

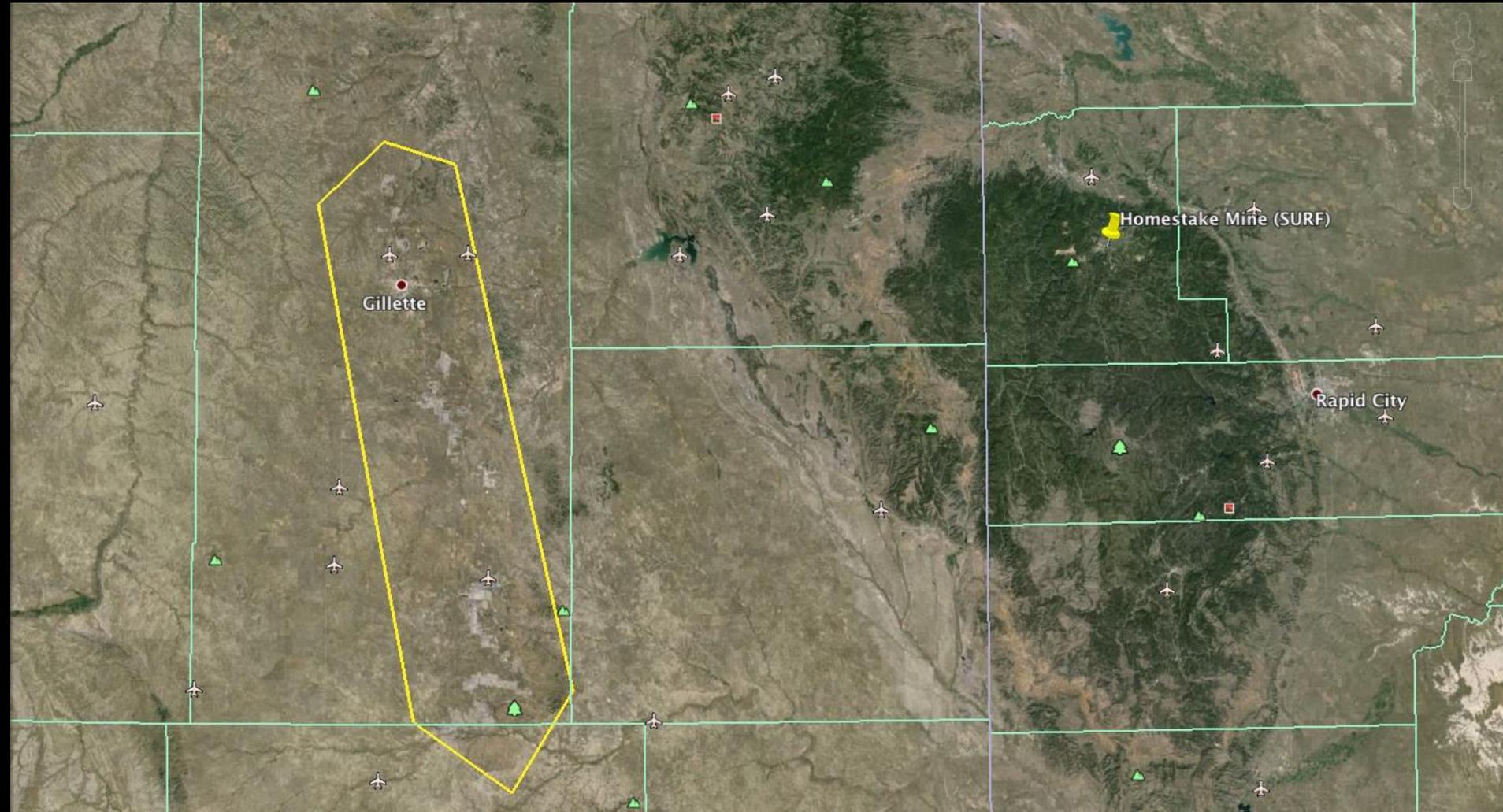
# Dispersion of Surface Waves in the Black Hills, SD

Presented by Ross Caton

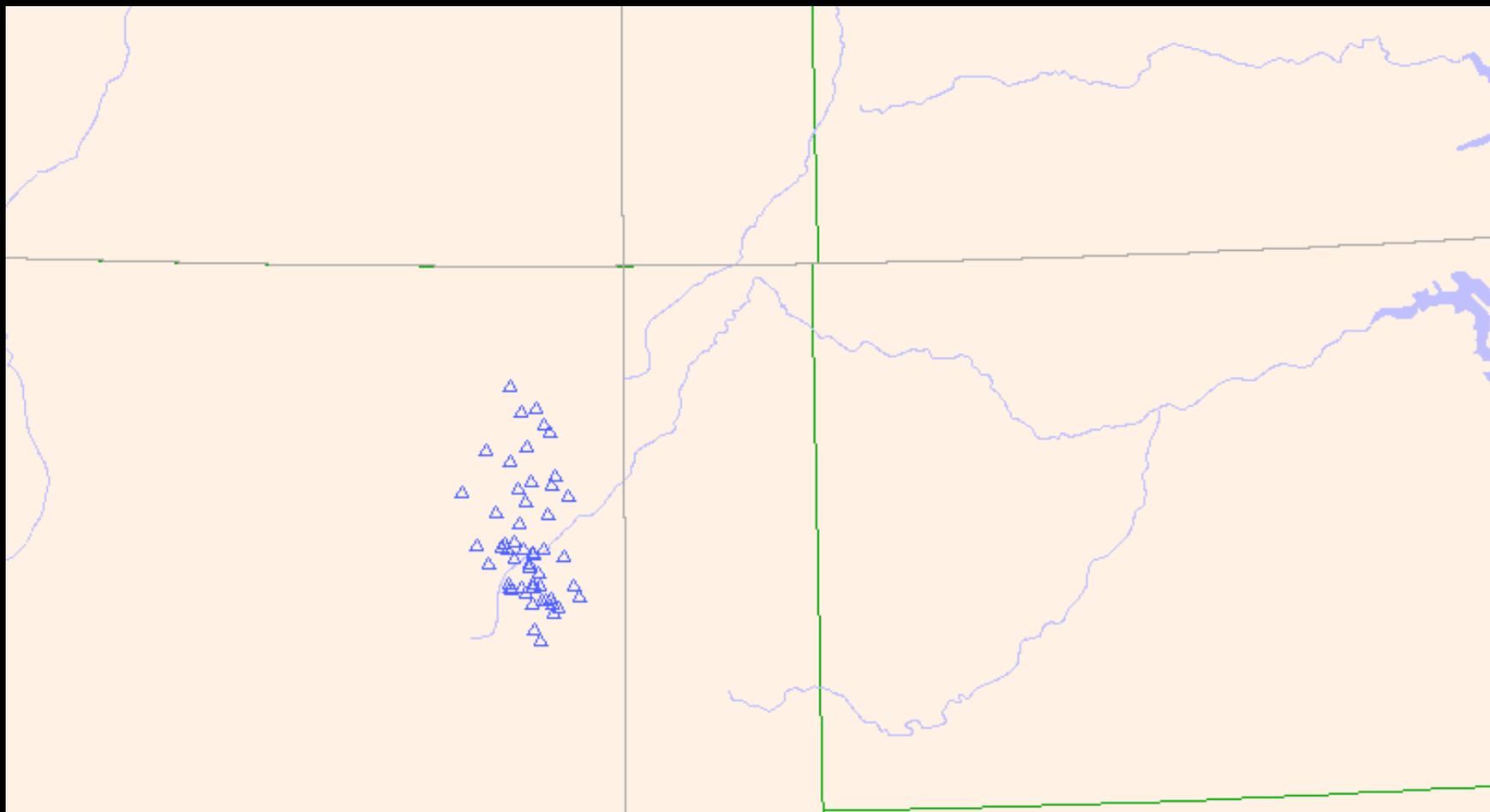
# Data

- 5 mining blasts from coal mines to the west, in Wyoming
- Blasts produced strong surface waves in  $\sim 1-10$  seconds period band, predominantly 2-5 seconds
- Chose seismometers at various depths in the mine

# Data



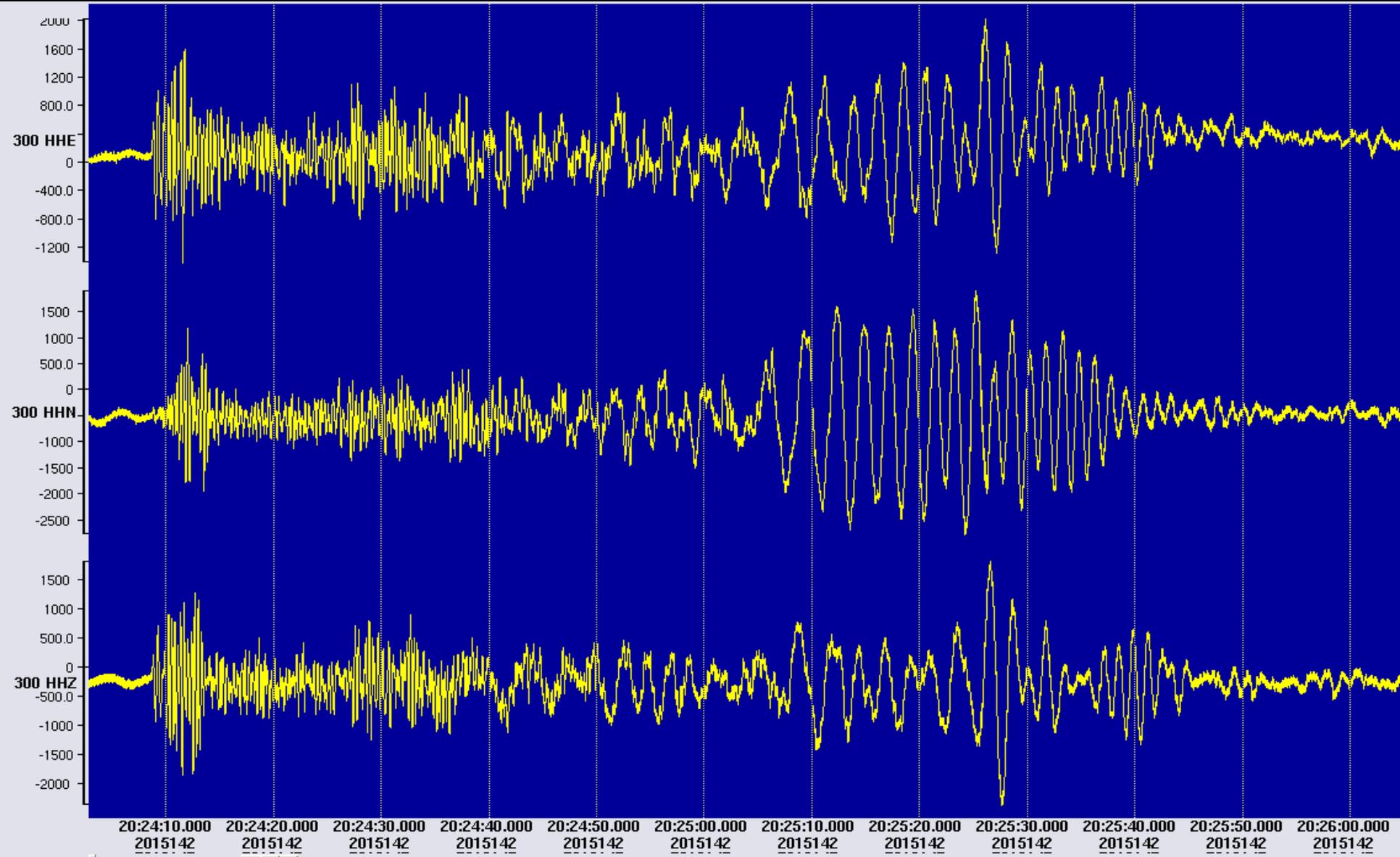
# Data



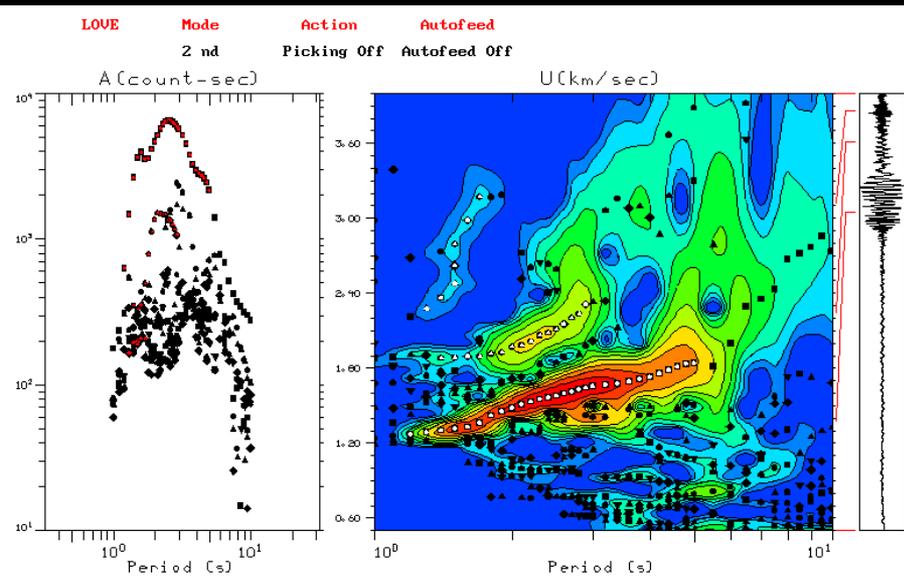
# Methods

- Used `do_mft` for multiple filter analysis
- MFT uses narrowband filters of the form
$$H_n(\omega) = \exp\{-\alpha[(\omega - \omega_n)/\omega_n]^2\}$$
- Amplitudes are calculated by the equation
$$A_n(t) = (h_n^2(t) + q_n^2(t))^{1/2}$$
- $q_n(t)$  is the inverse Fourier transform of
$$Q_n(\omega) = H_n(\omega)F(\omega)\exp(i\pi/2)$$
- First published by Dzierwonski et al. (1969)

# First Event



# First Event



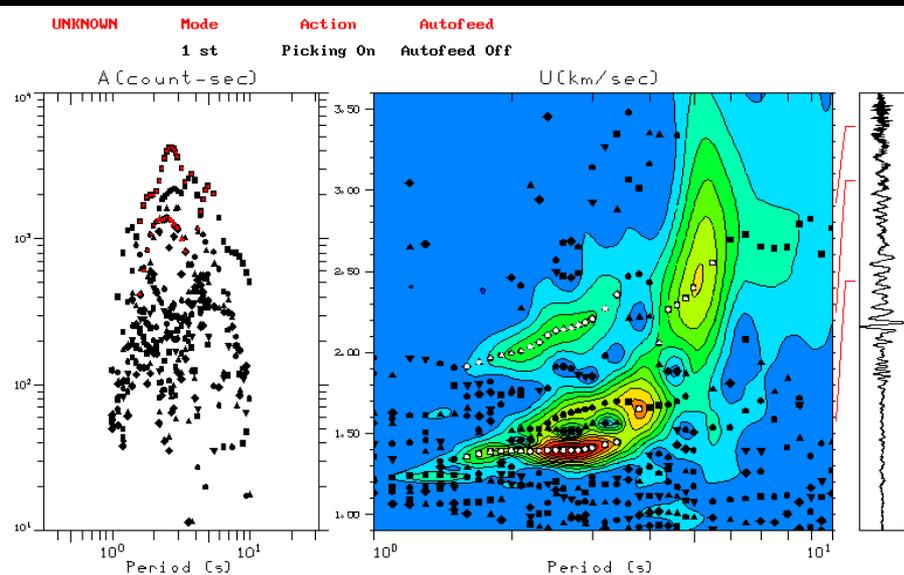
Moderate 1<sup>st</sup> overtone

Possible 2<sup>nd</sup> overtone on E2000

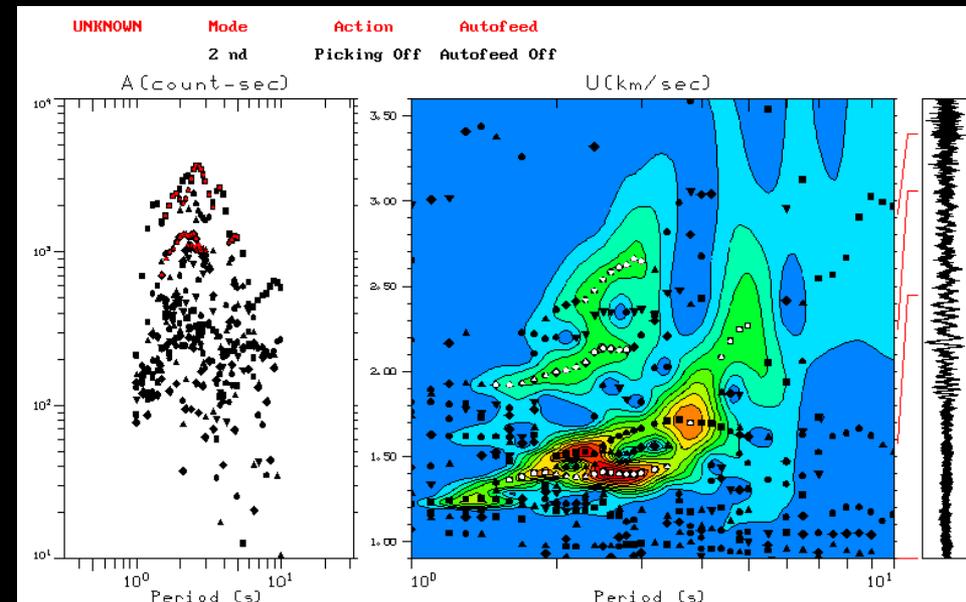
Branched fundamental on E & somewhat on Z (Rayleigh wave)

E channel fundamental changes with depth

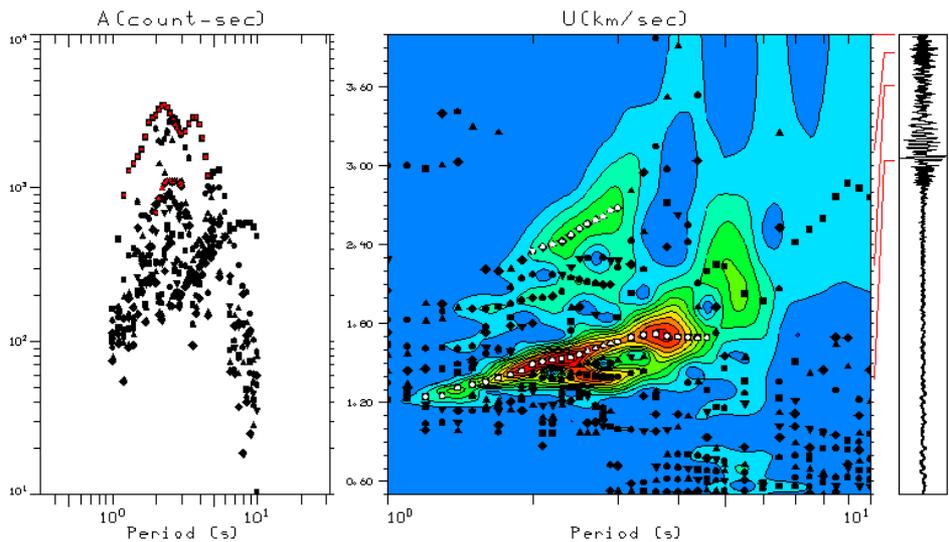
E2000, N (above) & C4850 Z (below)



YATES, E

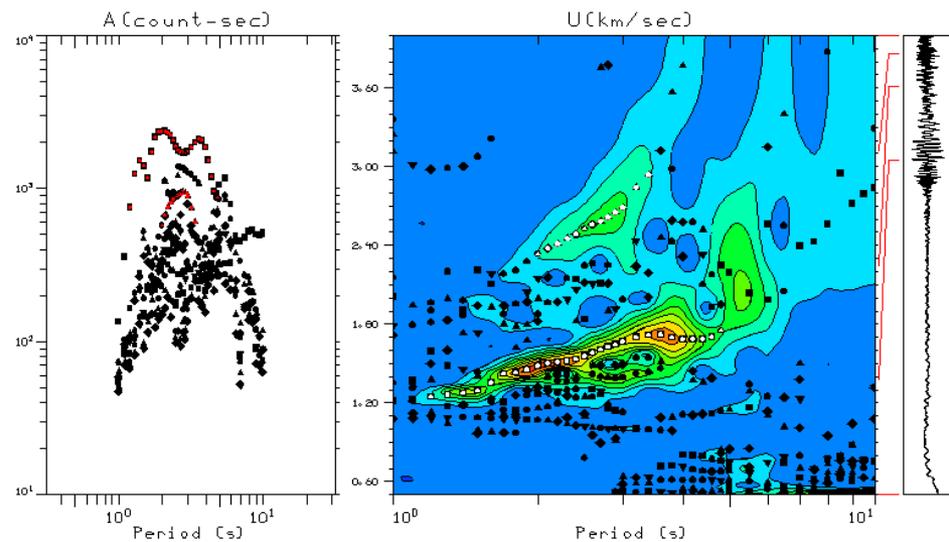


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300, E

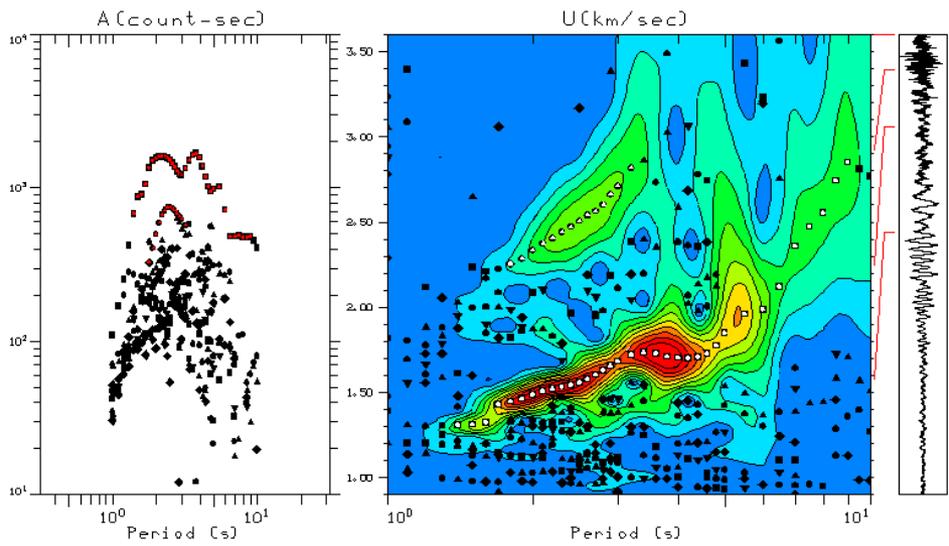
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E2000, E

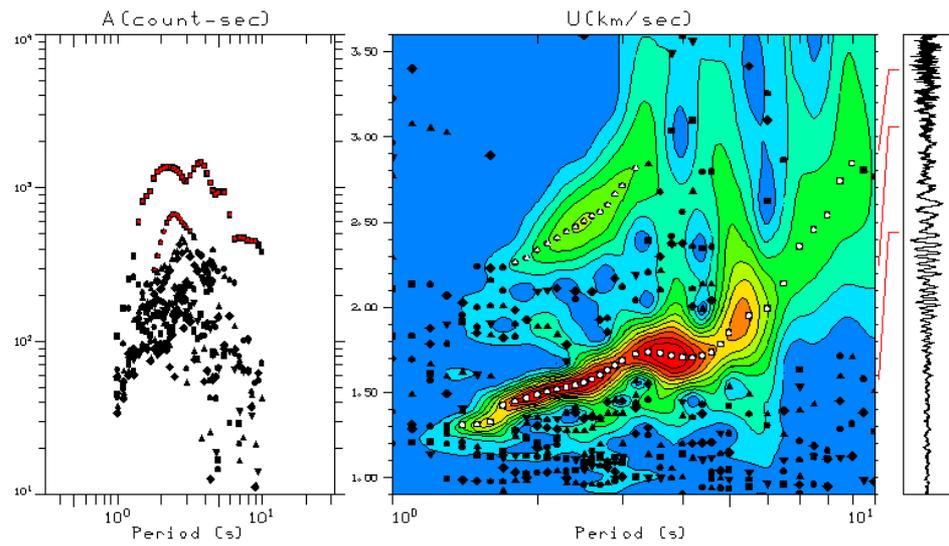
A4100, E

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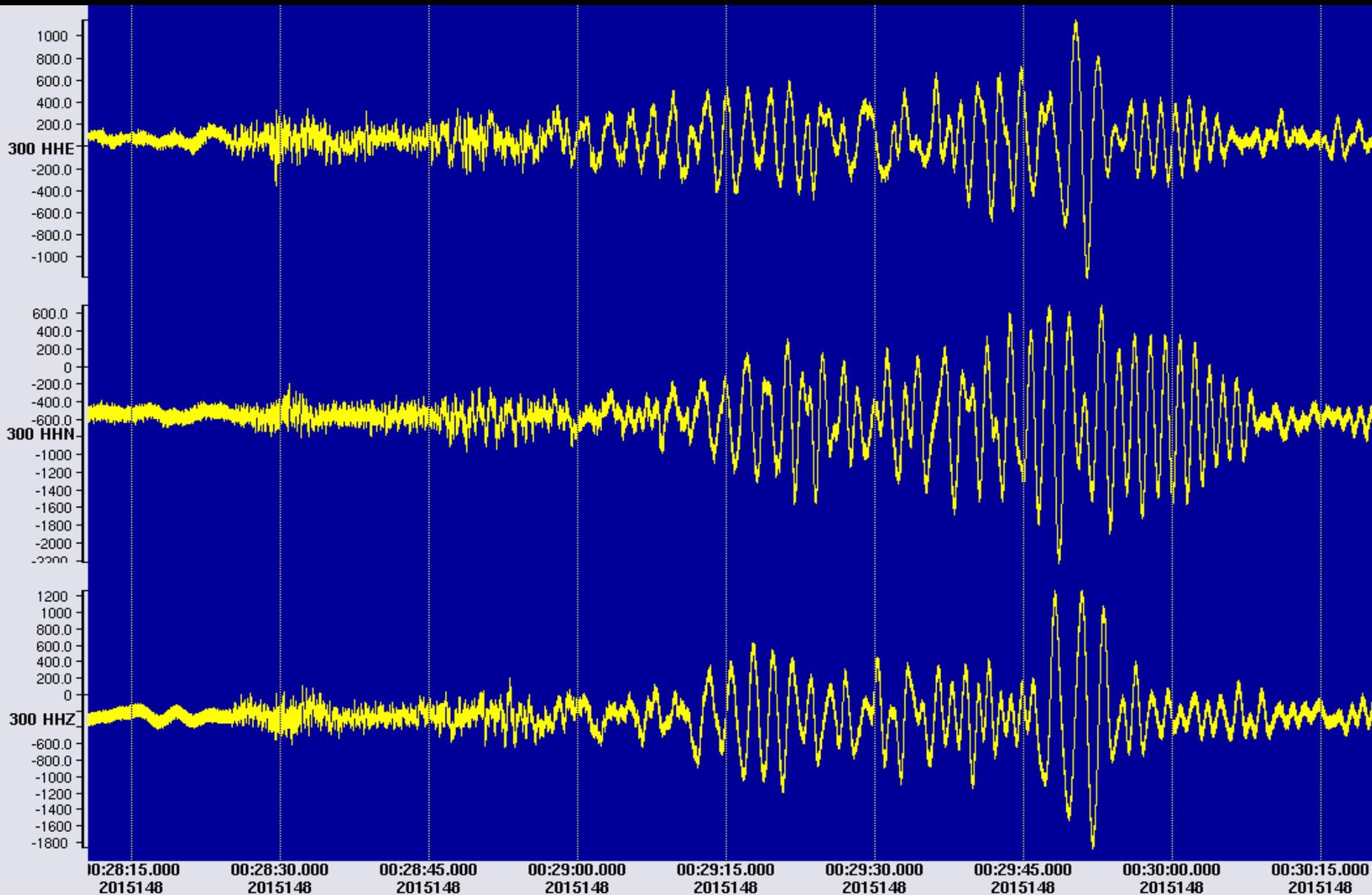


C4850, E

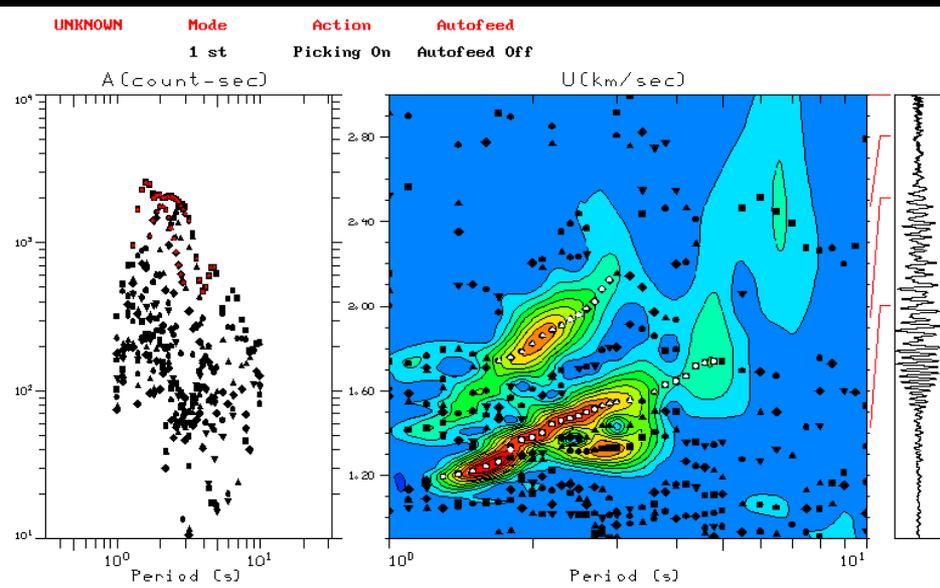
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# Second event



# Second event

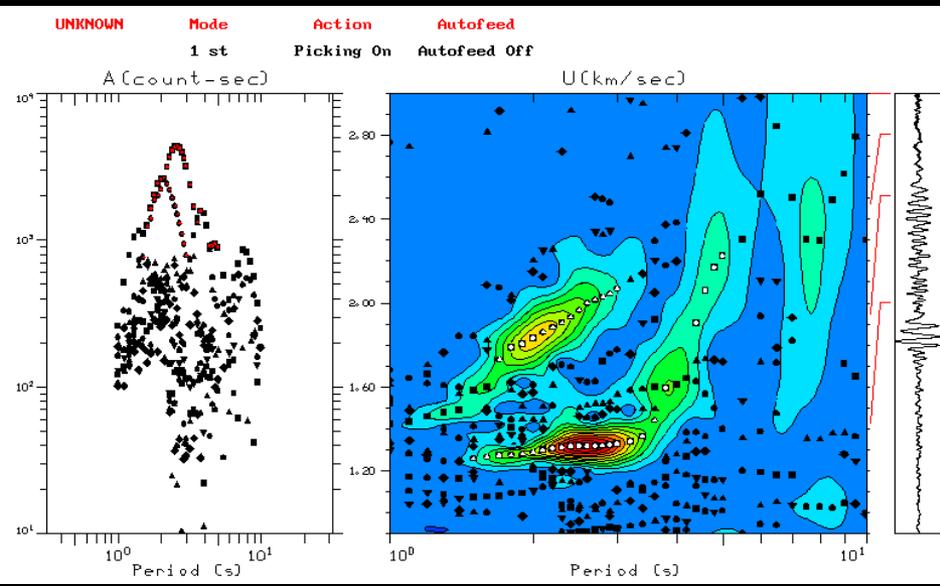


E2000, Z (below) & N (above)

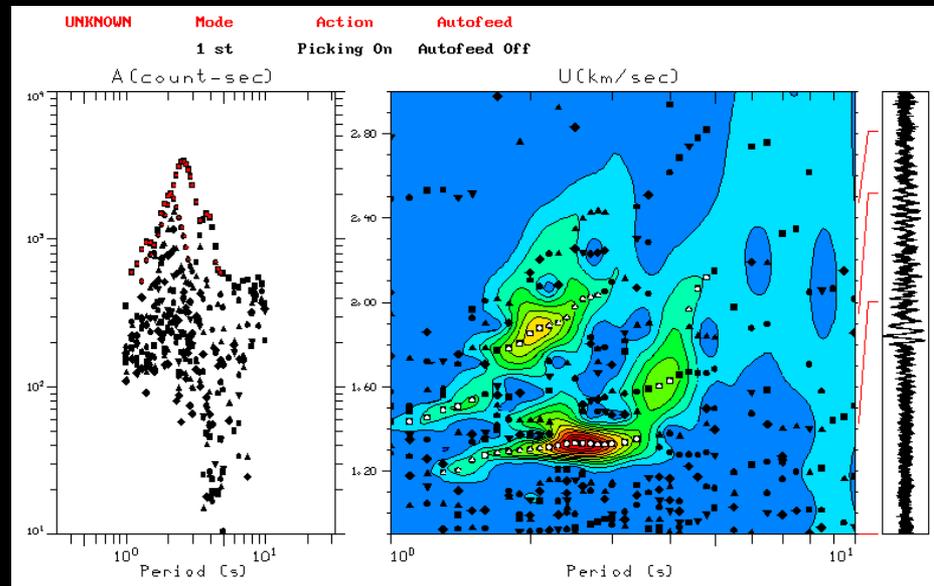
Second event (May 28<sup>th</sup>, 00:27 UTC) shows only one branch on z components, but multiple branches on north components

Stronger 1<sup>st</sup> overtone

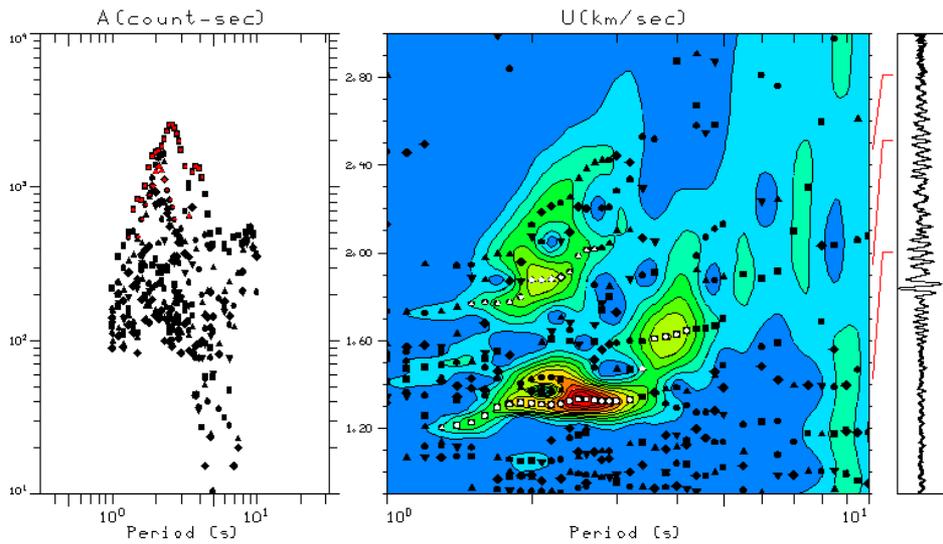
East component fundamental “migrates” with depth



YATES, E



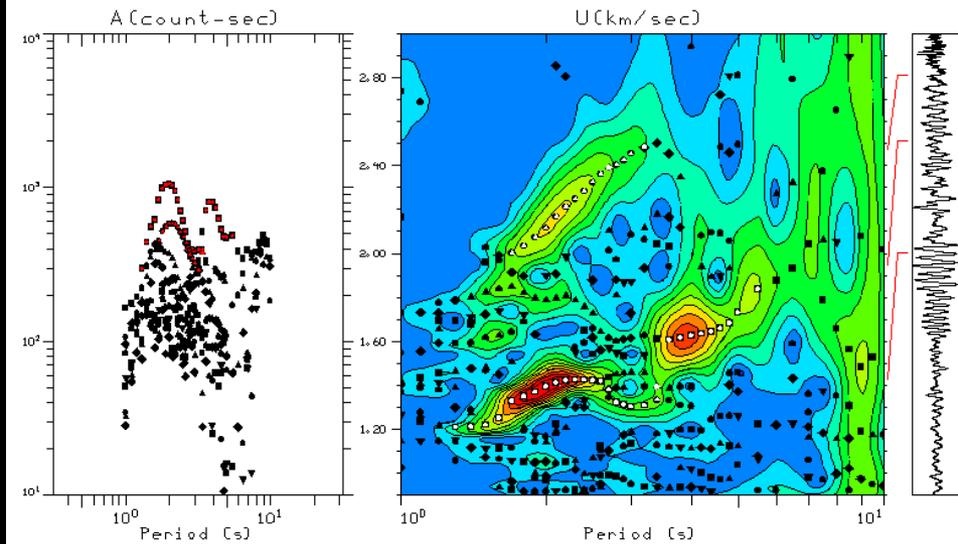
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300, E

E2000, E

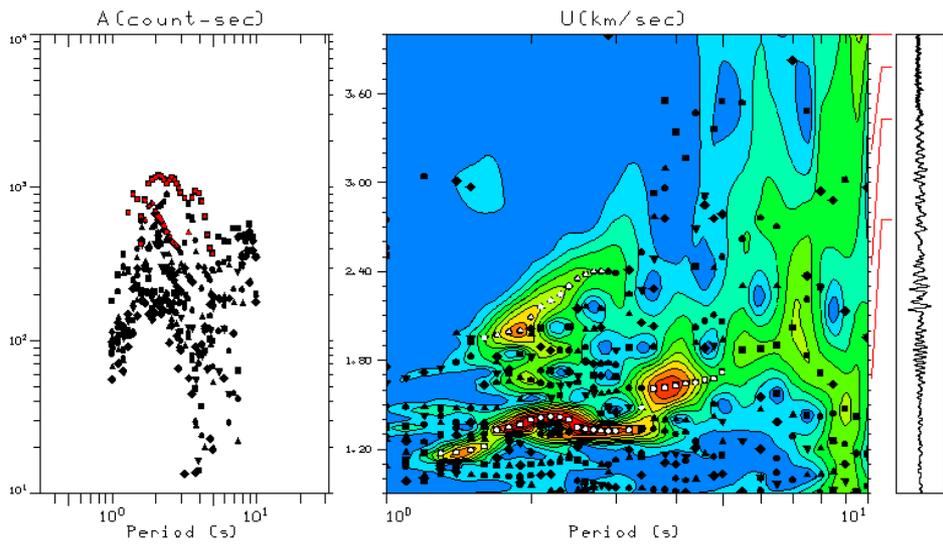
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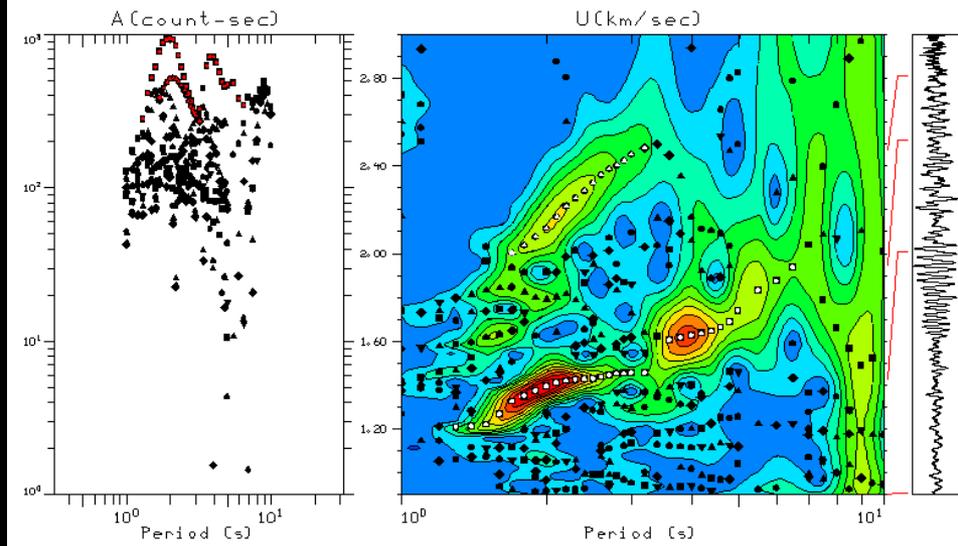
A4100, E

C4850, E

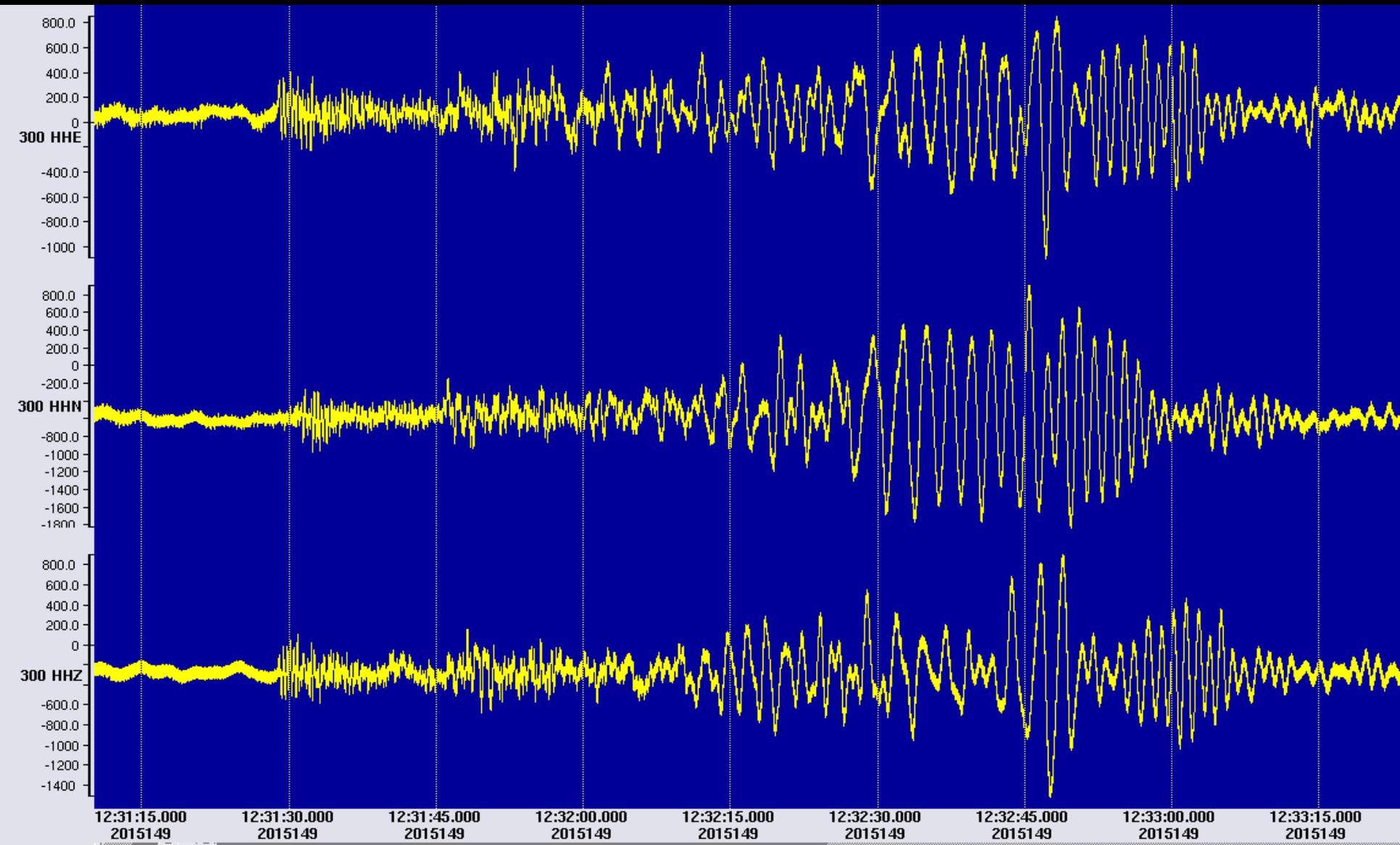
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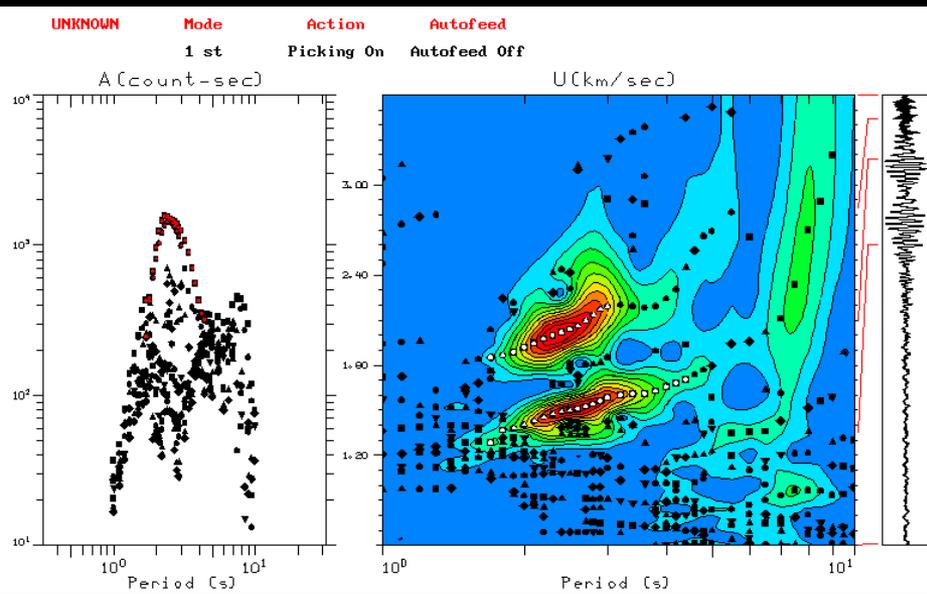
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# Fifth event



# Fifth event

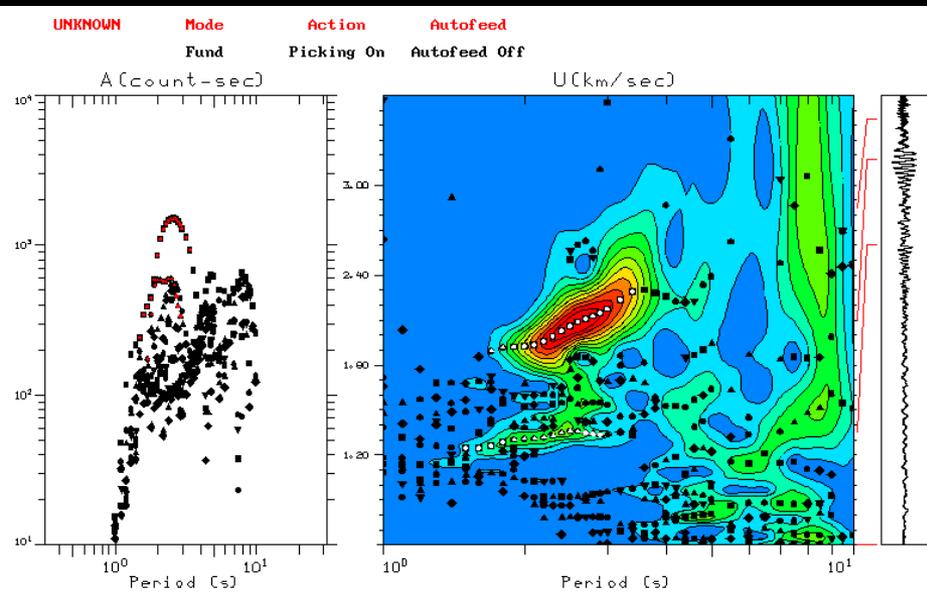


C4850, Z (below) & E2000 N (above)

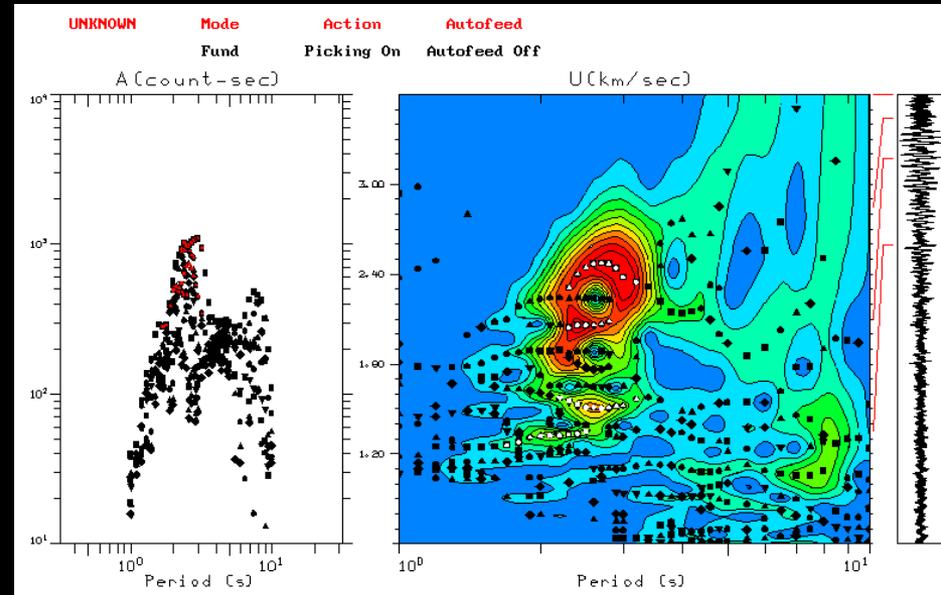
Nearly all Rayleigh energy in 1<sup>st</sup> overtone, very weak fundamental

Spectral hole on east component

Love has strong fundamental and first overtone



300, E



# Discussion

- Branched fundamentals may indicate multipathing
- Since the N components almost never have branched fundamentals, this would suggest a P-velocity anomaly only
- Does not appear to be related to azimuth
  - Events 1 & 2 are  $71^\circ$  and  $70^\circ$ , but look different
  - 1 & 4 look very similar, but are  $71^\circ$  and  $79^\circ$
  - 3 & 5 look very different, but are  $64^\circ$  and  $61^\circ$

# Discussion

- We can also examine the decay of surface waves with depth
- From Stein & Wyession, we know that Rayleigh waves decay as  $\exp(-k_x z)$  in a half-space

# Discussion

- The vanishing branch from the first event decays in a manner expected from a half space
- It has  $c_x \sim 1.4$  km/s and  $T \sim 2.5$ s, implying  $\lambda_x = 3.5$  km and  $k_x = 1.8$  km<sup>-1</sup>
- Decays roughly as  $\exp(-1.8 \text{ km}^{-1} z)$

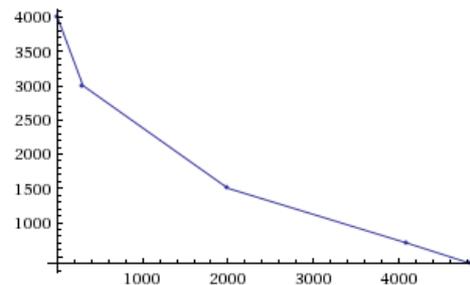
# Discussion

Depth (ft)	Observed amplitude (counts*s)	Predicted amplitude for half-space (counts*s)
0	4000	4000
300	3000	3200
2000	1500	1320
4100	700	400
4850	400	280

Input interpretation:

```
plot {{0, 4 × 103}, {300, 3 × 103},  
      {2000, 1.5 × 103}, {4100, 7 × 102}, {4850, 4 × 102}}
```

Plot:



# References

- Dziewonski, A., Bloch, S., & Landisman, M., 1969. A technique for the analysis of transient seismic signals, *Bull. Seism. Soc. Am.*, **59**, 427-444.
- Stein, S., & Wysession, M., 2003. *An Introduction to Seismology, Earthquakes, and Earth Structure*, Blackwell Publishing, Ltd., Malden, MA.

Questions?