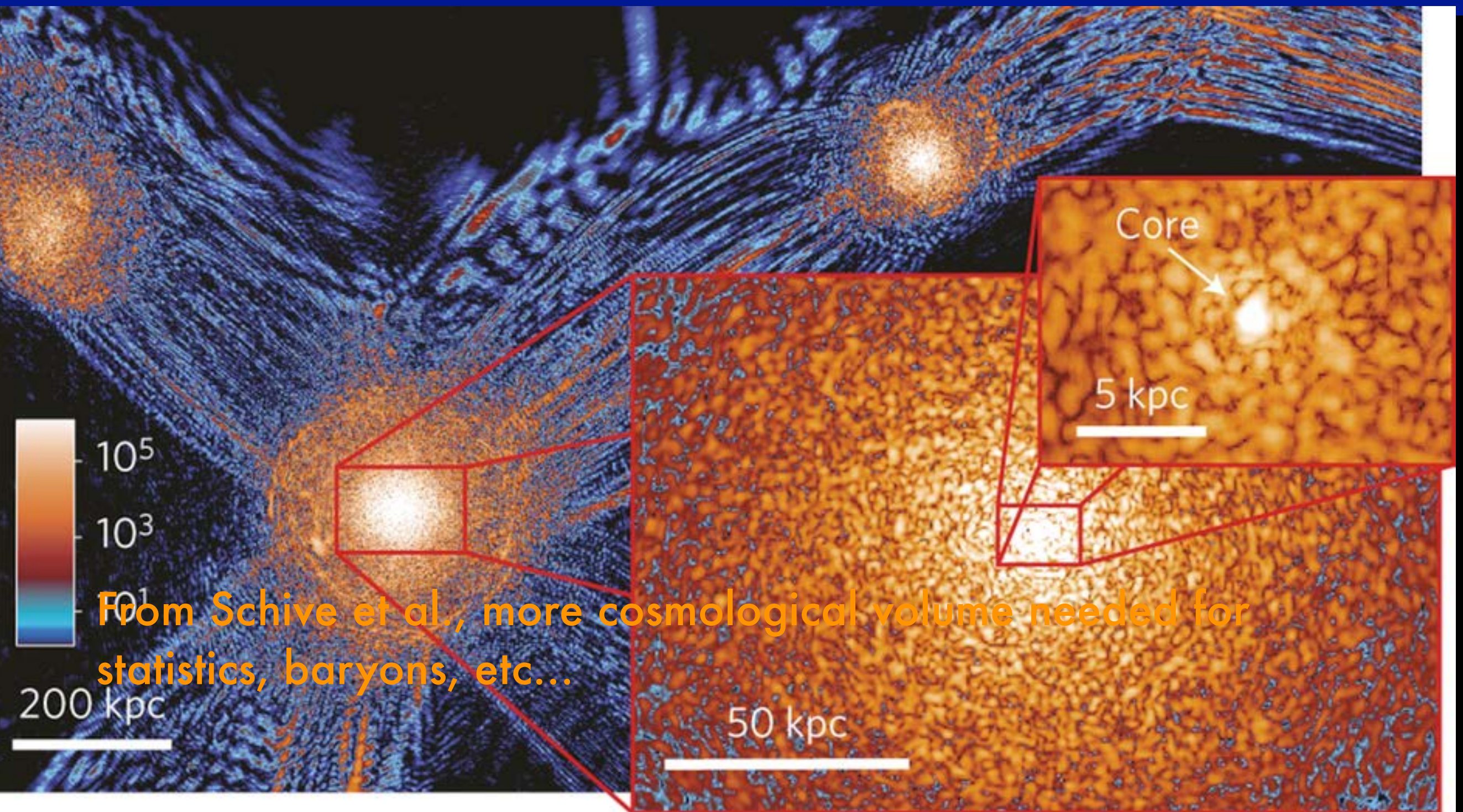


FUTURE WORK: ULAS CORES + CUSPS?



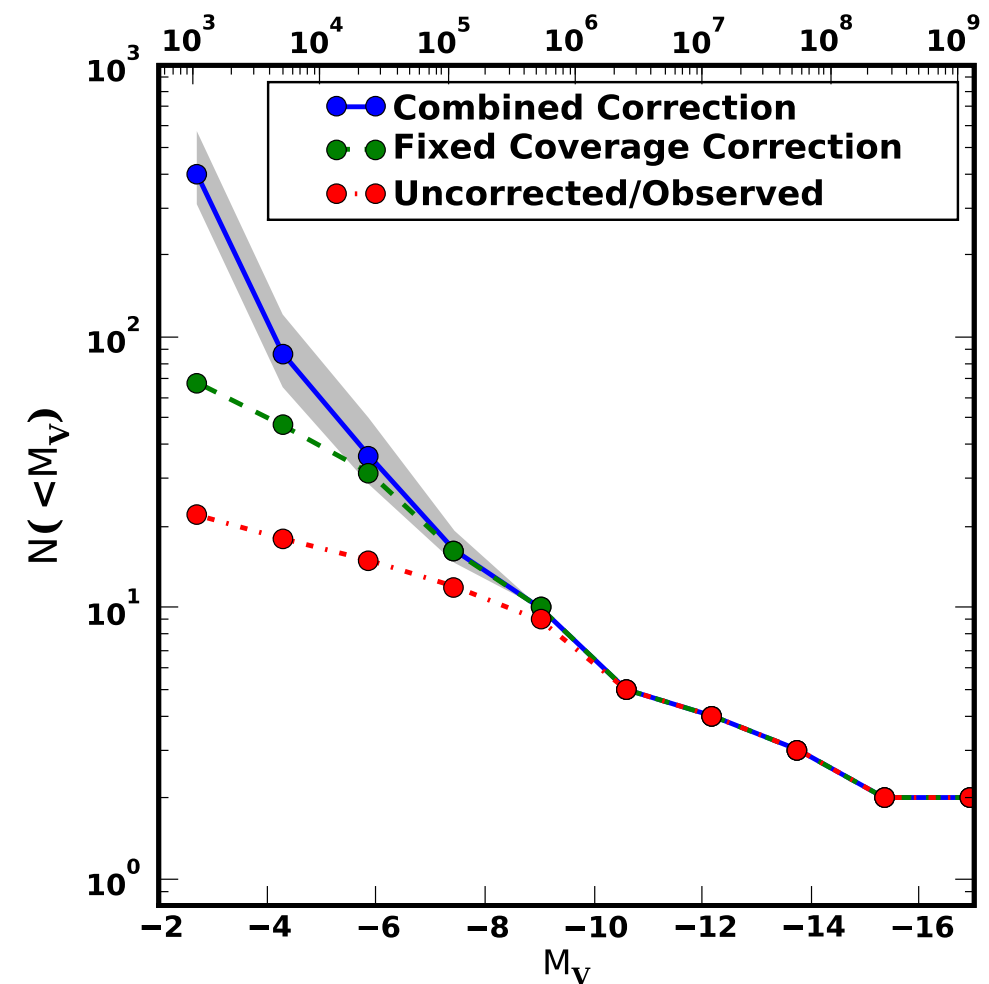
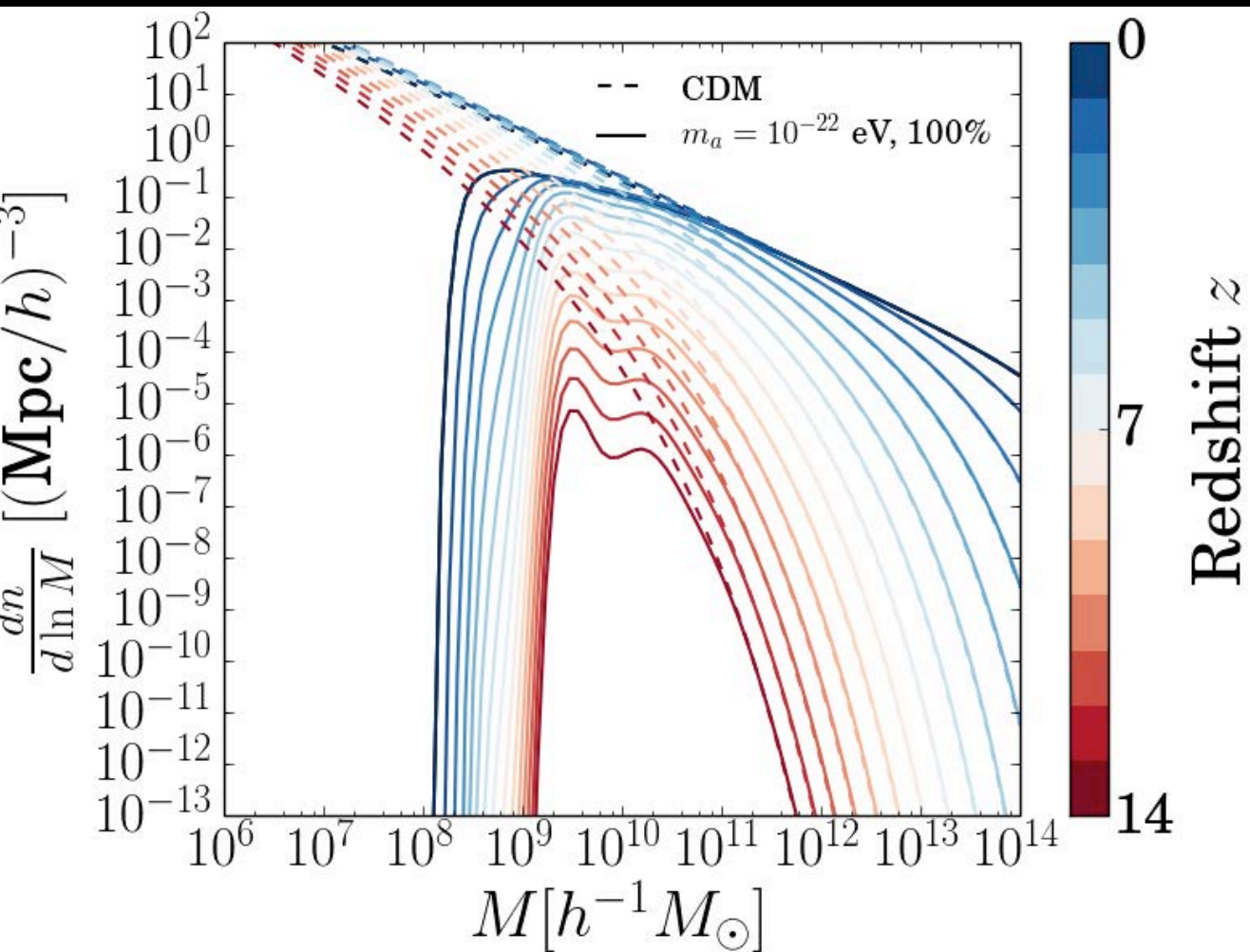
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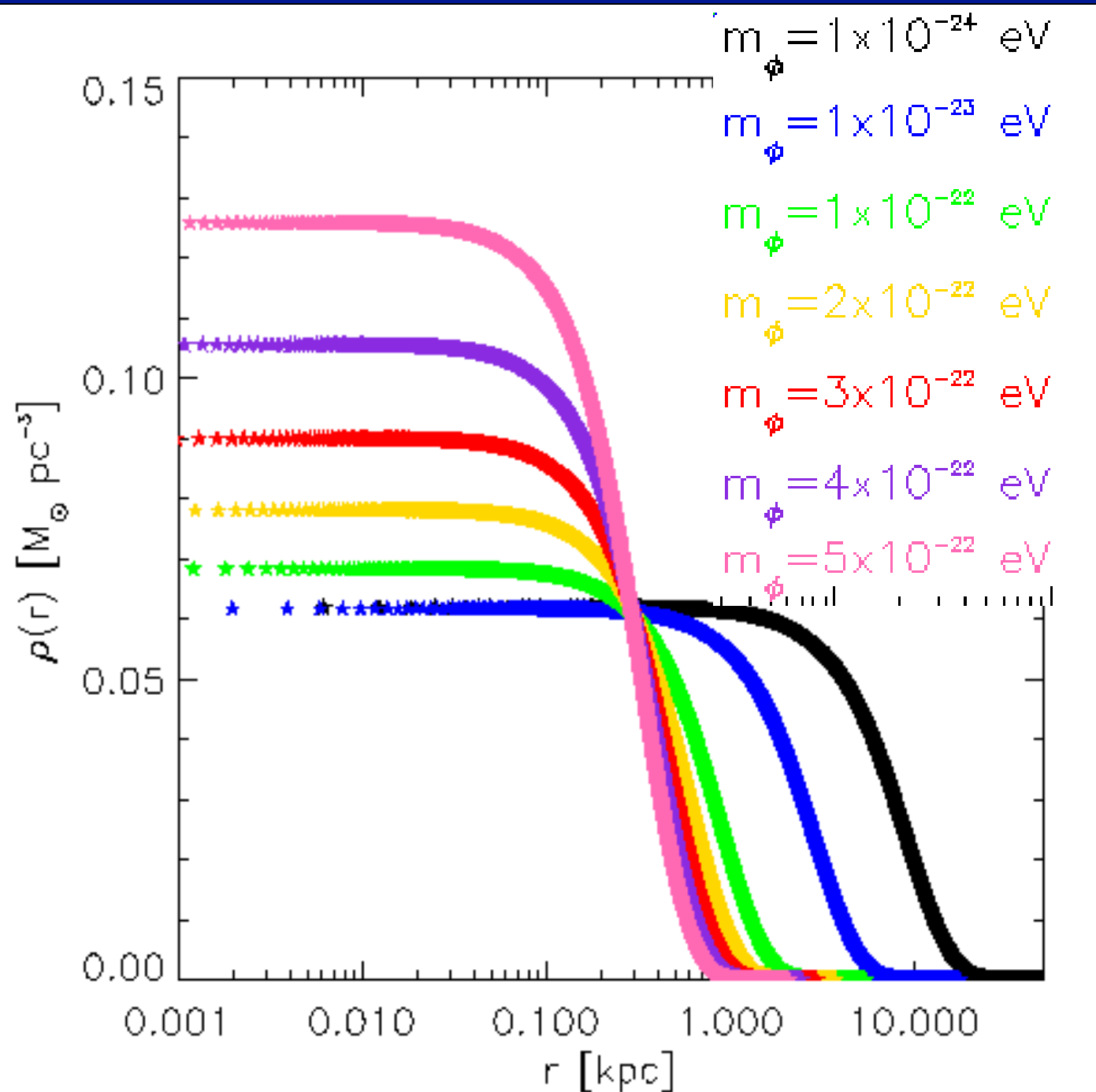
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Missing satellite problem?



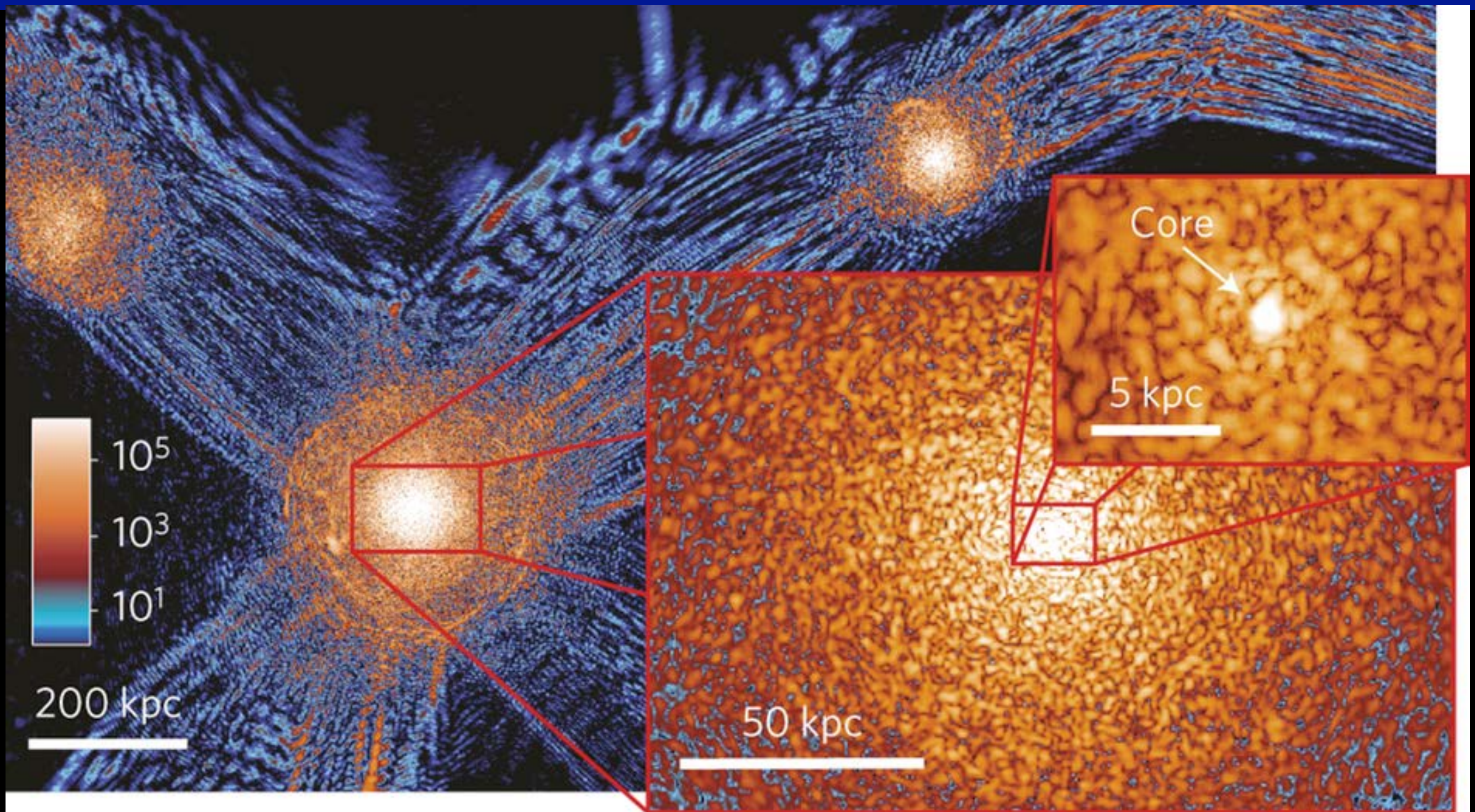
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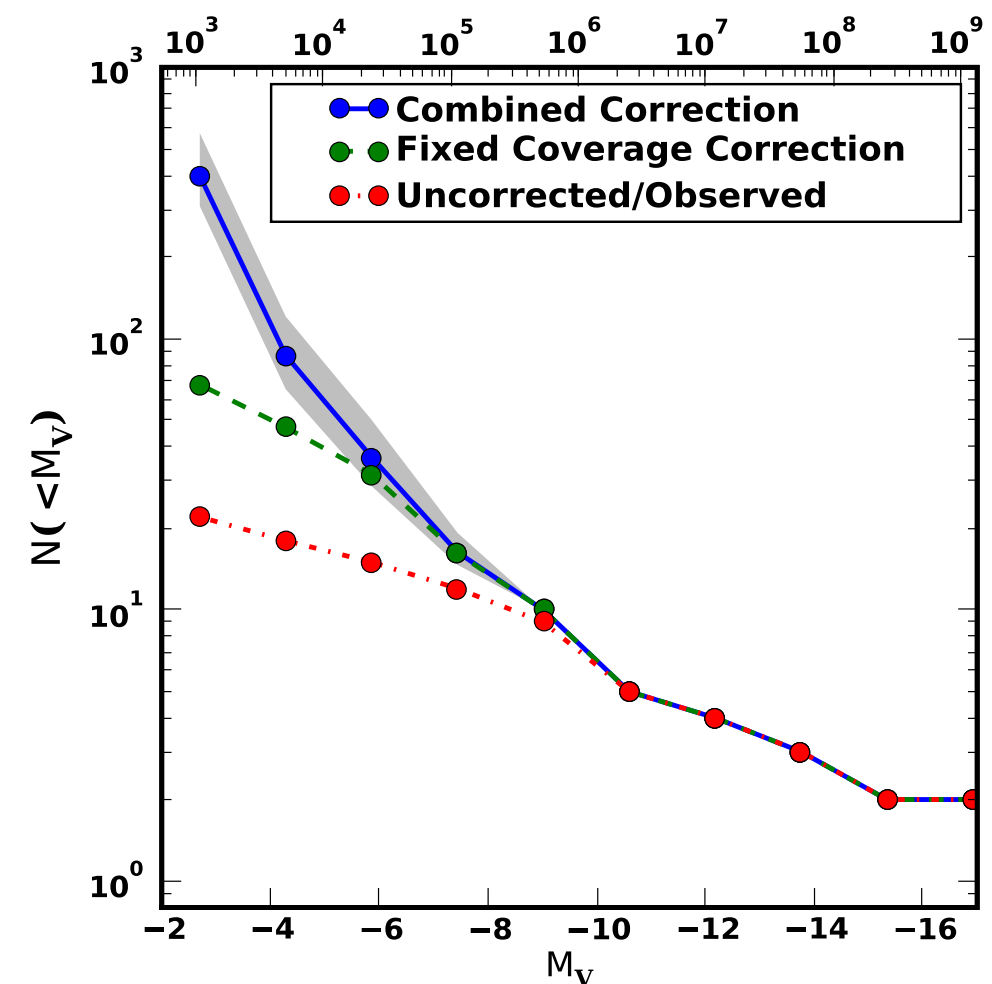
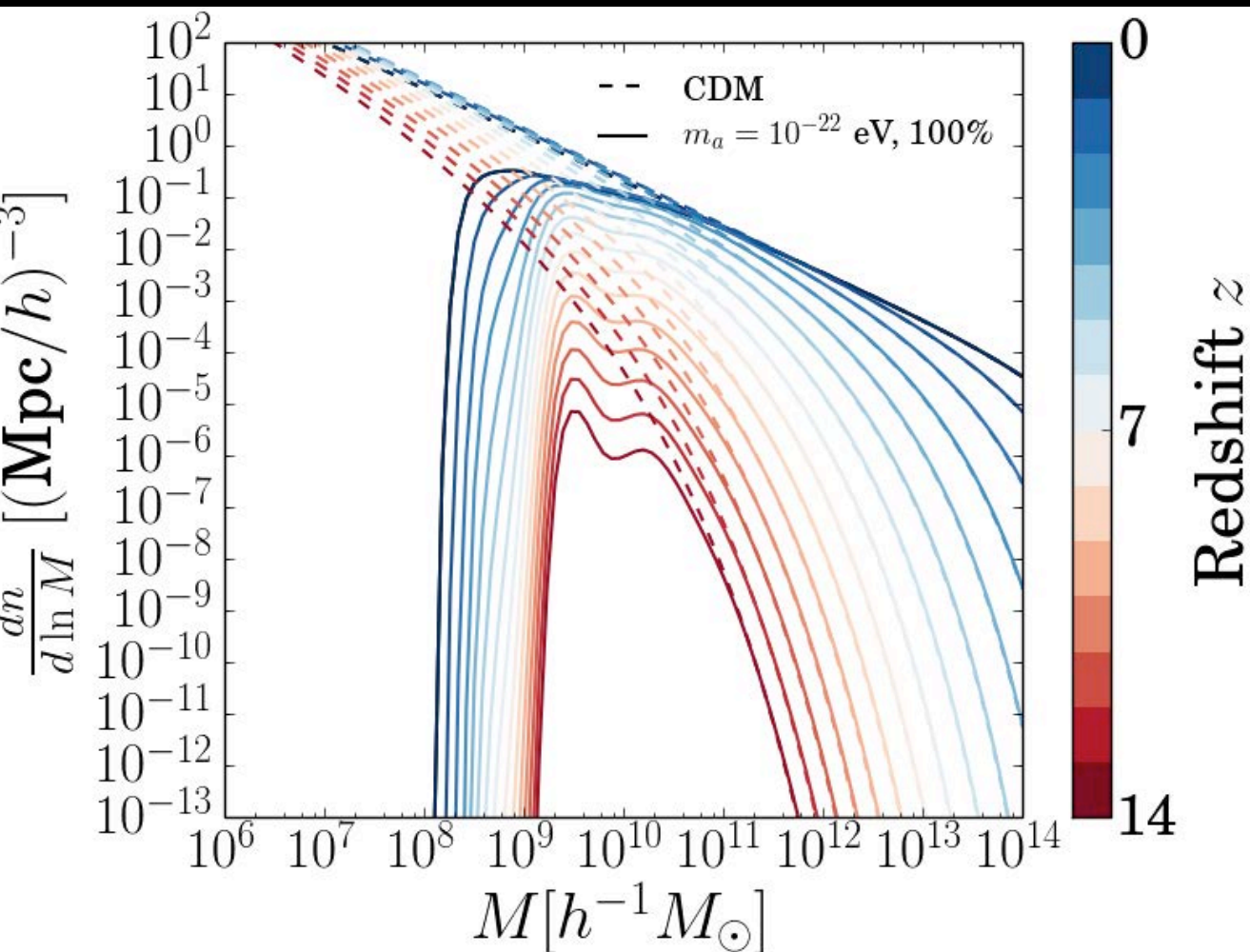
FUTURE WORK: ULAS CORES + CUSPS?



From Schive et al., more cosmological volume needed for statistics, baryons, etc...

FUTURE WORK: ULAS AND GALAXIES

Missing satellite problem?



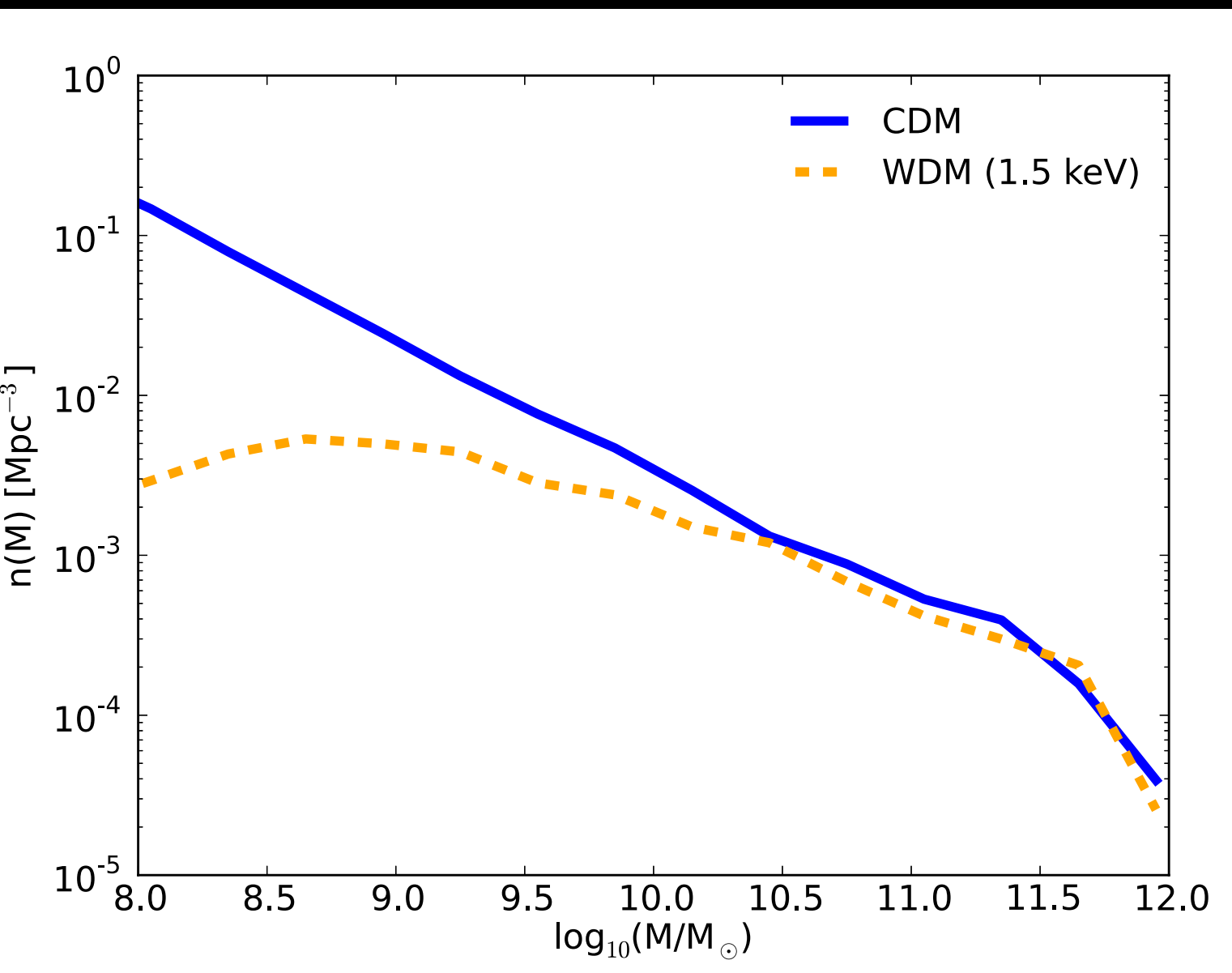
Marsh et al 2014, Klypin 1999, Bullock 2010

Dynamical friction, tidal disruption, substructure,
halo model, spherical collapse, better simulations
(much work to be done!)

FUTURE WORK: ULAS AND GALAXIES

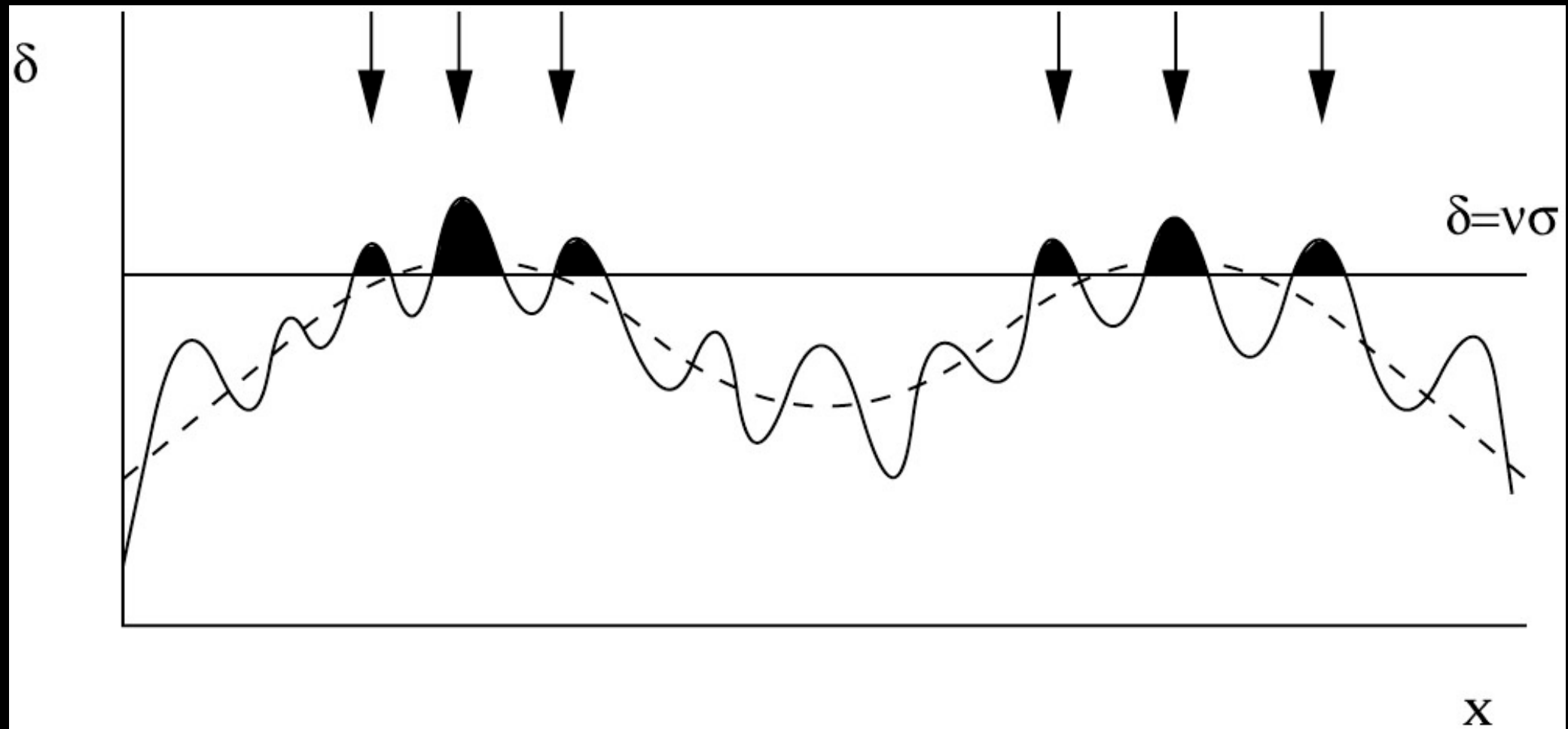
- * Galaxy correlation function (counts, bias)
- * Galaxy lensing
- * Substructure in halos [flux ratio anomalies in multiply lensed]

ULA substructure?



FUTURE WORK: ULAS AND GALAXIES

*Galaxies are biased tracers



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$$\delta_g = b \left(\frac{\delta\rho_m}{\rho_m} \right) \quad \text{vs.} \quad \delta_g = b \left(\frac{\delta\rho_m + \delta\rho_a}{\rho_m + \rho_a} \right)$$

*Galaxies are biased tracers

$$\delta_g = b \left(\frac{\delta\rho_m}{\rho_m} \right)$$

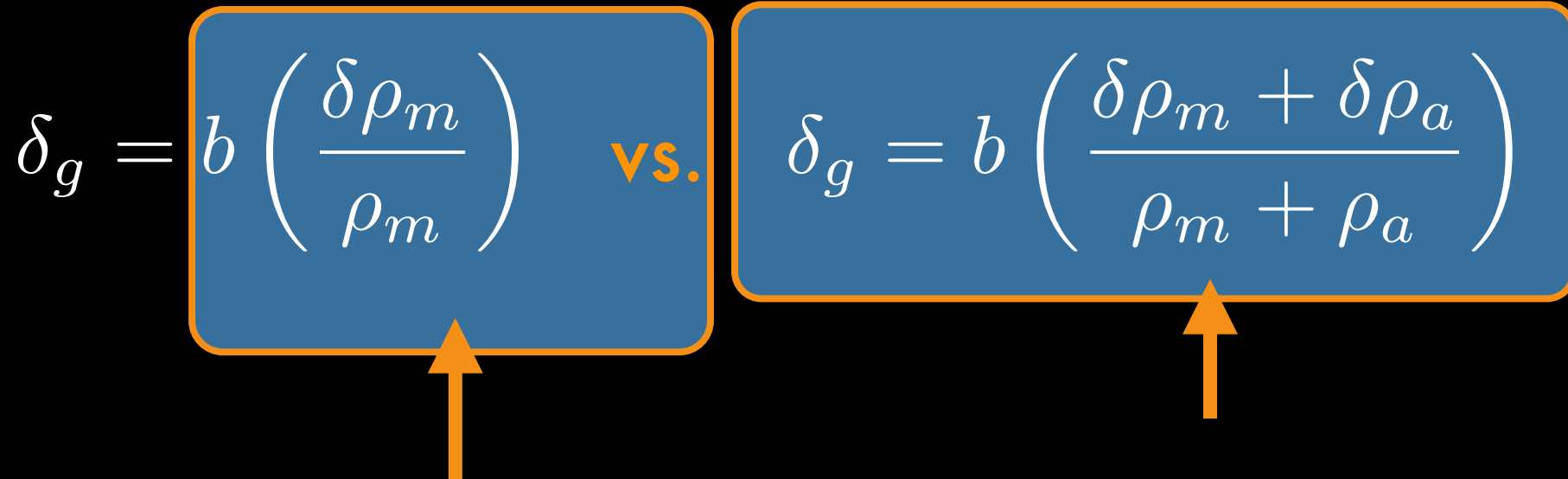
vs.

$$\delta_g = b \left(\frac{\delta\rho_m + \delta\rho_a}{\rho_m + \rho_a} \right)$$

Unfair penalty on scales where
axions don't cluster

*We use hard switch at $k_{osc} = k_{eq}$; $k_{osc} \equiv a_{osc}H_{osc}$

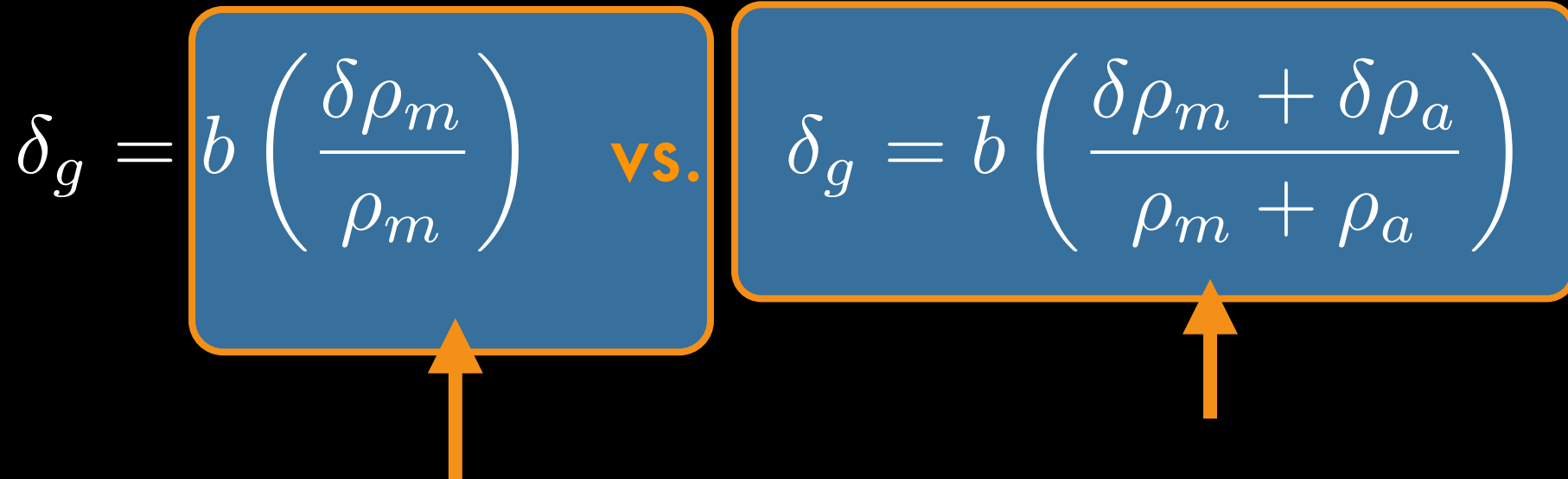
*Galaxies are biased tracers

$$\delta_g = b \left(\frac{\delta\rho_m}{\rho_m} \right) \quad \text{vs.} \quad \delta_g = b \left(\frac{\delta\rho_m + \delta\rho_a}{\rho_m + \rho_a} \right)$$


Doesn't include ULAs as matter component
on scales where they cluster

*We use hard switch at $k_{osc} = k_{eq}$; $k_{osc} \equiv a_{osc}H_{osc}$

- *Galaxies are biased tracers

$$\delta_g = b \left(\frac{\delta\rho_m}{\rho_m} \right) \quad \text{vs.} \quad \delta_g = b \left(\frac{\delta\rho_m + \delta\rho_a}{\rho_m + \rho_a} \right)$$


Doesn't include ULAs as matter component
on scales where they cluster

- *We use hard switch at $k_{osc} = k_{eq}$; $k_{osc} \equiv a_{osc}H_{osc}$
- *Realistic [smooth] treatment of scale-dependent bias needed (incorporating physics of ULA formation in halos)
 - *Often neglected (but shouldn't be) for neutrinos (LoVerde 2013)